# Density Functional Theory Studies of Csbased Double Perovskites for Solar Cell and Photocatalysis

(太陽電池と光触媒のためのセシウム ベースダブルペロブスカイトの密度汎 関数理論研究)

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### Abstract

In recent years, halide perovskite materials have attracted extensive interests and attention of researchers due to their high optical absorption coefficient, low electron hole recombination rate, long carrier diffusion length and low manufacturing cost. However, most of the highly efficient perovskite photovoltaic materials currently prepared contain heavy metal element lead, which seriously pollutes the environment and limits large-scale commercial application. In addition, perovskite materials are easy to decompose due to the influence of air and water, which restricts the photovoltaic performance. Cesium based double perovskite is expected to solve these problems because of its excellent stability and more choices for lead-free applications. Inspired by the advantages of cesium based double perovskite, our work mainly focuses on the theoretical research on the structural, electronic and optical properties of this kind of perovskites by density functional theory (DFT). The work aims to predict the potential of cesium based halogenated double perovskites in the application of perovskite solar cells and photocatalysis, and to clarify the microscopic physical and chemical mechanisms, thereby providing theoretical guidance for the experimental work.

In chapter 1, the research progress and background of the ABX<sub>3</sub> and Cs<sub>2</sub>BX<sub>6</sub> perovskites were introduced. In addition, the developments and status of perovskite solar cells and photocatalysts were also introduced. Finally, the purpose of this thesis was depicted.

In chapter 2, the detailed descriptions of the theoretical calculation methods were represented. The development process, theoretical framework and some new developments of the first principle theory were introduced. In addition, computational software packages used were briefly introduced.

In chapter 3, we simulated and optimized the structure of the  $Cs_2PtI_{6-y}Cl_y$ ,  $Cs_2PtI_{6-y}Br_y$ , and  $Cs_2PtBr_{6-y}Cl_y$  (y = 0, 1, 2, 3, 4, 5, 6) and systematically studied their electronic properties. The calculated tolerance factor and formation energy revealed good stability for all these compounds. In addition, the substitutional doping of halogen ions can effectively adjust the bandgap and show an obvious trend.

In chapter 4, structural, electronic, and optical properties of 30 kinds of Cs<sub>2</sub>BX<sub>6</sub> compounds were studied by DFT calculation. Theses perovskites with potential application in solar cells and photocatalysts were pre-screened based on bandgap calculation results. After studying the optical

properties and band edge positions, we found 8 kinds of cesium based double perovskites which have the application research value of single junction solar cells and photocatalysts.

In chapter 5, the band structure and density of state (DOS) of  $g-C_3N_4/Cs_2BBr_6$  (B=Pt, Ti, Sn) heterojunctions were studied by DFT. After  $g-C_3N_4$  contacted with double perovskite, the band edge positions of the two semiconductors changed, and then different types of band arrangement were formed due to the interaction between  $g-C_3N_4$  and the perovskite interface. The insight gained of this work is of direct relevance to the design of new catalysts relating to  $g-C_3N_4$  or  $Cs_2BBr_6$ .

Finally, we summarized this thesis and introduced the possible future development direction of related field. Computational techniques of our thesis can provide theoretical guidance for the rational design of Cs based double perovskite materials with improved photovoltaic and photocatalytic characteristics.

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### **Chapter 1. Introduction**

#### **1.1 Research background and significance**

Since the discovery of ABX<sub>3</sub> perovskite materials, people have never stopped their research and exploration. At first, because the development of relevant application fields is not very mature, the research on perovskite materials mainly focuses on structural characteristics, electromagnetic properties, etc.<sup>1,2</sup> In 1993, Helmolt and his research team from Germany found that room temperature magnetoresistance exceeded 60% in perovskite La<sub>2/3</sub>Ba<sub>1/3</sub>MnOx films.<sup>3</sup> Shortly afterwards, Jin and his collaborators in the United States observed a magnetoresistance effect of 99.9% in La<sub>0.67</sub>Ca<sub>0.33</sub>MnOx thin films prepared with PLD.<sup>4</sup> These colossal magnetoresistance (CMR) effects found in the research of perovskite materials have attracted extensive attention and further detailed research.

High temperature superconductors, multiferroic materials, colossal magnetoresistance materials, solar cell materials, and semi metallic magnetic materials are several important research fields in condensed matter physics in recent years. In these fields, some representative materials have perovskite or perovskite like structures. In 1996, Wu et al. reported a perovskite type unconventional high temperature superconductor Sr<sub>2</sub>YRu<sub>1-x</sub>Cu<sub>x</sub>O<sub>6</sub> without copper oxide surface, and its superconducting temperature was as high as 30 K.<sup>5</sup> In 1998, Kobayashi et al found that the double perovskite compound Sr<sub>2</sub>FeMoO<sub>6</sub> has a tunneling magnetoresistance effect at room temperature.<sup>6</sup> In 2015, the first multifarious material LaMn<sub>3</sub>Cr<sub>4</sub>O<sub>12</sub> with cubic perovskite lattice was discovered.<sup>7</sup> In addition, the discovery of a large number of semi metallic magnetic materials with perovskite structure, such as CaFeO<sub>3</sub>,<sup>8</sup> YMnS<sub>3</sub>,<sup>9</sup> NiCrO<sub>3</sub>,<sup>10</sup> Sr<sub>2</sub>NiOsO<sub>6</sub>,<sup>11</sup> has expanded the research field of perovskite to spintronics. In particular, in 2009, Miyasaka and his research team prepared quantum dots of ABX<sub>3</sub> type organic/inorganic hybrid perovskite materials such as CH<sub>3</sub>NH<sub>3</sub>PbI<sub>3</sub> and CH<sub>3</sub>NH<sub>3</sub>PbBr<sub>3</sub>, and applied them to dye sensitized solar cells, achieving a photoelectric conversion efficiency of 3.8%,<sup>12</sup> thus opening the prelude of ABX<sub>3</sub> type perovskite materials in the field of solar cell research and achieving great success.

Although the materials mentioned above have different physical properties, their basic structures can be summarized as ABX<sub>3</sub> perovskite structure or its derivative compounds. At the same time, the strong correlation existing in perovskite materials, especially the inextricable

relationship between structure and physical properties, also deepens people's further understanding of perovskite materials, thus pushing condensed matter physics to a wider and deeper level.

In addition, theoretically, ABX<sub>3</sub> perovskite materials can provide a variety of combinations, thus giving theoretical researchers a wider modeling space. Because the ions at A, B and X sites in ABX<sub>3</sub> perovskite materials have different electronic configurations, different ion radii and different types of exchange effects, it is possible to realize the assumption of a variety of different types of perovskites by changing the types of ions at A, B and X sites. All these provide a relatively perfect theoretical basis for revealing the characteristics of correlation interaction and electron transport in perovskite materials. The research on magnetic, optical and electrical properties of ABX<sub>3</sub> perovskite materials will have broad research prospects and research values.

## **1.2 ABX3 perovskite compounds**



Figure. 1. Scheme of the structure of ABX<sub>3</sub> perovskite.

The structure of perovskite compound is similar to calcium titanate (CaTiO<sub>3</sub>). As a byproduct in alkaline rocks, perovskite is one of the most abundant minerals on the earth. It was first discovered by Gustav Rose, a German mineralogist, in 1839 in the metamorphic rocks of the Ural Mountains in Russia, and later named after Von Perovski, a Russian geologist.<sup>13</sup>

In the narrow sense, perovskite refers to calcium titanate mineral. However, with the improvement of technology, some compounds with similar crystal structure to calcium titanate

have been found and obtained in the laboratory, such as LaMnO<sub>3</sub>, BiFeO<sub>3</sub>, BaTiO<sub>3</sub>, etc. Therefore, the perovskite referred to today is a class of compounds similar to the crystal structure of perovskite. Their chemical composition can be uniformly expressed as ABX<sub>3</sub>, in which A is usually a cation with large radius such as Na<sup>+</sup>, K<sup>+</sup>, Ba<sup>2+</sup>, Sr<sup>2+</sup>, Ca<sup>2+</sup>, etc; B is generally a cation with small radius, such as Nb<sup>5+</sup>, Fe<sup>3+</sup>, Ta<sup>5+</sup>, Th<sup>4+</sup>, Ti<sup>4+</sup>, etc; X is generally an anion, such as O<sup>2-</sup>, F<sup>-</sup>, Br<sup>-</sup>, etc. Since a variety of element atoms with different quantities can be at A, B and X positions, there are many kinds of perovskite compounds, which are widely used in geology and materials science.

Ideally, the crystal structure of ABX<sub>3</sub> perovskite is shown in Figure 1. It belongs to an equiaxed crystal system. The coordinate parameters of each atom in the cell are A (0, 0, 0), B (0.5, 0.5, 0.5) and X (0.5, 0.5, 0), respectively. The space group is Pm $\overline{3}$ m. Its crystal structure can be seen as that the octahedron formed by BX<sub>6</sub> is connected through a common vertex angle. The A cation is located in the center of the void formed by the octahedron, and its coordination number is 12. Since the ionic radii of A and X are very similar, from the view of dense packing, this structure can also be seen as a result of the hexagonal dense packing of the atomic layer formed by A and X along the (111) direction and the filling of octahedral voids by B ions.

For ordinary calcium iron ores, the chemical bonds in the structure are usually ionic bonds. In ionic compounds, the same charges will repel each other, while the opposite charges will attract each other. The hard sphere stacking model shows that the coordination number is usually determined by the radius ratio of positive and negative ions, that is, for a certain crystal structure, if the coordination number of positive and negative ions is determined, the value of the radius ratio of positive and negative ions is determined, the value of the radius ratio of positive and negative ions is determined. If anions and cations with different radii are combined with each other, the symmetry of the perovskite crystals will be different, thus obtaining a variety of perovskite structures with different distortion. Theoretically, the tolerance factor is commonly used to characterize this symmetry relationship of perovskite crystals, and its calculation expression is:<sup>14</sup>

$$\tau = \frac{R_A + R_x}{\sqrt{2}(R_B + R_x)} \tag{1}$$

where  $R_A$ ,  $R_B$  and  $R_X$  denote the ionic radius of the A, B and X in the A<sub>2</sub>BX<sub>6</sub> double perovskite structure, respectively. For most perovskite materials, the crystal structure is not an ideal cubic structure due to the regulation of the radius ratio of anions and cations, and most crystals will deform on the basis of the cubic structure. When  $\tau < 0.77$ , the crystal is ferrotitanium; If  $0.77 < \tau < 1.1$ , the crystal exists as perovskite; When  $\tau > 1.1$ , the crystal exists as aragonite or calcite.<sup>15</sup> Only when the tolerance factor is close to 1 or the crystal is in high temperature environment, the ideal cubic structure will appear.

The crystal structure of ABX<sub>3</sub> semiconductor perovskite determines its bandgap to some extent. Generally speaking, if the ionic radius decreases, the cell volume will shrink, the bandgap will become larger, and the absorption spectrum will shift blue. On the contrary, if the ionic radius is increased, the volume of the cell will expand, resulting in a narrowing of the bandgap and a red shift in the absorption spectrum. To maintain the three-dimensional crystal structure of ABX<sub>3</sub> semiconductor perovskite, it is necessary to ensure that its tolerance factor is between 0.77 and 1.1. At this time, the radii of anions and cations at A, B and X positions must be appropriate. Therefore, in order to form an ideal cubic perovskite and have a bandgap that meets the actual needs, it is necessary to select appropriate anions and cations.<sup>15</sup>

#### 1.3 Cs<sub>2</sub>BX<sub>6</sub> perovskite compounds

Typical perovskite compounds generally have the chemical composition of ABX<sub>3</sub>. Considering the type, quantity, ordered or disordered substitution of A, B and X ions, this ABX<sub>3</sub> type perovskite compound can be divided into many perovskites with different chemical compositions. Some modifications in the basic structure of perovskite, such as  $A_2B^{1+}B^{3+}X_6^{-16}$  and  $A_2B^{4+}X_6^{-16,17}$ , have been reported in the literature. By replacing each pair of adjacent B cations with a B<sup>1+</sup> and a B<sup>3+</sup> cation at the top, the  $A_2B^{1+}B^{3+}X_6$  structure (also known as anorthite) can be considered cubic. In terms of structure, if half of the B cations in the [BX<sub>6</sub>] cluster center are removed, it will be transformed into a double perovskite with the formula of  $A_2BX_6$ , such as  $Cs_2SnI_6$  or  $Cs_2PbBr_6$ , which can be considered as a derivative of ABX<sub>3</sub>, extending the type of cations used for substitution to B site.<sup>18</sup> Generally, it is referred to as antifluorite crystal (K<sub>2</sub>PtCl<sub>6</sub>) and described by the [BX<sub>6</sub>]<sup>2-</sup> octahedral cluster bridged by the A-site cation. The  $A_2BX_6$  structure was shows in Fig. 2 and has similar characteristics to ABX<sub>3</sub> perovskite, most of which have cubic structure.

A new sort of all inorganic Cs based halogenated perovskite has been developed by using oxygen evolution in water recently,<sup>19–21</sup> which effectively improves the thermal stability of the material, thereby prolongs the service life of the equipments.<sup>22</sup> In addition, the introduction of Cs can suppress the phase impurities, permitting the preparation with high purity

and defect-free perovskite films, which is less sensitive to processing conditions. This enables perovskite solar cells device performance to achieve repeatable high efficiency.<sup>23</sup> Recent studies on lead-free perovskite substitutes, especially  $A_2BX_6$ , usually report the synthesis and characterization of bulk powders or single crystals, such as  $Cs_2ZrCl_6$ ,  $Cs_2SnI_6$ ,  $Cs_2TiBr_6$ , and so on.<sup>24-26</sup>



Figure. 2. Scheme of the structure of A<sub>2</sub>BX<sub>6</sub> double perovskite.

#### 1.4 Perovskite solar cell

With the rapid development of human society, people's demand for energy has increased rapidly. The limitation of traditional fossil energy and a series of problems such as environmental pollution and climate warming caused by massive consumption have triggered an urgent demand for sustainable energy. Because of its good cleanliness and inexhaustible characteristics, solar energy has solved the increasingly acute problem of energy depletion and the contradiction between energy and environment. Therefore, how to use solar energy efficiently has become an urgent problem for scientists all over the world. Solar cells realize the conversion of solar energy to electric energy, making it possible for humans to effectively use solar energy. In 1883, Frits et al. prepared the first semiconductor/metal junction solar cell in human history, with a photoelectric conversion efficiency of about 1%.<sup>27</sup> In 1954, Bell Laboratories developed a crystalline silicon solar cell with a photoelectric conversion efficiency of 4.5%. These major events in the field of solar cell research and development have opened the prelude to the use of solar power by human beings.<sup>28</sup>

The development of solar cell technology has mainly gone through three stages: (1) the first generation of solar cells, in which the preparation materials of solar cells are mainly monocrystalline silicon and polycrystalline silicon. At present, the conversion efficiency of monocrystalline silicon solar cells has reached 25%, and the conversion efficiency of polycrystalline silicon solar cells has also exceeded 20%.<sup>29</sup> However, due to the extremely high requirements for the purity of the raw material silicon in the preparation of monocrystalline silicon and polycrystalline silicon solar cells, such cells are very expensive, and their energy consumption is also large. These factors have affected their further commercial applications.<sup>30</sup> (2) In the secondgeneration solar cell stage, which mainly includes thin film cell, such as amorphous silicon and polycrystalline silicon thin film cells. At present, the photoelectric conversion efficiency of such thin film cells also exceeds 20%.<sup>29</sup> This kind of solar cells also faces problems that cannot be solved, such as environmental pollution, high manufacturing cost, and unsustainable.<sup>31</sup> (3) Some third-generation new concept solar cells with high conversion efficiency, such as organic solar cells, dye sensitized cells, etc.<sup>32-34</sup> Among them, some solar cells based on ABX<sub>3</sub> perovskite materials have attracted great attention due to their rich raw materials and low manufacturing costs. In particular, in recent years, people have made a series of major breakthroughs in the research field of organic-inorganic hybrid perovskite solar cell, which makes this kind of perovskite solar cells become one of the research hotspots in the photoelectric field.<sup>35-39</sup>

In 2009, Miyasaka group prepared 9-10 nm quantum dots from organic-inorganic hybrid perovskite materials such as CH<sub>3</sub>NH<sub>3</sub>PbI<sub>3</sub> and CH<sub>3</sub>NH<sub>3</sub>PbBr<sub>3</sub>, and applied them to dye sensitized solar cells, obtaining 3.8% photoelectric conversion efficiency.<sup>35</sup> In 2011, Jeong Hyeok et al. increased the size of CH<sub>3</sub>NH<sub>3</sub>PbI<sub>3</sub> quantum dots to 2-3 nm, and the solar cell efficiency based on the quantum dots was about 6.54%.<sup>36</sup> In 2012, a solid hole conductor material was introduced into perovskite solar cells by scientists, and the efficiency was about 10%.<sup>40</sup> In 2013, people improved the preparation method of perovskite solar cells through sequential deposition, and increased the conversion efficiency of the cells to 15%.<sup>41</sup> In the same year, Lidzey and his collaborators obtained a perovskite type planar heterojunction cell with a conversion efficiency of 15.4% by vapor evaporation.<sup>42</sup> Through the efforts of many scientists, the conversion efficiency of perovskite solar cells has increased to 25.7% this year, as shown in Figure 3.<sup>43</sup>



Figure. 3. Power conversion efficiency of various solar cells.<sup>43</sup>

The structure of the perovskite solar cell is very similar to that of the dye sensitized solar cell because it is improved on the basis of the dye sensitized solar cell. Perovskite solar cells mainly adjust the optical properties by changing the chemical composition of perovskite materials. The main role of perovskite in planar heterojunction solar cells and mesoscopic structure solar cells is light absorber. The components of general perovskite solar cells include counter electrode, conductive glass substrate, hybrid perovskite optical absorption layer, electron transport layer, semiconductor porous film and hole transport layer, as shown in Figure 4.



Figure. 4. Sketch of device structure of a normal PSCs

Solar cells based on organic-inorganic hybrid perovskite have many advantages, such as low price, simple preparation process, high photoelectric conversion efficiency, etc. However, there are still several important factors that restrict the further development of solar cells. These factors mainly include: (1) The absorption spectrum of an ideal solar cell should be relatively wide, for example, it can absorb light waves from visible light to near-infrared wavelength in the range of 350-950 nm. However, due to the influence of the bandgap of perovskite, the light response range of these light absorbing materials based on organic-inorganic hybrid perovskite is relatively narrow. (2) Some existing organic-inorganic hybrid perovskite solar cell with high conversion efficiency contain lead element. Because of the toxicity of lead, it is explicitly prohibited in many countries. How to find a substitute for lead while maintaining high power conversion efficiency is an urgent problem to be solved. (3) The stability of organic-inorganic hybrid perovskite solar cells will be affected not only by the properties of the materials themselves, but also by environmental factors, processing conditions, UV light and other conditions. Therefore, how to improve the stability of organic-inorganic hybrid perovskite solar cells and experimental research.

In a word, it is of great scientific significance to find perovskites with good stability and ideal bandgap for the research and development of solar cells. In this research field, although researchers in various countries have done a lot of work, there is still a lack of strong explanation for some important issues, whether experimental or theoretical, such as authoritative reports on the structural stability of CH<sub>3</sub>NH<sub>3</sub>PbI<sub>3</sub> crystal in theory. On the way to explore new perovskite solar cell materials, in order to avoid a large number of repeated experiments when looking for replacement elements of Pb, it is possible to predict the structure and properties through theoretical simulation, and then conduct targeted experimental research. Due to the complexity of the organic-inorganic hybrid structure, the conclusions of some theoretical and experimental studies are not consistent at present, which requires more reliable calculation methods and more detailed parameter settings to verify the experimental results. Reasonable theoretical predictions are very important for exploring the working mechanism of organic-inorganic hybrid perovskite solar cells and optimizing their photovoltaic performance.

#### 1.5 Perovskite photocatalysis

In solar energy collection, photothermal, photovoltaic and photocatalysis are three different methods, which involve power generation, with an annual growth rate of about 33%.<sup>44</sup> Among them, the fields of photothermal and photovoltaic have been fully established and explored. On

the other hand, photocatalysis is a new field with great potential. It can convert the rich  $H_2O$ ,  $CO_2$ and N<sub>2</sub> on the earth into energy rich products, such as H<sub>2</sub>, CH<sub>4</sub>, CH<sub>3</sub>OH and NH<sub>3</sub>, by using solar energy through processes such as water decomposition to generate H<sub>2</sub>, organic pollutant degradation, CO<sub>2</sub> reduction, N<sub>2</sub> fixation, etc.<sup>45-52</sup> Through these photocatalytic processes, solar energy can be used for wastewater treatment and can be converted into useful chemical fuels such as H<sub>2</sub>, hydrocarbons and NH<sub>3</sub> using different raw materials. Solar light mainly includes three different kinds of energy radiation (ultraviolet (UV), visible light (vis) and near-infrared (NIR)). According to the optical absorption of the working photocatalyst, specific energy radiation can be used in the above photocatalytic process. In order to develop the main part of solar spectrum, it is of great significance to design and develop efficient photocatalysts that can capture visible light and near infrared region. NIR active photocatalysts are of great importance because they can obtain NIR light from the solar spectrum, and because of the high penetration depth of NIR radiation, they can also be used in cloudy days.<sup>53</sup> The use of this highly efficient photocatalyst to collect solar energy from all regions can contribute to global energy security, because it may limit the dependence on non-renewable energy and may combat environmental pollution to limit climate change.

The perovskite oxides (ABO<sub>3</sub>) are originated from CaTiO<sub>3</sub> and are widely studied for various photocatalytic applications owing to their high stability, adjustable structures, and excellent photocatalytic activity. Several kinds of element can be adjusted at A and B-sites resulting in a huge family.<sup>54</sup> The availability of these different sites allows the researchers to replace or dope different elements and to fabricate new materials with high photocatalytic activity. In addition, the substitution or doping of cations at A and B sites with other elements leads to changes in composition and symmetry, leading to the formation of cations or oxygen vacancies, which seriously affects the band structure, light absorption, adsorption and photocatalytic performance of perovskite materials. In addition, O-site doping can also change the bandgap, thereby changing the optical properties of perovskites. Therefore, the photocatalytic activity of perovskite materials can be easily adjusted. Different nanostructures, composites and heterojunctions can also be prepared by using different modification sites.<sup>55, 56</sup>

#### **1.6 Challenges and motivation of this thesis**

As mentioned above, perovskite solar cells are the most promising and most likely to be

commercialized third generation solar cells. Due to the existence of organic cations, the thermal stability of organic-inorganic hybrid perovskite solar cells is not ideal. All inorganic devices exhibit excellent thermal stability when substituted with Cs ions. In addition, the toxicity of lead ions in halide perovskite absorption materials is the main bottleneck in practical applications. Perovskite composed of other divalent cations instead of lead may have poor photoelectric properties due to its large band gap. Therefore, attempts have been made to explore the perovskite like structure through double perovskite. Cs<sub>2</sub>BX<sub>6</sub>, a new type of perovskite, provides a new idea for researchers to prepare green materials without loss of photoelectric properties, and shows excellent stability in light, humidity and temperature.

Recently, these lead halide double perovskites have been extended to the field of photocatalysis. Various lead halide double perovskite and its composites have been studied to improve their hydrogen evolution performance. Through the construction of heterojunction, the charge separation between double perovskite and g-C<sub>3</sub>N<sub>4</sub> is significantly promoted, and the photocatalytic activity can be effectively improved under visible light irradiation. Heterojunction between perovskite and other semiconductor materials can effectively promote charge separation and maintain the stability of photocatalyst.

There are few studies to predict the properties of cesium based halogenated double perovskites through simulation calculation. The potential application of these materials in solar cells and photocatalysts is worth exploring. The results of theoretical calculation can provide a rough prediction for experimental work, reduce the time cost of experimental exploration, and make the experiment more purposeful. In order to solve the above problems, the following three attempts have been made in this thesis. Firstly, we have successfully investigated the structure, stability and electronic properties of Cs<sub>2</sub>PtBr<sub>y</sub>Cl<sub>6-y</sub>, Cs<sub>2</sub>PtI<sub>y</sub>Br<sub>6-y</sub>, and Cs<sub>2</sub>PtI<sub>y</sub>Cl<sub>6-y</sub> (y = 0, 1, 2, 3, 4, 5, 6) using DFT calculations. The general trends in bandgaps and stability are anticipated to provide a guideline for the design of novel stable inorganic halide perovskite materials with ideal properties. Secondly, the structural, electronic, and optical properties of Cs<sub>2</sub>BX<sub>6</sub> compounds were calculated using first-principles calculations of Perdew–Burke–Ernzerhof (PBE) and Heyd–Scuseria–Ernzerhof (HSE) with spin-orbit coupling (SOC) methods, with 30 combinations of B = Ti, Zr, Ge, Hf, Pd, Te, Mo, Sn, Pt, and Pb cations, X = Cl, Br, and I halogen ion. Cs<sub>2</sub>Til<sub>6</sub>, Cs<sub>2</sub>GeBr<sub>6</sub>, Cs<sub>2</sub>PtI<sub>6</sub>, Cs<sub>2</sub>PdBr<sub>6</sub>, and Cs<sub>2</sub>TiBr<sub>6</sub>, Cs<sub>2</sub>SnBr<sub>6</sub>, and Cs<sub>2</sub>PtBr<sub>6</sub> for solar cell applications. The band edge positions of Cs<sub>2</sub>TeI<sub>6</sub>, Cs<sub>2</sub>SnBr<sub>6</sub>, and Cs<sub>2</sub>PtBr<sub>6</sub> for solar cell applications.

matched the water redox potential. Thirdly, the structural, electronic properties and photocatalytic mechanism of  $g-C_3N_4/Cs_2BBr_6$  (B= Pt, Sn, Ti) are systematically investigated by performing first-principles calculations. Our calculation results show that the  $g-C_3N_4/Cs_2PtBr_6$  and  $g-C_3N_4/Cs_2SnBr_6$  heterojunction forms staggered band arrangement. The  $g-C_3N_4/Cs_2TiBr_6$  forms a straddling gap heterojunction after contact.

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### **Chapter 2. Fundamentals of theoretical calculation**

In this chapter, we will introduce the theoretical framework of density functional theory (DFT), as well as some recent developments. Here, Schrodinger equation theory is introduced, followed by the theory and derivation of DFT. Then we will introduce the Hartree Fock equation and Kohn Sham (KS) equation, exchange correlation functional approximation and plane wave basis set. The time-dependent density functional theory will also be briefly understood. Finally, some software packages used in this paper are introduced.

#### **2.1 Density functional theory**

With the development of computer technology and the improvement of computing performance, many quantitative software simulating material properties have emerged, most of which are developed based on DFT. The DFT is one of the important methods to deal with the energy theory of multi particle systems, and it is also considered to be one of the most effective tools to analyze the electronic and structural properties of solids. The important task of the band theory of solid is to determine the energy level of electrons, and the knowledge of band theory of solid can explain the basic physical properties of solids. Therefore, the band theory of solids one of the most important theories in condensed matter physics research. Solid materials contain a large number of atomic nuclei and extranuclear electrons, which constitute a very complex multi particle and multi electron system. In order to determine the basic idea of DFT in dealing with such problems is to separate the motion of atomic nucleus and external electrons in solid by adiabatic approximation, and then simplify the multi electron problem into a single electron problem by Hartree Fock approximation. This chapter will briefly introduce some basic theories and ideas of density functional theory.

#### 2.2 Schrodinger equation of multi particle system

The solid material can be regarded as a system composed of atomic nucleus and external electrons, and its total Schrodinger equation can be expressed as:<sup>1</sup>

$$H\Psi(\vec{r},\vec{R}) = E^H \Psi(\vec{r},\vec{R}) \tag{1}$$

In the above formula,  $\vec{R}$  represents the set of coordinates of all atomic nuclei in the multi particle system.  $\vec{r}$  corresponds to the set of all extranuclear electronic coordinates in the system. In the absence of an external field, the Hamiltonian of a multiparticle system should include three parts: The total energy of electrons in the system  $(H_e)$ , the total energy of atomic nuclei  $(H_N)$  and the total energy generated by the interaction between atomic nuclei and electrons  $(H_{e-N})$ . Therefore, the Hamiltonian expansion of the multi particle system is

$$H = H_e + H_N + H_{e-N} \tag{2}$$

The Hamiltonian  $H_e$  of an electron can be expressed as the sum of the kinetic energy of all electrons and the Coulomb potential energy between all electrons, that is

$$H_{e} = T_{e}(\vec{r}) + V_{e}(\vec{r}) = -\sum_{i} \frac{\hbar^{2}}{2m} \nabla_{r_{i}}^{2} + \frac{1}{2} \sum_{i \neq i'} \frac{e^{2}}{|r_{i} - r_{j}|}$$
(3)

In formula (3),  $\hbar$  is the reduced Planck constant, *m* is the electron mass, and *e* is the electron electric quantity. Similarly, the Hamiltonian of atomic nuclei can be expanded as the sum of kinetic energy and interaction potential energy of all atomic nuclei:

$$H_{N} = T_{N}(\vec{R}) + V_{N}(\vec{R}) = -\sum_{j} \frac{\hbar^{2}}{2M_{j}} \nabla_{R_{j}}^{2} + \frac{1}{2} \sum_{j \neq j'} V_{N}(\vec{R}_{j} - \vec{R}_{j'})$$
(4)

In Formula (4),  $M_j$  is the mass of the *j*th nucleus. It can be seen that the formula does not give a specific expression of the potential energy of the interaction between atomic nuclei, but shows that the amount is related to the relative position of atomic nuclei. The potential energy of electron nucleus interaction in multi particle system can be written:

$$H_{e-N}(\vec{r},\vec{R}) = -\sum_{i,j} V_{e-N}(\vec{r}_i - \vec{R}_j)$$
(5)

Although Formula (1) - (5) can well describe the state of the multi particle system, it is very difficult to directly solve the Schrodinger equation due to the large number of particles and complex interactions in the multi particle system, so it needs to be approximated and simplified.

#### 2.3 Born-Oppenheimer approximation

In the multi particle system, the mass of the electron is far less than that of the atomic nucleus (about one thousandth), and the movement of the atomic nucleus is much slower than that of the

electron. Therefore, it can be considered that the atomic nucleus only makes small vibration near the equilibrium position, while the electron moves at a high speed outside the nucleus; Whenever the nucleus produces a small movement, the electrons around it can always be rapidly adjusted to a new equilibrium state. In this case, the motion of the nucleus and the electron in the multi particle system is considered to be independent of each other and can be treated separately: when studying the motion of the nucleus, the specific position of the electron in space need not be considered; When the motion of electrons is considered, the nucleus can be considered as stationary (instantaneous stationary). This approximate treatment method was proposed by German theoretical physicist Born and American physicist Oppenheimer, so it is called Born Oppenheimer approximation, also known as adiabatic approximation.<sup>2</sup>

Under the condition that only the motion of electrons is considered, the atomic nucleus can be regarded as static, the kinetic energy is zero, the multi particle system is simplified to the multi electron system, and the Hamiltonian and the corresponding Schrodinger equation can be written

$$H_0(\vec{r}, \vec{R}) = H_e(\vec{r}) + V_N(\vec{R}) + H_{e-N}(\vec{r}, \vec{R})$$
(6)

$$H_{0}(\vec{r},\vec{R})\Phi_{n}(\vec{r},\vec{R}) = E_{n}(\vec{R})\Phi_{n}(\vec{r},\vec{R})$$
(7)

Where *n* is the quantum number of the electronic state, the parameter  $\vec{R}$  in the electronic wave function  $\Phi_n(\vec{r}, \vec{R})$  corresponds to the instantaneous position coordinate of the atomic nucleus, and the kinetic energy of the atomic nucleus can also be reintroduced as a perturbation.

#### 2.4 Hartree-Fock (HF) approximation

Although the multi particle system has been successfully simplified into a multi electron system through the Born Oppenheimer approximation, due to the complex electron-electron interaction, it is still difficult to solve the Schrodinger equation of the multi electron system. In the multi electron system, any electron can be regarded as moving in the equivalent potential field generated by other electrons. The interaction energy between the electron and all other electrons is only related to the position of the electron. In 1928, Hartree of St. John's College proposed that the multi electron problem can be transformed into a single electron problem by averaging the Coulomb interaction between electrons (mean field).<sup>3</sup> Therefore, the wave function of the multi electron system can be expanded as the product of the single electron wave function, namely,

$$\phi(r) = \varphi_1(r_1)\varphi_2(r)\varphi_3(r_3)\cdots\varphi_n(r_n) \tag{8}$$

The above equation is also called Hartree wave function. Substitute equation (8) into the Schrodinger equation of multi electron system, and obtain the single electron equation by separating variables:

$$\left[ -\nabla^2 + V(\vec{r}) + \sum_{i'(\neq i)} \int d\vec{r}' \frac{|\varphi_{i'}(\vec{r}')|^2}{|\vec{r}' - \vec{r}|} \right] \varphi_i(\vec{r}) = E_i \varphi_i(\vec{r})$$
(9)

The above equation, also known as Hartree equation, describes the motion of a single electron (coordinate  $\vec{r}$ ) in the lattice potential  $V(\vec{r})$  and the average potential generated by all other electrons.

Although Hartree wave function satisfies Pauli exclusion principle and each electron has different quantum states, it ignores the Fermion property of the electron: when exchanging positions, the wave function of the electron must satisfy antisymmetry. In 1930, Fock used a series of linear combinations of single electron wave functions satisfying the commutative antisymmetry to represent the multi electron wave functions:<sup>4</sup>

$$\phi = \frac{1}{\sqrt{N!}} \begin{vmatrix} \varphi_{1}(\vec{q}_{1}) & \varphi_{2}(\vec{q}_{2}) & \cdots & \varphi_{N}(\vec{q}_{1}) \\ \varphi_{1}(\vec{q}_{2}) & \varphi_{2}(\vec{q}_{2}) & \cdots & \varphi_{N}(\vec{q}_{2}) \\ \vdots \\ \varphi_{1}(\vec{q}_{N}) & \varphi_{2}(\vec{q}_{N}) & \cdots & \varphi_{N}(\vec{q}_{N}) \end{vmatrix}$$
(10)

Where  $\vec{q}_i$  is the electron coordinate and is a function of position  $\vec{r}_i$  and spin. Hartree Fock equation of single electron can be written:

$$\left[-\nabla^{2} + V(\vec{r}) + \sum \int d\vec{r}' \frac{\rho(\vec{r}') - \rho_{i}^{HF}(\vec{r}, \vec{r}')}{\left|\vec{r}' - \vec{r}\right|}\right] \varphi_{i}(\vec{r}) = E_{i} \varphi_{i}(\vec{r})$$
(11)

Since the orthogonality of the spin function leads to the sum of spins equal to zero,  $\vec{r_i}$  is used instead of  $\vec{q_i}$  in the above equation.

In Formula 11, the last two terms on the left are only related to the position vector  $\vec{r_i}$  of the electron, which can be represented by a Coulomb effective potential field  $V_{eff}(\vec{r})$  uniformly distributed for all electrons:

$$\left[-\nabla^2 + V_{eff}(\vec{r})\right]\varphi_i(\vec{r}) = E_i\varphi_i(\vec{r})$$
(12)

Through Hartree Fock approximation, Schrodinger equation based on single electron effective potential can be used to replace Schrodinger equation of multi electron system. However, Hartree Fock approximation ignores the spin antiparallel repulsion between electrons and only considers the exchange interaction between electrons, so it cannot be used to strictly solve the single electron Schrodinger equation.

#### 2.5 Hohenberg Kohn (HK) theorem

Hohenberg and Kohn proved two basic theorems in the study of non-uniform electron gas, which laid the foundation of DFT:<sup>5</sup>

Theorem 1: The ground state energy of the identical Fermion system without spin is the only functional of the particle number density function  $\rho(\vec{r})$ .

The particle number density here is defined as

$$\rho(\vec{r}) = \left\langle \Phi \middle| \Psi^{+}(\vec{r})\Psi(\vec{r}) \middle| \Phi \right\rangle \tag{13}$$

Where  $\Phi$  is the ground state wave function. Theorem 1 points out that the particle number density is a basic variable that determines the physical properties of the ground state of the multi particle system. Once the density function is determined, all the ground state properties of the system, including energy, wave function, etc., can be uniquely determined.

Theorem 2: When the number of particles is constant, the energy functional  $E[\rho(\vec{r})]$  finds the extreme value of the particle number density function  $\rho(\vec{r})$ , which is equal to the ground state energy.

For a given local potential  $v(\vec{r})$ , the energy functional  $E[\rho(\vec{r})]$  is defined as

$$E[\rho(\vec{r})] = \int d\vec{r} v(\vec{r}) \,\rho(\vec{r}) + \left\langle \Phi \left| T + U \right| \Phi \right\rangle \tag{14}$$

#### 2.6 Kohn Sham (KS) equation

In the previous section, we mentioned that based on the HK theorem, the Hamiltonian of the system is unknown because of the kinetic energy functional of interaction and the form of electronic interaction. In order to solve the Schrodinger equation of the system, Kohn and Sham

simplified the interaction system as non-interaction.<sup>5</sup> Finally, the mathematical expression of Kohn Sham equation can be obtained:

$$\left\{-\nabla^2 + v(\vec{r}) + \int d\vec{r}' \frac{\rho(\vec{r}')}{|r-r'|} + \frac{\delta E_{xx}\left[\rho(\vec{r})\right]}{\delta\rho(\vec{r})}\right\} \psi_i(\vec{r}) = E \psi_i(\vec{r})$$
(15)

Where the effective potential is

$$V_{KS}(\vec{r}) = v(\vec{r}) + \int d\vec{r}' \frac{\rho(\vec{r}')}{|r - r'|} + \frac{\delta E_{xc} \left[\rho(\vec{r})\right]}{\delta \rho(\vec{r})} = v(\vec{r}) + V_{coul} \left[\rho(\vec{r})\right] + V_{xc} \left[\rho(\vec{r})\right]$$
(16)

Compared with Hartree Fock approximation, KS equation is derived from DFT theory and is accurate. The only item that cannot be determined is the exchange correlation item (XC) that contains all complex interactions. If the exact exchange correlation potential can be obtained, the exact ground state properties of the system can be solved by KS equation.

#### 2.7 Exchange correlation potential

As discussed above, the solution of DFT finally focuses on the construction of exchange correlation potential. In general, the exchange correlation potential is related to the charge density distribution. In a broad sense, the exchange correlation potential is not local, but describes the properties of the spatial distribution, which makes it difficult to accurately construct the exchange correlation potential. So far, two mainstream approximation methods have been developed. The first is the local density approximation (LDA).<sup>6</sup> The second is the generalized gradient approximation (GGA).<sup>7</sup>

LDA regards the space charge density as a slow and continuous change function. This method simplifies the non-uniform electron gas system to a homogeneous case, and its exchange correlation potential has the following form:

$$E_{xc} \cong E_{xc}^{LDA} = \int \rho(\vec{r}) \varepsilon_{xc} \left[\rho(\vec{r})\right] d\vec{r} \tag{17}$$

Where  $\varepsilon_{xc}[\rho(\vec{r})]$  is the local exchange correlation energy density. In the local density approximation, the exchange correlation energy  $E_{xc}^{LDA}$  is decomposed into the exchange energy  $E_x$  and the correlation energy  $E_c$ . The former generally adopts the results of the homogeneous electron gas

model directly, while the expression of the latter needs to be obtained through quantum Monte Carlo simulation of the homogeneous electron gas model.

LDA method is relatively simple, and satisfactory results are obtained for systems with uniform electron density distribution, such as simple metals. However, because only the local charge distribution is considered, when dealing with systems with obvious changes in charge density, such as macromolecular systems, crystals dominated by covalent bonds, the calculated results have a large deviation from the actual values.

LDA neglects the interaction between various local electron gases, which leads to deviation in the calculation results. On the basis of LDA, GGA fully considers the interaction between different regions, and adds a gradient correction term to the exchange correlation functional that represents the charge density of the non-uniformity of the charge distribution. The exchange correlation energy of generalized gradient approximation can be written as:

$$E_{xc} \cong E_{xc}^{GGA} = \int \rho(\vec{r}) \varepsilon_{xc} \left[ \rho(\vec{r}), \nabla \rho(\vec{r}) \right] d\vec{r}$$
<sup>(18)</sup>

In general, due to the correction of the non-uniformity of the charge density distribution, the results given by GGA are closer to the actual values for covalent crystals, macromolecules and other heterogeneous systems. However, it should be noted that GGA is not better than LDA in all cases, and the computation time of GGA will increase significantly.

#### 2.8 Hybrid functional method

When calculating the electronic structure, there is no way to offset the correlation term and the exchange term, thus causing a large error. Using the hybrid functional method, the exact exchange term of Hartree Fock is added to the expression of the exchange correlation potential. Such hybrid functional forms include B3LYP, HSE03, HSE06, etc. At present, HSE06 is a hybrid functional that can more accurately describe the electronic structure of semiconductor. <sup>8</sup> The semi local GGA is expanded in a non-local way, and the exchange correlation energy of the hybrid functional is expressed as:

$$E_{XC}^{HSE} = \frac{1}{4} E_X^{SR}(\mu) + \frac{3}{4} E_X^{PBE,SR}(\mu) + E_X^{PBE,LR}(\mu) + E_C^{PBE}$$
(19)

Where  $\mu$  is the shielding parameter, and the superscript SR/LR corresponds to the short range/long range action respectively. When the mixed parameter is 0, the HSE functional degenerates into Perdew–Burke–Ernzerhof (PBE) functional. When the shielding parameter  $\mu$  tends to zero, the HSE functional is called PBE0 functional, while when the shielding parameter  $\mu$  tends to infinity, the HSE functional still degenerates into PBE functional

#### 2.9 VASP Package Introduction

VASP, fully known as Vienna ab initio Simulation Package, is a software package developed by the University of Vienna for electronic structure and ab initio molecular dynamics calculation and simulation, and is currently the most commonly used commercial software for computing condensed matter physics and computational material science. VASP obtains the wave function and energy of the system by approximately solving Schrodinger equation. VASP is based on the calculation of the pseudo potential plane wave basis set.<sup>9,10</sup> It uses the method of mode conservation pseudo potential, ultra-soft pseudo potential, and projection plus plane wave to express the pseudo interaction between electrons and ion entities. It uses the matrix diagonalization technique to solve the ground state wave function of electrons. The mixed density scheme of Pulay and Broyden is applied in the iterative solution, so as to accelerate the energy convergence of the self-consistent cycle. The main functions of VASP:

Periodic boundary conditions or supercell models are applied to deal with atoms, molecules, clusters, nanowires, films, surface systems and solids, specifically as follows: (1) atomic geometric structure parameters of materials: such as lattice constant, bond length, bond angle, atomic position, etc. (2) Mechanical properties of materials. (3) The electronic structure of the material. (4) Linear and nonlinear optical properties of materials. (5) The magnetism of the material. (6) Lattice dynamics of materials. (7) Dynamic simulation from scratch.

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## Chapter 3. DFT study of X-site ion substitution doping of Cs<sub>2</sub>PtX<sub>6</sub> on structural and electronic properties

#### **3.1 Introduction**

The inorganic-organic hybrid perovskites solar cells (HPSCs), which are expected to generate renewable resources and resolve global energy problems because of their favorable properties including low cost, superior absorption coefficient<sup>1,2</sup>, appropriate band gap and easy fabrication process.<sup>3,4</sup> The power conversion efficiencies (PCEs) achieved by these materials have steadily improved and currently reach 25.5%.<sup>5</sup> The chemical formula of this kind of perovskite is ABX<sub>3</sub>, where A is inorganic ion ( $Cs^+$ ,  $Rb^+$  or  $K^+$ ) or monovalent organic cation (MA<sup>+</sup>, CH(NH<sub>2</sub>)<sup>2+</sup>(FA)), B is divalent cation (Ge<sup>2+</sup>, Sn<sup>2+</sup> or Pb<sup>2+</sup>) and X is halide ion (I<sup>-</sup>, Br<sup>-</sup> or Cl<sup>-</sup>).<sup>6,7</sup> The cations A and B are combined with 12 and 6 X, respectively.<sup>8,9</sup> Although superior photovoltaic properties have been realized, some challenges still exist with the HPSCs, i.e., the toxicity of lead (Pb), and the perovskites that suffer from a poor chemical stability in air.<sup>10,11</sup> Replacing organic components in the perovskite materials with inorganic components may be an ultimate solution to the problem of thermal instability.<sup>12-14</sup>Therefore, many researchers have developed a new type of all inorganic Cs-based halogenated perovskite CsBX<sub>3</sub> by oxygen evolution in water. The decomposition of the compounds can be retarded by replacing the organic cations with inorganic cesium ions.<sup>15-17</sup> On the other hand, to avoid the toxicity of lead, this has stimulated research into using alternative materials instead of lead for the perovskite compounds. The double and vacancy ordered perovskites have appeared with general formulas  $A^{+1}_{2}B^{+1}B^{+3}X_{6}$  and  $A^{+1}_{2}B^{+4}X_{6}$  respectively, and have many potential applications in optoelectronics and hybrid perovskite halides due to better stability and low toxicity than the traditional ABX<sub>3</sub> perovskites.<sup>18-20</sup> Besides, the advantage that they can be simply prepared into thin films has also attracted the attention of scientists in the field of optoelectronics. Accordingly calculating the physical properties of novel double perovskite will have a wide application prospect.<sup>21</sup> Bahmad et al. studied the magnetic properties, magnetizations and magnetic susceptibilities, and phase diagrams of double perovskite

 $Sr_2VMoO_6$  and  $Sr_2RuHoO_6$  using the Monte Carlo Simulation.<sup>22,23</sup> Mahmood et al. studied the optoelectronics and thermoelectric applications of lead-free double perovskites halides  $Cs_2TiCl_6$  and  $Cs_2TiBr_6$  using density functional theory.<sup>24</sup> Galin et al. simulated the oxygen diffusion in the solid solutions of PrBaCo<sub>2</sub>O<sub>5.5</sub>-based double perovskites by the molecular dynamics method.<sup>25</sup> In recent years, many efforts have been extensively made to study the photoelectricity of the A<sub>2</sub>BX<sub>6</sub> type. In this double perovskite structure, the selection of atoms with varying ion radii can significantly affect the diverse physical properties displayed. Such a unique performance adjustment method can produce optoelectronic devices, magnetoelectric memory and multifunctional spintronics.<sup>26,27</sup> If half of the B ions in the center of the [BX<sub>6</sub>] cluster are removed, the checkered pattern of A<sub>2</sub>BX<sub>6</sub> can be regarded as a derivative of the ABX<sub>3</sub> structure.<sup>28</sup> The selection of the B-site cation has been reported as Sn and Te with an infrared light absorption ability, and can also be transition metal elements of the +4 states such as Pt.<sup>29-31</sup>

Our group<sup>10</sup> has synthesized large-size Cs<sub>2</sub>PtI<sub>6</sub> single crystal and high-quality Cs<sub>2</sub>PtI<sub>6</sub> thin film by a simple method and studied its photovoltaic properties. In the same year, Maike et al.<sup>32</sup> and Sajjad et al.<sup>33</sup> explored the extraordinary stability of Cs<sub>2</sub>PtI<sub>6</sub> in various environments by means of experiment and first principle calculation. For photovoltaic applications, the cost of Pt may be considered prohibitively high. However, Pt provides an excellent model for the substitution of Pb, and Pt based perovskite can be used as interface modification material. Similar to traditional perovskite, halide based double perovskite has been proved to adjust the band gap to optimize the photoelectric properties because ion substitution can produce metal to insulation properties. The substitution and doping of the X-site halogen in  $Cs_2PtX_6$  (X= Cl, Br, I) will also affect the electronic properties of these perovskites. Based on the understanding of the crystal structure and chemical composition of the perovskite compounds, novel perovskite materials for efficient photovoltaic applications can be found by calculation methods such as the density functional theory (DFT). Zeng et al. predicted a series of  $Cs_2TiI_xBr_{6-x}$  (x = 0, 2, 4, 6) leadfree halide perovskites for solar cells applications based on DFT, and the results were confirmed by experimental efforts.<sup>34</sup> Mahmood et al. calculated that bromine substituted chlorine has a great influence on the optical and thermoelectric properties in novel double perovskite Rb<sub>2</sub>PtX<sub>6</sub>, which is almost consistent with the experimental results.<sup>35</sup> Consequently, the theoretical study of these double perovskites can provide a basis for exploring novel device applications.

In this paper, we simulated and optimized the structure of the  $Cs_2PtI_{6-y}Cl_y$ ,  $Cs_2PtI_{6-y}Br_y$ ,  $Cs_2PtBr_{6-y}Cl_y$  (y = 0, 1, 2, 3, 4, 5, 6) and systematically studied their electronic properties by using the generalized gradient approximation of the Perdew–Burke–Ernzerhof (PBE) functional of projector augmented waves (PAW). This function can save calculation time, but it is not accurate when calculating the solid band gap. Therefore, the band gap was calculated with the help of the Heyd-Scuseria-Ernzerhof hybrid functional (HSE06), and we have achieved a good balance between a reasonable computational cost and accuracy of the results. According to the predicted band gap variation law, we selected some perovskites for further calculation using the more accurate but also computationally more expensive HSE06 functional. This work provided a good theoretical foundation for understanding the structural and electronic properties of these compounds. Moreover, the results of the theoretical calculations can provide a rough prediction for the experimental work, reduce the time cost of experimental exploration and avoid meaningless consumptions of the raw materials.

#### **3.2** Computational details

In this study, we used the first principles DFT by the Vienna Ab initio simulation package (VASP) code with a plane-wave basis set.<sup>36</sup> Both the generalized gradient approximation (GGA) of the PBE functional and HSE06 have been used to calculate the structural and electronic properties.<sup>37,38</sup> The atomic pseudo potential was described by the PAW method.<sup>39</sup> The electronic configurations of the Cs, Pt, I, Br and Cl atoms are [Xe]6s<sup>1</sup>, [Xe]5d<sup>9</sup>6s<sup>1</sup>, [Kr]4d<sup>10</sup>5s<sup>2</sup>5p<sup>5</sup>, [Ar]3d<sup>10</sup>4s<sup>2</sup>4p<sup>5</sup> and [Ne]3s<sup>2</sup>3p<sup>5</sup>, respectively. All the structures considered in this paper are fully relaxed using the conjugate gradient algorithm until the total electronic energy and force converge on individual ion was less than 0.1e<sup>-4</sup> eV and 0.001 eV/Å, respectively. The energy cutoff for the plane wave basis for all compounds was set to 400 eV. The grid of k-points employed for computing integrals over the Brillouin zone for geometry optimizations and density of states calculations was taken as 4×4×4. The original models and substitutional doping models of the Cs<sub>2</sub>PtX<sub>6</sub> (X= Cl, Br, I) perovskites were established by Vesta. According to the predicted band gap variation law, we selected Cs<sub>2</sub>PtCl<sub>6</sub>, Cs<sub>2</sub>PtBr<sub>6</sub>, Cs<sub>2</sub>PtI<sub>6</sub> and Cs<sub>2</sub>PtICl<sub>5</sub> for further calculation using the more accurate but also computationally more expensive HSE06 method.

#### **3.3 Results and discussions**

As illustrated in Fig. 1a, the  $Cs_2PtX_6$  (X= Cl, Br, I) has a face centered cubic structure with space group Fm3m (No.225), which is alternately formed by isolated [PtX<sub>6</sub>] clusters and twisted tetragonal Cs cations (space group P4/mnc). In this figure, the  $[PtX_6]^{4-}$  octahedra are shaded with the purple balls in the corners representing halogen. The Cs cations are green balls that are located in the center of 12 halogen ions, and the Pt cations are silver balls and located in the center of the octahedron. The perovskite primitive cell with 9 atoms was chosen as single halogen substitution structure (Fig. 1b). First of all, we need to build the models of Cs<sub>2</sub>PtBr<sub>y</sub>Cl<sub>6-y</sub>, Cs<sub>2</sub>PtI<sub>y</sub>Br<sub>6-y</sub> and  $Cs_2PtI_yCl_{6-y}$  (y = 0, 1, 2, 3, 4, 5, 6). After consulting the relevant crystal databases and references, we did not find a single halogen doped Cs<sub>2</sub>PtX<sub>6</sub> model. Based on the known crystal As illustrated in Fig. 1a, the Cs<sub>2</sub>PtX<sub>6</sub> (X= Cl, Br, I) has a face centered cubic structure with space group Fm3m (No.225), which is alternately formed by isolated [PtX<sub>6</sub>] clusters and twisted tetragonal Cs cations (space group P4/mnc). In this figure, the  $[PtX_6]^{4-}$  octahedra are shaded with the purple balls in the corners representing halogen. The Cs cations are green balls that are located in the center of 12 halogen ions, and the Pt cations are silver balls and located in the center of the octahedron. The perovskite primitive cell with 9 atoms was chosen as single halogen substitution structure (Fig. 1b). First of all, we need to build the models of  $Cs_2PtBr_yCl_{6-y}$ ,  $Cs_2PtI_yBr_{6-y}$  and  $Cs_2PtI_yCl_{6-y}$  (y = 0, 1, 2, 3, 4, 5, 6). After consulting the relevant crystal databases and references, we did not find a single halogen doped Cs<sub>2</sub>PtX<sub>6</sub> model. Based on the known crystal models of Cs<sub>2</sub>PtCl<sub>6</sub>, Cs<sub>2</sub>PtBr<sub>6</sub> and Cs<sub>2</sub>PtI<sub>6</sub>, the X-site atoms of Cs<sub>2</sub>PtX<sub>6</sub> are substituted in a primitive cell, so that we constructed the theoretical calculation doped models. Table 1 shows the lattice constant and formation energy of Cs2PtX<sub>6</sub> calculated by the semi-local GGA-PBE functional. The lattice constant of the undoped symmetrical cells of Cs<sub>2</sub>PtCl<sub>6</sub>, Cs<sub>2</sub>PtBr<sub>6</sub> and Cs<sub>2</sub>PtI<sub>6</sub> are 10.35 Å, 11.04 Å and 11.67 Å respectively, which are close to the experimental values (Cs2PtCl6: 10.19 Å, Cs2PtBr6: 10.67 Å, Cs2PtI6: 11.37 Å),<sup>40-42</sup> indicating that the parameters and models we used are reasonable. We further used another halogen with different doping concentrations to replace the X-site cations to build the lattice model of  $Cs_2PtX_6$ . It can be seen from Table 1 that halogen ions with a small doping radius will reduce the crystal lattice constant and the cell volume (ion radius:  $I^- > Br^- > CI^-$ ).



**Figure. 1.** (a) Schematic crystal structure of Cs<sub>2</sub>PtX<sub>6</sub> (X=Cl, Br, I) with PtX<sub>6</sub> octahedral structure. (b) Primitive cell structure of Cs<sub>2</sub>PtX<sub>6</sub>. Structures visualized with the support of VESTA.

Table 1. Optimized lattice parameters and formation energy of different conc	entration
ratios of halogen doped in Cs <sub>2</sub> PtX <sub>6</sub> (X= Cl, Br, I) primitive cell.	

Compound	a (Å)	<i>Volume</i> (Å <sup>3</sup> )	Formation Energy (eV)
Cs <sub>2</sub> PtCl <sub>6</sub>	7.32	277.16	-11.25
$Cs_2PtBrCl_5$	7.42	288.47	-11.04
$Cs_2PtBr_2Cl_4$	7.50	297.93	-10.85
$Cs_2PtBr_3Cl_3$	7.58	307.45	-10.67
$Cs_2PtBr_4Cl_2$	7.65	316.30	-10.48
Cs <sub>2</sub> PtBr <sub>5</sub> Cl	7.72	325.78	-10.29
$Cs_2PtBr_6$	7.81	337.21	-10.11
$Cs_2PtIBr_5$	7.86	343.87	-9.64
$Cs_2PtI_2Br_4$	7.98	359.85	-9.18
$Cs_2PtI_3Br_3$	8.05	368.89	-8.70
$Cs_2PtI_4Br_2$	8.11	377.01	-8.27
$Cs_2PtI_5Br$	8.19	388.27	-7.86
$Cs_2PtI_6$	8.25	397.19	-7.44
$Cs_2PtI_5Cl$	8.15	382.81	-8.02
$Cs_2PtI_4Cl_2$	7.99	360.54	-8.61
Cs <sub>2</sub> PtI <sub>3</sub> Cl <sub>3</sub>	7.85	341.57	-9.20
--------------------------------------------------	------	--------	--------
$Cs_2PtI_2Cl_4$	7.82	337.90	-9.88
Cs <sub>2</sub> PtICl <sub>5</sub>	7.64	315.04	-10.52

Except for the lattice constants, we also calculated the Goldschmidt's tolerance factor  $(\tau)$  to study the structural properties of crystal using the following equation<sup>43,44</sup>:

$$\tau = \frac{R_A + R_x}{\sqrt{2}(R_B + R_x)} \tag{1}$$

where  $R_A$ ,  $R_B$  and  $R_X$  denote the ionic radius of the A, B and X in the A<sub>2</sub>BX<sub>6</sub> double perovskite structure, respectively. The  $\tau$  evaluated whether the A-Site atoms can stabilize the frame of the octahedron  $[BX_6]^{4-}$ . For the Cs<sub>2</sub>PtX<sub>6</sub> perovskites, the corresponding Shannon ionic radii of Cs<sup>+</sup>, Pt<sup>2+</sup>, Cl<sup>-</sup>, Br<sup>-</sup> and I<sup>-</sup> are 1.67, 0.62, 1.81, 1.96, 2.2 Å, respectively. The value of  $\tau$  is between 0.813 and 1.106, which matches with the higher symmetry.<sup>45</sup> It can be seen from Fig. 2 that the  $\tau$  of all the compounds ranged from 0.97 to 1.013, meeting the constraint conditions given by the definition and indicating that the perovskites are stable at room temperature in the cubic form.





It was necessary to calculate  $\tau$  for predicting the structural stability of the perovskites, however, the structural stability alone is not enough to judge whether a perovskite can be formed. Therefore, in order to evaluate the thermodynamic stability, we calculated the formation energy (*E*<sub>f</sub>) of the undoped and halogen doped Cs<sub>2</sub>PtX<sub>6</sub> perovskites.<sup>12,46</sup> The *E*<sub>f</sub> can be defined as the difference between the total energy of the compound and the sum of the energies of the main components in the standard form, and the formula is given by

$$E_{\rm f} = E_{\rm bulk} - n_{CS} E_{\rm atom}^{\rm Cs} - n_{Pt} E_{\rm atom}^{\rm Pt} - n_{Cl} E_{\rm atom}^{\rm Cl} - n_{Br} E_{\rm atom}^{\rm Br} - n_l E_{\rm atom}^{\rm I}$$
(2)

in which  $E_{\text{bulk}}$  is the total energy of Cs<sub>2</sub>PtX<sub>6</sub>;  $E_{\text{atom}}$  represents the energy of the free atom k (k = Cs, Pt, I, Br, and Cl), and n<sub>k</sub> is the number of atoms k in the primitive cell. The obtained calculation results are listed in Table 1 and Fig. 3, which show that the formation energy varies with the ratio of the X doping. All compounds in our research have negative formation energies, indicating that the compounds can be synthesized under the given environmental conditions.<sup>28</sup> The lower the formation energy, the easier the compound is to be formed and the more stable it is.<sup>46,47</sup> Comparing the data in Table 1, we noticed that Cs<sub>2</sub>PtI<sub>6</sub> has the most unstable structure but doping Cl<sup>-</sup> and Br<sup>-</sup> can significantly reduce the formation energy and improve the thermodynamic stability of the cell. It can be obviously seen from Fig. 3, when Cs<sub>2</sub>PtX<sub>6</sub> is substitution doped with a halogen having a small radius, the formation energy will decrease, thus improving the stability of the cell.



**Figure. 3.** The formation energy of  $Cs_2PtX_6$  (X=Cl, Br, I) varies with the ratio of X doping. The abscissa represents the ratio of two halogens in the compounds.

Table 2. Calculated band gaps with PBE (GGA) and HSE06 functional of halogen substitution doped Cs<sub>2</sub>PtX<sub>6</sub> (X= Cl, Br, I) compounds perovskites.

Compound	Eg (GGA-PBE)/eV	$E_g$ (HSE06)/eV
Cs <sub>2</sub> PtCl <sub>6</sub>	2.02	3.31
$Cs_2PtBrCl_5$	1.78	

$Cs_2PtBr_2Cl_4$	1.68	
$Cs_2PtBr_3Cl_3$	1.58	
$Cs_2PtBr_4Cl_2$	1.51	
Cs <sub>2</sub> PtBr <sub>5</sub> Cl	1.46	
$Cs_2PtBr_6$	1.45	2.33
Cs <sub>2</sub> PtIBr <sub>5</sub>	1.07	
$Cs_2PtI_2Br_4$	0.97	
$Cs_2PtI_3Br_3$	0.87	
$Cs_2PtI_4Br_2$	0.80	
$Cs_2PtI_5Br$	0.63	
$Cs_2PtI_6$	0.61	1.39
$Cs_2PtI_5Cl$	0.69	
$Cs_2PtI_4Cl_2$	0.87	
$Cs_2PtI_3Cl_3$	1.02	
$Cs_2PtI_2Cl_4$	1.13	
Cs <sub>2</sub> PtICl <sub>5</sub>	1.30	2.07



Figure. 4. Band structures of the (a) Cs<sub>2</sub>PtI<sub>6</sub>, (b) Cs<sub>2</sub>PtI<sub>5</sub>Cl, (c) Cs<sub>2</sub>PtI<sub>4</sub>Cl<sub>2</sub>, (d) Cs<sub>2</sub>PtI<sub>3</sub>Cl<sub>3</sub>,
(e) Cs<sub>2</sub>PtI<sub>2</sub>Cl<sub>4</sub> and (f) Cs<sub>2</sub>PtICl<sub>5</sub> calculated by PBE functional.

In order to investigate the latent changing tendency of the halogen doped Cs<sub>2</sub>PtX<sub>6</sub> perovskites, we calculated the band structure and density of states (DOS) of each perovskite. Based on the relaxed structures, the band gaps were calculated by PBE functional and listed in Table 2 in the span range of 0.61 to 2.02 eV. For Cs<sub>2</sub>PtI<sub>y</sub>Cl<sub>6-y</sub>, Cs<sub>2</sub>PtI<sub>y</sub>Br<sub>6-y</sub>, and Cs<sub>2</sub>PtBr<sub>y</sub>Cl<sub>6-y</sub> (y = 0, 1, 2, 3, 4, 5, 6), the band structures are shown in Fig. 4, Fig. 5 and Fig. 6, respectively. It can be seen from the Cs<sub>2</sub>PtI<sub>y</sub>Cl<sub>6-y</sub>, the indirect band gap of Cs<sub>2</sub>PtI<sub>6</sub> was estimated to be 0.61 eV, which is in favorable agreement with the value reported in the Materials Projects and the literature using a similar computational approach.<sup>21</sup> In addition, we found that the type of band gap of the Cs<sub>2</sub>PtBr<sub>y</sub>Cl<sub>6-y</sub> and Cs<sub>2</sub>PtI<sub>y</sub>Cl<sub>6-y</sub> changed from direct to indirect when y is from 0 to 1 in Fig. 4 and Fig. 6, and all the other perovskites have indirect band structure, conduction band minimum (CBM) and the valence band maximum (VBM) are at the X point and GAMMA point, respectively. This phenomenon indicated that the doping of a halogen will change the band structure type of Cs<sub>2</sub>PtCl<sub>6</sub>, but not destroy the main characteristics of the band structure of the other compounds.



Figure. 5. Band structures of the (a) Cs<sub>2</sub>PtBr<sub>6</sub>, (b) Cs<sub>2</sub>PtIBr<sub>5</sub>, (c) Cs<sub>2</sub>PtI<sub>2</sub>Br<sub>4</sub>, (d) Cs<sub>2</sub>PtI<sub>3</sub>Br<sub>3</sub>,
(e) Cs<sub>2</sub>PtI<sub>4</sub>Br<sub>2</sub> and (f) Cs<sub>2</sub>PtI<sub>5</sub>Br calculated by PBE functional.



**Figure. 6.** Band structures of the (a) Cs<sub>2</sub>PtCl<sub>6</sub>, (b) Cs<sub>2</sub>PtBrCl<sub>5</sub>, (c) Cs<sub>2</sub>PtBr<sub>2</sub>Cl<sub>4</sub>, (d) Cs<sub>2</sub>PtBr<sub>3</sub>Cl<sub>3</sub>, (e) Cs<sub>2</sub>PtBr<sub>4</sub>Cl<sub>2</sub> and (f) Cs<sub>2</sub>PtBr<sub>5</sub>Cl calculated by PBE functional.

In our research,  $Cs_2PtI_6$  has the narrowest band gap, while  $Cs_2PtCl_6$  has the largest value of band gap. The present calculation results show an obvious trend with the size of the X-site anion in Fig. 7. In the  $[PtX_6]^{4-}$  octahedron, the lighter Cl<sup>-</sup> is replaced by the heavier Br<sup>-</sup> and I<sup>-</sup>, resulting in the enhanced interaction between Pt and X-site anions, which have an important impact on the characteristics of the band structure. Owing to electronegativity (Cl > Br > I) and atomic radius (I > Br > Cl), the difference of the Pt-Cl distance is more significant than that of Pt-Br and Pt-I, which leads to the larger band gap of the Cl<sup>-</sup> doped perovskite than that of the other halogen doped perovskites.<sup>28,48</sup> The electronic properties of the different concentration ratios of halogen doping in Cs<sub>2</sub>PtX<sub>6</sub> (X= Cl, Br, I) are further explained by the DOS.



**Figure. 7.** The band gap (calculated by PBE method) of Cs<sub>2</sub>PtX<sub>6</sub> varies with the ratio of X doping (X=Cl, Br, I). The abscissa represents the ratio of two halogens in the compounds.

Figure 8, 9 and 10 show the calculated DOS of the Cs<sub>2</sub>PtI<sub>y</sub>Cl<sub>6-y</sub>, Cs<sub>2</sub>PtI<sub>y</sub>Br<sub>6-y</sub> and  $Cs_2PtBr_vCl_{6-v}$  perovskites, respectively, and the Fermi energy is set to zero. All the materials exhibit semiconductor properties because the valence band of DOS does not cross over the Fermi level. The analysis of the orbital characteristics of Cs<sub>2</sub>PtI<sub>6</sub> shows that the VBM is mainly contributed by the I-p orbitals and a small contribution of Pt-d, while the CBM also consists of the interaction of Pt-d orbitals with I-p orbitals. The contribution of the Cs orbitals of all materials in the total density of states (TDOS) is unimportant in both the valence band and conduction band. When I atom is replaced by Cl or Br atom, we can see similar pattern with a few differences in the partial density of states (PDOS) diagram. From Fig. 8, it is clear that the p orbitals of Cl will contribute more and more to the valence and conduction bands when the doping concentration increases, and which sits back quite deep in the valence band, resulting in the movement of PDOS towards lower energy. With the increasing content of Br<sup>-</sup> and I<sup>-</sup>, the contribution of the heavier halogen tends to be close to the Fermi energy, leading to decrease of the band gap. The electrostatic force of valence electrons in nucleus will weaken with the increase of atomic radius, which will reduce the energy between valence band and conduction band. Therefore, for the narrow bandgaps, only a small amount of incident energy is needed to excite the bound electron guide band to move to the free conduction state.<sup>49,50</sup> Almost all the bandgap transitions of these

compounds occur in the mixed state from the X-p and Pt-d orbital of the conduction band to the X-p orbital of the valence band.



Figure. 8. The density of states (DOS) of the (a)  $Cs_2PtI_6$ , (b)  $Cs_2PtI_5Cl$ , (c)  $Cs_2PtI_4Cl_2$ , (d)  $Cs_2PtI_3Cl_3$ , (e)  $Cs_2PtI_2Cl_4$  and (f)  $Cs_2PtICl_5$ .



Figure. 9. Density of states (DOS) of the (a)  $Cs_2PtBr_6$ , (b)  $Cs_2PtIBr_5$ , (c)  $Cs_2PtI_2Br_4$ , (d)  $Cs_2PtI_3Br_3$ , (e)  $Cs_2PtI_4Br_2$  and (f)  $Cs_2PtI_5Br$ .



Figure. 10. Density of states (DOS) of the (a)  $Cs_2PtCl_6$ , (b)  $Cs_2PtBrCl_5$ , (c)  $Cs_2PtBr_2Cl_4$ , (d)  $Cs_2PtBr_3Cl_3$ , (e)  $Cs_2PtBr_4Cl_2$  and (f)  $Cs_2PtBr_5Cl_6$ .

Since the PBE functional tends to underestimate the bandgaps, the variation law of bandgaps was used as a screening criterion for further calculations based on HSE06 level. With the consideration of the computational cost, we only calculate the hybrid-functional band structure of Cs<sub>2</sub>PtCl<sub>6</sub>, Cs<sub>2</sub>PtBr<sub>6</sub>, Cs<sub>2</sub>PtI<sub>6</sub> and Cs<sub>2</sub>PtICl<sub>5</sub>. Fig.11 shows the HSE band structures of the four perovskites selected as representatives. It is worth mentioning that although the bandgap values calculated by the two methods are different, they have similar band structures. It can be seen from Table 2 that the hybrid functional band gaps of the four perovskites are 3.31 eV, 2.33 eV, 1.39 eV and 2.07 eV, respectively. As for Cs<sub>2</sub>PtI<sub>6</sub>, the calculated HSE bandgap is 1.39 eV, which is roughly consistent in experimental value of 1.37 eV, proving the reliability of the calculation results.<sup>10</sup> According to the trend in the bandgaps calculated by PBE method, we can predict that other unscanned HSE bandgaps of the compounds will change in a small range. The band gap of Cs<sub>2</sub>PtI<sub>y</sub>Cl<sub>6-y</sub> is between 1.39 eV and 3.31 eV, while that of Cs<sub>2</sub>PtI<sub>y</sub>Br<sub>6-y</sub> and Cs<sub>2</sub>PtBr<sub>v</sub>Cl<sub>6-v</sub> are from 1.39 to 2.33 eV and 2.33 to 3.31 eV, respectively. The range of the bandgaps for the most potential candidates is usually between 1.0 eV and 1.9 eV. Considering that the results of HSE06 functional calculation slightly overestimate the band gap, the Cs<sub>2</sub>PtI<sub>y</sub>Br<sub>6-y</sub> and Cs<sub>2</sub>PtI<sub>y</sub>Cl<sub>6-y</sub> with appropriate band gap may be potentially ideal for pure perovskite and tandem perovskite solar cell materials.



Figure. 11. Band structures of the (a) Cs<sub>2</sub>PtCl<sub>6</sub>, (b) Cs<sub>2</sub>PtBr<sub>6</sub>, (c) Cs<sub>2</sub>PtI<sub>6</sub>, (d) Cs<sub>2</sub>PtICl<sub>5</sub> calculated by HSE06 functional.

# **3.4 Conclusions**

In summary, we have successfully investigated the structure, stability and electronic properties of  $Cs_2PtBr_yCl_{6-y}$ ,  $Cs_2PtI_yBr_{6-y}$ , and  $Cs_2PtI_yCl_{6-y}$  (y = 0, 1, 2, 3, 4, 5, 6) using DFT calculations, 18 perovskites in total. Based on the structural analysis, both the crystal lattice constant and the cell volume of  $Cs_2PtX_6$  (X= Cl, Br, I) suffer a monotonic increase with the decreasing content of halogen ions with small doping radii. In the study of the stability, the calculated tolerance factors for all the perovskites are well within the specified range. The formation energies of all the compounds are negative. Moreover, the value of formation energy of investigated  $Cs_2PtX_6$  perovskites with higher Cl<sup>-</sup> content is lower, which indicates that the thermodynamic stability of structure can be improved by replacing the I<sup>-</sup> or Br<sup>-</sup> with an appropriate amount of Cl<sup>-</sup>. The electronic properties based on PBE level results show that the band gap tends to increase when I<sup>-</sup> is replaced by Cl<sup>-</sup> and Br<sup>-</sup> in the halogen substitution of the X-site. Furthermore,  $Cs_2PtI_yBr_{6-y}$  and  $Cs_2PtI_yCl_{6-y}$  (Except  $Cs_2PtCl_6$ )

have band gap values of 1.3-2.3 eV calculated by HSE06 functional, indicating that they have the potential to be used in perovskite and tandem perovskite solar cells. Based on this work, the general trends in bandgaps and stability are anticipated to provide a guideline for the design of novel stable inorganic halide perovskite materials with ideal properties.

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# Chapter 4. Computational screening of Cs based vacancy-ordered double perovskites for solar cell and photocatalysis applications

## 4.1 Introduction

Halide perovskites have been expected to be the next generation of important materials for various optoelectronic applications due to their low-cost, excellent absorption coefficient, suitable bandgap, and facile fabrication process.<sup>1-4</sup> The perovskite solar cells, in particular, have achieved remarkable power conversion efficiency (PCE) over a short research time. Since the debut of MAPbI<sub>3</sub> and MAPbBr<sub>3</sub> as photovoltaic materials,<sup>5</sup> the PCEs were steadily improved and reach 25.5% nowadays.<sup>6</sup> Furthermore, this type of perovskite with exceptional charge transfer ability has also witnessed a vigorous development in photocatalysis over the traditional oxide perovskites in the past few years.<sup>7–9</sup> Their potential applications in the organic pollutants degradation, the decomposition of H<sub>2</sub>O to H<sub>2</sub> and O<sub>2</sub>, and CO<sub>2</sub> reduction by solar energy have triggered ripples of excitement.<sup>10</sup> Halide perovskites possess a crystal structure of general formula ABX<sub>3</sub>, similar to that of typical perovskites with general formula ABO<sub>3</sub>. In the halide perovskite crystal structure, the larger metal ion (e.g. Cs<sup>+</sup>) or monovalent organic cation (e.g.  $MA^+$ ) is located at the A-site, and the B-site is smaller metal ion (Ge<sup>2+</sup>,  $Sn^{2+}$ ,  $Pb^{2+}$ , etc) as well as X is halide ion. Although many researchers have witnessed the phenomenal growth of halide perovskite, both inorganic and hybrid, there are still challenges to the booming field of solar cells and photocatalysis, i.e., the instability and lead toxicity that some perovskites suffer from.<sup>11</sup> The toxicity of lead ions in halide perovskite absorbing materials is the main bottleneck for practical application. Lead is one of the three major heavy metal contaminants and a heavy metal element that seriously endangers humans and the environment.<sup>12</sup> Even if only a small amount of exposure, lead can seriously threaten health, causing problems including impaired brain development, renal failure, and nerve injury.<sup>13</sup> Therefore, it also hinders the lead halide perovskite largescale production and commercial application. To overcome these limitations, researchers are focusing on replacing Pb with non-toxic metals. However, studies have shown that the oxidation tendency of same group elements like Sn and Ge changes from + 2 states to + 4 states, which is

incompatible with totally replacing Pb.<sup>14,15</sup> The perovskites composed of other divalent cations instead of lead may have poor photoelectric properties due to a large bandgap.<sup>16,17</sup> Hence, attempts have been made to explore perovskite-like structures through double perovskites, in which monovalent and trivalent ones transmute two adjacent divalent lead ions.<sup>18</sup> So far, according to the different types of B and B' cations, researchers have synthesized four sorts of double perovskites with general formulas A<sub>2</sub>BB'X. A-side from the general formula A<sub>2</sub>BX<sub>6</sub>, represented by a vacancy in the B cation and a tetravalent B' cation, the other three types all take the scheme of Pb<sup>2+</sup> replacing monovalent and trivalent ions.<sup>7</sup> This kind of new perovskite provides researchers with a new idea to prepare green materials without losing photoelectric properties and shows excellent stability in light, moisture, and temperature.<sup>19,20</sup> Due to the existence of unstable organic cations, the thermal decomposition temperature of hybrid perovskite is low. For the solution of thermal instability, some scholars prefer to replace the organic components in perovskite with inorganic metal ions, such as Cs<sup>+</sup>.<sup>21–23</sup> A new sort of all inorganic Cs based halogenated perovskite has been developed by using oxygen evolution in water recently.<sup>24–26</sup> This effectively improves the thermal stability of the material, thereby prolongs the service life of the equipments.<sup>27</sup> In addition, the introduction of Cs can suppress the phase impurities, permitting the preparation with high purity and defect-free perovskite films, which is less sensitive to processing conditions. This enables perovskite solar cells device performance to achieve repeatable high efficiency.<sup>28</sup> Recent studies on lead-free perovskite substitutes, especially A2BX6, usually report the synthesis and characterization of bulk powders or single crystals, such as Cs<sub>2</sub>ZrCl<sub>6</sub>, Cs<sub>2</sub>SnI<sub>6</sub>, Cs<sub>2</sub>TiBr<sub>6</sub>, and so on.<sup>29-31</sup> All these investigations show that A<sub>2</sub>BX<sub>6</sub> structure can be readily doped with different impurity ions, especially at the position of 6-fold coordinated tetravalent cations. Substitution alloying is expected to realize the lead-free perovskite and optimize the properties for device applications.<sup>32</sup> Furthermore, in some studies comparing hole transport characteristics of  $Cs_2SnX_6$  and  $Cs_2TiX_6$  (X = Cl, Br, I), systematic variations in the transport and optical properties were observed the halogen anions substitution with different sizes and electronegativity.<sup>33,34</sup> Zeng et al. also reported a novel sort of all inorganic perovskites Cs<sub>2</sub>TiI<sub>x</sub>Br<sub>6-x</sub> based on earth-rich, leadfree, and ultrastable Ti (IV). They have proved that titanium-based photonic crystals have desirable attributes.<sup>35</sup> Although this is only a small experimental sample of A<sub>2</sub>BX<sub>6</sub> family material, which

have distinctly shown the significance of B-X composition is worthy of future exploration in the field of photocatalysis as well as solar cells.

To guide future research into the theoretical calculation of the properties of more extensive double perovskite, this study used a calculation method based on density functional theory (DFT) to investigate the structural, electronic, and optical properties of Cs<sub>2</sub>BX<sub>6</sub> compounds, with the goal of finding suitable candidates for photocatalysts and perovskite solar cells. For this purpose, the study began with 30 perovskite materials including cesium ions, 10 metals, and 3 halogens, as shown in Fig.1. The A<sub>2</sub>BX<sub>6</sub> double perovskite can be thought of as a derivative structure of standard  $A_2B'BX_6$  perovskites, in which the vacancy substitutes the B-site cation, yielding vacancy-ordered double perovskites. The studied crystal model is shown in Fig. 1; the  $Cs_2BX_6$ usually has a face-centered cubic structure with space group Fm3m (No.225), which is alternately formed by isolated [BX<sub>6</sub>] clusters and twisted tetragonal Cs cations (space group P4/mnc). In the DFT framework, the most advanced hierarchical calculation method based on the first-principles is used for high-throughput screening. After using the tolerance factor and enthalpy of formation  $(\Delta H)$  to evaluate the stability (or formability) of the perovskites geometric structure, the bandgaps of the optimized perovskites are calculated at the PBE (Perdew-Burke-Ernzerhof), and HSE (Heyd-Scuseria-Ernzerhof) levels with spin-orbit coupling (SOC) of theory. We employed a single procedure to prescreen the materials with potential in solar cells and photocatalysis, and set the bandgap threshold at 1.6 eV. These selected perovskites were further explored for their optical properties and band-edged positions. This study lays a solid theoretical foundation for understanding these compounds' structural and electronic properties. The experimental data of other studies prove the reliability of our calculation results. Furthermore, the results predicted by theoretical calculation can provide efficient guidance for the experimental plan, so as to improve the work efficiency and making the research more purposeful.

#### Cs based double perovskites



**Figure. 1.** The cubic phases of hybrid double perovskites of the form Cs<sub>2</sub>BX<sub>6</sub> were studied using 10 different metals (B, yellow) and 3 different halides (X, green).

## 4.2 Calculation methods

All calculations on the compounds were performed using PBE-GGA (generalized gradient approximation) and HSE with SOC based DFT study by the Vienna Ab initio simulation package (VASP) code with a plane-wave basis set.<sup>36–38</sup> GGA is an approximation of functionals for exchange and correlation in DFT calculation, which contains more physical information, such as charge density and gradient information of charge density, which can generally make the calculation result more accurate<sup>37</sup>. The projector augmented waves (PAW) approach was used to characterize the atomic pseudopotential.<sup>39</sup> The energy cutoff for the plane-wave basis for all compounds was set to 400 eV. The k-points grid of  $4\times4\times4$  was employed for computing integrals over the Brillouin zone for geometric optimizations and analysis of the density of states (DOS). According to the convergence testing results of three randomly picked compounds Cs<sub>2</sub>TiCl<sub>6</sub>, Cs<sub>2</sub>PdBr<sub>6</sub>, and Cs<sub>2</sub>TeI<sub>6</sub> in Fig. 2, it is found that the selections of plane-wave cutoff, k-point density, and the energy convergence criterion are sufficient to provide the total energy converging to within 0.001 eV/atom, lattice constants within 0.1 Å, and band gaps within 0.01 eV. In this work, the optimized perovskites' optical properties and electronic properties were first calculated by PBE functional, a less expensive function in terms of computational time without enough accuracy for

calculating the bandgaps of solids. After prescreening, HSE functional with SOC was used to perform the high-precision calculation for remaining perovskites. After prescreening, HSE functional with SOC was used to perform the high-precision calculation for remaining perovskites. All the structures considered in this study were fully relaxed using the conjugate gradient algorithm until the force converge on individual ions were less than 0.001 eV/Å at the PBE level, and within 0.05 eV/Å for HSE+SOC. Fig. 3 show the variation of the DFT bandgap of perovskites with two distinct functional and with or without SOC. In halide perovskite systems containing heavy elements, the SOC effect must be seriously considered, and SOC can significantly reduce the calculated bandgap for cesium-based halide perovskites. <sup>40–42</sup>



**Figure. 2.** Convergence testing of Cs<sub>2</sub>TiCl<sub>6</sub>(a: Cutoff, b: K-points, c: EDIFF), Cs<sub>2</sub>PdBr<sub>6</sub>(d: Cutoff, e: K-points, f: EDIFF) and Cs<sub>2</sub>TeI<sub>6</sub>(g: Cutoff, h: K-points, i: EDIFF).



### Valence band maximum

**Figure. 3.** Diagram of difference in the DFT bandgaps with the 2 functionals (PBE and HSE) without and with SOC.

## 4.3 Results and discussions

### 4.3.1 Structural and thermodynamic stability

Perovskites' structural and thermodynamic stability are important area of research for practical applications. Due to weakly bonded soft organic cations, inorganic halide perovskite is more stable than hybrid perovskite.<sup>43</sup> However, as inorganic cations and halogen ions vary, the stability of inorganic halide perovskite changes as well. In screening perovskites, the perovskite structure structural stability (or formability) under various chemical compositions is usually the preliminary evaluation for the studied materials. The structures of 30 perovskite materials were optimized at the PBE functional level using DFT, and their enthalpy of formation ( $\Delta H$ ), Gibbs free energy ( $\Delta G$ ), and entropy ( $\Delta S$ ) were calculated. Note that the  $\Delta H$  is enough to determine the perovskite stability at 0 K, but it could be different from that at room temperature.<sup>44</sup> Therefore, we also calculated the reaction free energy at room temperature (298.15 K), and considered the zeropoint energy ( $\Delta E_{ZPE}$ ) correction. The optimized lattice parameters,  $\Delta H$ ,  $\Delta G$ ,  $\Delta S$ , Goldschmidt tolerance factor (t), octahedral factor ( $\mu$ ), and new tolerance factor ( $\tau$ ) of Cs<sub>2</sub>BX<sub>6</sub> symmetrical cubic cell, are included in Table 1.

**Table 1** Optimized lattice parameters, enthalpy of formation ( $\Delta H$ ), Gibbs free energy ( $\Delta G$ ), entropy ( $\Delta S$ ), Goldschmidt tolerance factor (t), octahedral factor ( $\mu$ ), and new tolerance factor ( $\tau$ )

Compound	a (Å)	$\Delta H(eV/f.u.)$	$\Delta G(eV/f.u.)$	$\Delta S(\text{meV/K})$	t	μ	τ
Cs <sub>2</sub> TiCl <sub>6</sub>	10.34	-16.37	-17.11	3.21	0.977	0.475	3.900
Cs <sub>2</sub> TiBr <sub>6</sub>	10.84	-13.63	-14.63	3.86	0.963	0.439	4.074
Cs <sub>2</sub> TiI <sub>6</sub>	11.83	-10.04	-11.20	4.27	0.943	0.391	4.353
Cs <sub>2</sub> ZrCl <sub>6</sub>	10.54	-19.21	-20.03	3.44	1.031	0.398	4.234
Cs <sub>2</sub> ZrBr <sub>6</sub>	11.02	-15.10	-16.14	3.97	1.013	0.367	4.443
Cs <sub>2</sub> ZrI <sub>6</sub>	11.95	-11.34	-12.53	4.31	0.988	0.327	4.776
Cs <sub>2</sub> GeCl <sub>6</sub>	10.57	-12.45	-13.21	3.28	1.027	0.403	4.202
Cs <sub>2</sub> GeBr <sub>6</sub>	11.07	-10.03	-11.04	3.87	1.009	0.372	4.407
Cs <sub>2</sub> GeI <sub>6</sub>	11.76	-6.92	-8.12	4.35	0.985	0.332	4.736
Cs <sub>2</sub> HfCl <sub>6</sub>	10.48	-18.12	-18.94	3.43	1.035	0.392	4.341
Cs <sub>2</sub> HfBr <sub>6</sub>	11.00	-15.16	-16.21	3.98	1.017	0.362	4.480
Cs <sub>2</sub> HfI <sub>6</sub>	11.95	-11.27	-12.47	4.35	0.991	0.323	4.818
$Cs_2PdCl_6$	10.31	-10.73	-11.43	3.12	0.977	0.475	3.900
Cs <sub>2</sub> PdBr <sub>6</sub>	10.93	-9.19	-10.19	3.85	0.963	0.439	4.074
Cs <sub>2</sub> PdI <sub>6</sub>	11.64	-7.14	-8.3	4.27	0.943	0.391	4.353
Cs <sub>2</sub> TeCl <sub>6</sub>	10.61	-11.75	-12.64	3.60	0.939	0.536	3.795
Cs <sub>2</sub> TeBr <sub>6</sub>	11.13	-9.89	-11.00	4.14	0.927	0.495	3.950
Cs <sub>2</sub> TeI <sub>6</sub>	12.06	-7.37	-8.61	4.47	0.910	0.441	4.197
$Cs_2MoCl_6$	10.32	-12.52	-13.24	3.18	1.060	0.359	4.508
Cs <sub>2</sub> MoBr <sub>6</sub>	10.84	-10.02	-11.01	3.83	1.040	0.332	4.739
$Cs_2MoI_6$	11.60	-6.83	-5.42	4.21	1.012	0.295	5.108
$Cs_2SnCl_6$	10.48	-13.38	-14.19	3.38	0.881	0.635	3.900
$Cs_2SnBr_6$	11.14	-11.14	-12.20	3.99	0.873	0.587	4.030
$Cs_2SnI_6$	12.01	-8.05	-9.27	4.40	0.861	0.523	4.239
$Cs_2PtCl_6$	10.19	-11.25	-11.93	3.08	1.000	0.442	4.013
$Cs_2PtBr_6$	10.67	-10.11	-11.10	3.83	0.984	0.408	4.200
Cs <sub>2</sub> PtI <sub>6</sub>	11.37	-7.44	-8.59	4.21	0.962	0.364	4.500
Cs <sub>2</sub> PbCl <sub>6</sub>	11.58	-11.75	-12.64	3.58	0.870	0.657	3.976
Cs <sub>2</sub> PbBr <sub>6</sub>	11.11	-9.90	-11.04	4.18	0.862	0.607	4.102

of Cs<sub>2</sub>BX<sub>6</sub> symmetrical cell.

$Cs_2PbI_6$	11.99	-7.26	-8.58	4.68	0.851	0.541	4.303
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The optimized primitive cells of all compounds were shown in Fig. 4-13. Taking the  $Cs_2PtX_6$  optimized primitive cell as an example (Fig. 4), the lattice constant of  $Cs_2PtI_6$ ,  $Cs_2PtBr_6$ , and  $Cs_2PtCl_6$  is 11.67 Å, 11.04 Å, and 10.35 Å, respectively. These results are close to the experimental values ( $Cs_2PtI_6$ : 11.37 Å,  $Cs_2PtBr_6$ : 10.67 Å,  $Cs_2PtCl_6$ : 10.19 Å),<sup>45–47</sup> suggesting that the construction of the model and the selection of calculation parameters are reasonable.



Figure. 4. Primitive cell structure of (a) Cs<sub>2</sub>PtI<sub>6</sub>, (b) Cs<sub>2</sub>PtBr<sub>6</sub> and (c) Cs<sub>2</sub>PtCl<sub>6</sub>.



Figure. 5. Primitive cell structure of (a) Cs<sub>2</sub>TiCl<sub>6</sub>, (b) Cs<sub>2</sub>TiBr<sub>6</sub> and (c) Cs<sub>2</sub>TiI<sub>6</sub>.



Figure. 6. Primitive cell structure of (a) Cs<sub>2</sub>ZrCl<sub>6</sub>, (b) Cs<sub>2</sub>ZrBr<sub>6</sub> and (c) Cs<sub>2</sub>ZrI<sub>6</sub>.



Figure. 7. Primitive cell structure of (a) Cs<sub>2</sub>GeCl<sub>6</sub>, (b) Cs<sub>2</sub>GeBr<sub>6</sub> and (c) Cs<sub>2</sub>GeI<sub>6</sub>.



Figure. 8. Primitive cell structure of (a) Cs<sub>2</sub>HfCl<sub>6</sub>, (b) Cs<sub>2</sub>HfBr<sub>6</sub> and (c) Cs<sub>2</sub>HfI<sub>6</sub>.



Figure. 9. Primitive cell structure of (a) Cs<sub>2</sub>PdCl<sub>6</sub>, (b) Cs<sub>2</sub>PdBr<sub>6</sub> and (c) Cs<sub>2</sub>PdI<sub>6</sub>.



Figure. 10. Primitive cell structure of (a) Cs<sub>2</sub>TeCl<sub>6</sub>, (b) Cs<sub>2</sub>TeBr<sub>6</sub> and (c) Cs<sub>2</sub>TeI<sub>6</sub>.



Figure. 11. Primitive cell structure of (a) Cs<sub>2</sub>MoCl<sub>6</sub>, (b) Cs<sub>2</sub>MoBr<sub>6</sub> and (c) Cs<sub>2</sub>MoI<sub>6</sub>.



Figure. 12. Primitive cell structure of (a) Cs<sub>2</sub>SnCl<sub>6</sub>, (b) Cs<sub>2</sub>SnBr<sub>6</sub> and (c) Cs<sub>2</sub>SnI<sub>6</sub>.



Figure. 13. Primitive cell structure of (a) Cs<sub>2</sub>PbCl<sub>6</sub>, (b) Cs<sub>2</sub>PbBr<sub>6</sub> and (c) Cs<sub>2</sub>PbI<sub>6</sub>.

The  $\Delta H$  can be defined as the difference between the total energy of the compound and the energies of each component in the standard state, and the formula is as follows:  $\Delta H = E_{\text{bulk}} - n_{Cs} E_{\text{atom}}^{\text{Cs}} - n_{B} E_{\text{atom}}^{\text{B}} - n_{X} E_{\text{atom}}^{\text{X}}$ (1)

where  $E_{\text{bulk}}$  represents the total energy of Cs<sub>2</sub>BX<sub>6</sub>;  $E_{\text{atom}}$  is the energy of the free atoms B and X, and n represents the number of free atoms in the primitive cell. The reaction free energies can be obtained by the following equation

$$\Delta G = \Delta H + \Delta E_{ZPE} - T\Delta S \tag{2}$$

where the  $\Delta S$  and  $\Delta E_{ZPE}$  are the difference of entropy and zero-point energy, respectively. The negative  $\Delta H$  and  $\Delta G$  indicate the excellent stability of all compounds, which will not decompose into respective binary components. Moreover, the reliability of the thermodynamic stability evaluation was further verified by calculating perovskite materials (Cs<sub>2</sub>TiI<sub>6</sub>, Cs<sub>2</sub>GeBr<sub>6</sub>, Cs<sub>2</sub>PtI<sub>6</sub>, Cs<sub>2</sub>PdBr<sub>6</sub>, Cs<sub>2</sub>TeI<sub>6</sub>, Cs<sub>2</sub>TiBr<sub>6</sub>, Cs<sub>2</sub>SnBr<sub>6</sub>, and Cs<sub>2</sub>PtBr<sub>6</sub>) suitable for solar cells or photocatalysts in solar water splitting after final screening by the commonly used convex hull method.<sup>48</sup> The enthalpies of formation of the potential binary and ternary competitive phases of Cs<sub>2</sub>BX<sub>6</sub> are illustrated in Fig. 14, and all compounds correspond on the x-axis. The dashed line represents the convex hull, that is, the set of enthalpies change lines of all competing phases. If the  $\Delta H$  of the perovskite studied is less than the convex hull of all phases, which means that the compound is thermodynamically stable, otherwise, the material may be metastable or prone to decomposition.<sup>49</sup> From the convex hull approach of the various competing phases of Cs<sub>2</sub>TiI<sub>6</sub>, Cs<sub>2</sub>GeBr<sub>6</sub>, Cs<sub>2</sub>PtI<sub>6</sub>, Cs<sub>2</sub>PdBr<sub>6</sub>, Cs<sub>2</sub>TeI<sub>6</sub>, Cs<sub>2</sub>TiBr<sub>6</sub>, Cs<sub>2</sub>SnBr<sub>6</sub>, and Cs<sub>2</sub>PtBr<sub>6</sub>, it can be seen all the screened perovskites are thermodynamically stable.



**Figure. 14.** The enthalpy of formation of the potential binary and ternary competitive phase of (a) Cs<sub>2</sub>TiI<sub>6</sub>, (b) Cs<sub>2</sub>GeBr<sub>6</sub>, (c) Cs<sub>2</sub>PtI<sub>6</sub>, (d) Cs<sub>2</sub>PdBr<sub>6</sub>, (e) Cs<sub>2</sub>TeI<sub>6</sub>, (f) Cs<sub>2</sub>TiBr<sub>6</sub>, (g) Cs<sub>2</sub>SnBr<sub>6</sub>, and (h) Cs<sub>2</sub>PtBr<sub>6</sub>. The dashed line represents the convex hull, that is, the set of enthalpy change lines of all competing phases.

The Goldschmidt tolerance factor ( $t = (r_A + r_X)/\sqrt{2(r_B + r_X)}$ ) and the octahedral factor ( $\mu$  $= r_B/r_X$ ) are commonly used to predict the formation of perovskites by ion radius (r) to get a more distinct idea about the stability of these perovskites at room temperature.<sup>50,51</sup> Generally, the cubic structure of halide perovskites can maintain stability at 0.89 < t < 1and  $0.44 < \mu < 0.90$ <sup>52</sup> Table 1 shows that the  $\tau$  of all compounds meet the constraint conditions, representing that perovskites are relatively stable in the cubic phase at room temperature. However, the calculation results of  $\mu$  are not all in a stable range, which is related to the perovskite structural characteristics. The symmetry-lowering phase transition causes the cooperative octahedral tilt and rotation of the vacancy-ordered structure with the general formula A<sub>2</sub>BX<sub>6</sub> after cooling. The constituent atoms' ionic radius mismatch, affects this phase transition.<sup>53</sup> By comparing structural maps separated by halide, Fedorovskiy et al. also conclude that the  $\mu$  factor may not be closely related to the formation of cubic double perovskite.<sup>54</sup> Significantly, for more than 90 years, perovskite design has been based on the Goldschmidt tolerance factor. However, as reported by recent studies, its accuracy is often not enough. In 2019, Bartel et al. initiated a new tolerance factor with a total accuracy of 92%, which was used to test the experimental group and generalized in a wide range of single and double perovskites.<sup>55</sup>

$$\tau = \frac{r_X}{r_B} - n_A \left( n_A - \frac{r_A/r_B}{\ln(r_A/r_B)} \right) \tag{3}$$

in which  $n_A$  represents the oxidation state of A-site cation,  $r_A$  and  $r_B$  represent the radius of ions,  $r_A > r_B$  by definition, and  $\tau < 4.18$  indicates perovskite.  $\tau$  is only trained for ABX<sub>3</sub> compounds, but it is easy to adapt to A<sub>2</sub>BB'X<sub>6</sub> double perovskite since it relies only on compositions rather than structures. It can be concluded from Table 1, that when Zr, Ge, Hf, and Mo are selected for B-site cations, no matter what the halogen ion is, the value of  $\tau$  will be greater than 4.18, meaning that the probability of this component forming a stable perovskite structure is low. Cl<sup>-</sup> contributes more to structural stability than Br<sup>-</sup> and I<sup>-</sup>, which is consistent with the calculation results of  $\Delta H$  and  $\Delta G$ . Note that since the  $\tau$  was not verified on vacancy-ordered double perovskite A<sub>2</sub>BX<sub>6</sub>, its accuracy could be in doubt.  $Cs_2PtI_6$ , for instance, has been successfully synthesized and investigated effectively, and it is not capable of forming stable perovskite as predicted by the  $\tau$ .<sup>11,56</sup>

#### 4.3.2 Electronic properties

One of the important characteristics of these perovskite materials is the bandgap. The optimum bandgap of single-junction perovskite solar cells is usually within the range of 0.9-1.6 eV.<sup>35,57</sup> The bandgaps of these 30 perovskites were calculated using DFT at the PBE levels, and the results were employed as a pre-screening benchmark. The PBE-based band structure and DOS of the studied 30 perovskites were displayed in Fig. 15–19. However, PBE functional underestimates the bandgaps of periodic systems in most cases. To account for numerical inaccuracies, we maintain a margin of 0.3 eV at the low ends, i.e., the perovskites with bandgap values of 0.6-1.6 eV at the PBE level were selected for further study.



Figure. 15. Band structures and density of states of the (a) Cs<sub>2</sub>TiI<sub>6</sub>, (b) Cs<sub>2</sub>TiBr<sub>6</sub>, (c) Cs<sub>2</sub>TiCl<sub>6</sub>,
(d) Cs<sub>2</sub>ZrI<sub>6</sub>, (e) Cs<sub>2</sub>ZrBr<sub>6</sub>, (f) Cs<sub>2</sub>ZrCl<sub>6</sub> calculated by PBE functional.



Figure. 16. Band structures and density of states of the (a) Cs<sub>2</sub>GeI<sub>6</sub>, (b) Cs<sub>2</sub>GeBr<sub>6</sub>, (c) Cs<sub>2</sub>GeCl<sub>6</sub>,
(d) Cs<sub>2</sub>HfI<sub>6</sub>, (e) Cs<sub>2</sub>HfBr<sub>6</sub>, (f) Cs<sub>2</sub>HfCl<sub>6</sub> calculated by PBE functional.



Figure. 17. Band structures and density of states of the (a) Cs<sub>2</sub>PdI<sub>6</sub>, (b) Cs<sub>2</sub>PdBr<sub>6</sub>, (c) Cs<sub>2</sub>PdCl<sub>6</sub>,
(d) Cs<sub>2</sub>TeI<sub>6</sub>, (e) Cs<sub>2</sub>TeBr<sub>6</sub>, (f) Cs<sub>2</sub>TeCl<sub>6</sub> calculated by PBE functional.



**Figure. 18.** Band structures and density of states of the (a) Cs<sub>2</sub>MoI<sub>6</sub>, (b) Cs<sub>2</sub>MoBr<sub>6</sub>, (c) Cs<sub>2</sub>MoCl<sub>6</sub>, (d) Cs<sub>2</sub>SnI<sub>6</sub>, (e) Cs<sub>2</sub>SnBr<sub>6</sub>, (f) Cs<sub>2</sub>SnCl<sub>6</sub> calculated by PBE functional.


Figure. 19. Band structures and density of states of the (a) Cs<sub>2</sub>PtI<sub>6</sub>, (b) Cs<sub>2</sub>PtBr<sub>6</sub>, (c) Cs<sub>2</sub>PtCl<sub>6</sub>,
(d) Cs<sub>2</sub>PbI<sub>6</sub>, (e) Cs<sub>2</sub>PbBr<sub>6</sub>, (f) Cs<sub>2</sub>PbCl<sub>6</sub> calculated by PBE functional.

According to the theoretical calculation results, the bandgap of perovskites containing Zr and Hf is too large for single-junction perovskite solar cells, but structures combining Mo with halogens generated exceptionally narrow bandgaps and may even exhibit metallic properties as shown in Fig. 20. It can be assumed that the researched perovskites, when made up of cesium-based double perovskites, do not have the potential to produce a single solar cell worth looking forward to. Note that for the change of B-site cations in Hf, Zr, and Ti as well as Pt and Pd, the bandgap increases with the ionic radius increase. However, chemical trend was not observed in the Ge, Sn, and Pb. The transition from chloride to bromide to iodide gradually narrows the bandgap; it will have reference significance for the bandgap regulation engineering of perovskites.

Ti	2.21	1.54	0.86		- 4.0
Zr	3.67	2.77	1.8		- 3.5
Ge	2.21	0.93	-0.05	в	- 3.0
Hf	4.2	3.24	2.2	anc	-25
Pd	1.4	0.78	0.13	αŭ 1	2.0
Te	2.68	2.05	1.39	) dt	- 2.0
Mo	-0.08	-0.12	-0.19	eV	- 1.5
Sn	2.57	1.38	0.23	$\smile$	- 1.0
Pt	2.02	1.45	0.61		- 0.5
Pb	1.29	0.23	-0.09		- 0.0
	CI	Br	I		_

Figure. 20. Results of bandgap prescreening of the studied 30 perovskites.

Cs<sub>2</sub>TiBr<sub>6</sub>, Cs<sub>2</sub>TiI<sub>6</sub>, Cs<sub>2</sub>GeBr<sub>6</sub>, Cs<sub>2</sub>PdCl<sub>6</sub>, Cs<sub>2</sub>PdBr<sub>6</sub>, Cs<sub>2</sub>TeI<sub>6</sub>, Cs<sub>2</sub>SnBr<sub>6</sub>, Cs<sub>2</sub>PtBr<sub>6</sub>, Cs<sub>2</sub>PtI<sub>6</sub>, and Cs<sub>2</sub>PbCl<sub>6</sub> were chosen for the calculation of the band structure using HSE+SOC functional, which is well known to give a more accurate estimate for the periodic systems bandgaps, the bandgap of Cs<sub>2</sub>TeI<sub>6</sub> (1.61 eV) belongs to the boundary value of the screening range, so it was also considered. All studied materials calculated bandgaps with HSE+SOC are listed in Table 2, and some experimental bandgaps from other literature studies are included in Table 3. As expected, the theoretical results demonstrate that the bandgap of all materials increased to a certain extent. The exact increase, however, is dependent on specific metals and halogens. From this screening study, 5 perovskites, Cs<sub>2</sub>TiI<sub>6</sub>, Cs<sub>2</sub>GeBr<sub>6</sub>, Cs<sub>2</sub>PtI<sub>6</sub>, Cs<sub>2</sub>PdBr<sub>6</sub>, and Cs<sub>2</sub>TeI<sub>6</sub> were chosen, exhibiting indirect bandgaps except for Cs<sub>2</sub>GeBr<sub>6</sub>, as shown in Fig. 21. The valence band (VB) maximum and the conduction band (CB) minimum are at the GAMMA and X points, respectively. Cs<sub>2</sub>TiI<sub>6</sub>, Cs<sub>2</sub>CeBr<sub>6</sub>, Cs<sub>2</sub>PtI<sub>6</sub>, cs<sub>2</sub>PtI<sub>6</sub>, and Cs<sub>2</sub>PtI<sub>6</sub> were chosen as ideal target materials, and their optical properties were further studied. Note that the bandgaps difference between PBE and HSE + SOC of the studied materials is about 0.6 eV, however this difference seems to be greatly affected by the cations at the B position. Using  $Cs_2TeI_6$  and  $Cs_2PtI_6$  with small and large differences of two functional (PBE and HSE+SOC) bandgaps as a reference, respectively, their experimental bandgaps (1.59 eV of  $Cs_2TeI_6^{19}$  and 1.37 eV of  $Cs_2PtI_6^{11}$ ) are very close to the predicted bandgaps, indicating that the calculation method used for this study is feasible.

Compound	Eg (HSE-SOC) /eV
Cs <sub>2</sub> TiBr <sub>6</sub>	2.16
$Cs_2TiI_6$	1.32
Cs <sub>2</sub> GeBr <sub>6</sub>	1.50
$Cs_2PdCl_6$	2.03
$Cs_2PdBr_6$	1.22
$Cs_2TeI_6$	1.61
$Cs_2SnBr_6$	1.95
$Cs_2PtBr_6$	2.33
$Cs_2PtI_6$	1.39
$Cs_2PbCl_6$	1.99

Table 2 Calculated bandgaps of HSE functional with SOC.

**Table 3** Calculated band gaps with PBE (GGA), HSE+SOC functional and experimental bandgap of Cs2BX6 compounds perovskites.

Compound	Eg (GGA-PBE)/eV	$E_g$ (HSE-SOC) /eV	Expt. /eV
Cs <sub>2</sub> TiCl <sub>6</sub>	2.21		
Cs <sub>2</sub> TiBr <sub>6</sub>	1.54	2.16	2.00 <sup>[31]</sup>
$Cs_2TiI_6$	0.86	1.32	1.02 <sup>[35]</sup>
$Cs_2ZrCl_6$	3.67		
$Cs_2ZrBr_6$	2.77		

Cs <sub>2</sub> ZrI <sub>6</sub>	1.80		
Cs <sub>2</sub> GeCl <sub>6</sub>	2.21		
Cs <sub>2</sub> GeBr <sub>6</sub>	0.93	1.50	
Cs <sub>2</sub> GeI <sub>6</sub>	-0.05		
Cs <sub>2</sub> HfCl <sub>6</sub>	4.20		
Cs <sub>2</sub> HfBr <sub>6</sub>	3.24		
$Cs_2HfI_6$	2.20		
Cs <sub>2</sub> PdCl <sub>6</sub>	1.40	2.03	
Cs <sub>2</sub> PdBr <sub>6</sub>	0.78	1.22	
$Cs_2PdI_6$	0.13		
Cs <sub>2</sub> TeCl <sub>6</sub>	2.68		
Cs <sub>2</sub> TeBr <sub>6</sub>	2.05		
$Cs_2TeI_6$	1.39	1.61	1.59 <sup>[19]</sup>
Cs <sub>2</sub> MoCl <sub>6</sub>	-0.08		
Cs <sub>2</sub> MoBr <sub>6</sub>	-0.12		
Cs <sub>2</sub> MoI <sub>6</sub>	-0.19		
Cs <sub>2</sub> SnCl <sub>6</sub>	2.57		
Cs <sub>2</sub> SnBr <sub>6</sub>	1.38	1.95	
$Cs_2SnI_6$	0.23		
$Cs_2PtCl_6$	2.02		
$Cs_2PtBr_6$	1.45	2.33	2.85 <sup>[66]</sup>
$Cs_2PtI_6$	0.61	1.39	1.37 <sup>[11]</sup>
Cs <sub>2</sub> PbCl <sub>6</sub>	1.29	1.99	
Cs <sub>2</sub> PbBr <sub>6</sub>	0.23		
Cs <sub>2</sub> PbI <sub>6</sub>	-0.09		



Figure. 21. Band structures of the (a) Cs<sub>2</sub>TiI<sub>6</sub>, (b) Cs<sub>2</sub>GeBr<sub>6</sub>, (c) Cs<sub>2</sub>PtI<sub>6</sub>, (d) Cs<sub>2</sub>PdBr<sub>6</sub> and (e) Cs<sub>2</sub>TeI<sub>6</sub> calculated by HSE+SOC method.

The DOS was used to further study the electronic properties of selected compounds. The total density of states (TDOS) and partial density of states (PDOS) plots are shown in Fig. 22. All the materials exhibit a semiconducting nature since the TDOS of VB doesn't go through the Fermi level. Electronic contribution of the individual atoms in the stabilized structure is clarified by the knowledge on orbital properties. It can be seen from Fig. 22a, b, that the Cs orbitals of  $Cs_2TiI_6$  are located deep in the VB (~ -8 eV), making little contribution to the VB and CB near the Fermi level. The d states of Ti exist in the core region of VB (~ -2 eV) and at the bottom of CB. In a valence band edge (VBE), the major contribution comes from the p orbital of I, and the electrons transition from the VB to the CB after the carriers gain energy. For Cs<sub>2</sub>GeBr<sub>6</sub> (Fig. 22c, d), the VBE is mainly contributed by Cs and Br-p orbitals, where Cs is also presented deep in the VB and CB ( $\sim \pm 7$  eV). The CB region near the Fermi level is composed of Br-p orbitals, while Ge-d orbitals mainly contribute to the core region of CB. A similar situation is observed for the Cs<sub>2</sub>PtI<sub>6</sub> (Fig. 22e, f), Cs<sub>2</sub>PdBr<sub>6</sub> (Fig. 22g, h), and Cs<sub>2</sub>TeI<sub>6</sub> (Fig. 22i, j), concerning Cs<sub>2</sub>TiI<sub>6</sub>, the Cs orbitals of these four materials are located far away from the Fermi level, indicating that the Cs has little effect on the band edge states. Moreover, their conduction band edge (CBE) is formed due to the mix contribution of Pt/Pd/Te/Ti-d and Br/I-p orbitals. Through the band states of Cs<sub>2</sub>PtI<sub>6</sub> and Cs<sub>2</sub>PdBr<sub>6</sub>, it can be observed that the d orbitals of B-site metal substituted cations and the p orbitals of halogen ions have obvious interaction, which usually affects

the thermoelectric properties of materials.<sup>48</sup> A minor contribution from other states also exists, but their overall influence can be ignored.



Figure. 22. The DOS of the (a, b) Cs<sub>2</sub>TiI<sub>6</sub>, (c, d) Cs<sub>2</sub>GeBr<sub>6</sub>, (e, f) Cs<sub>2</sub>PtI<sub>6</sub>, (g, h) Cs<sub>2</sub>PdBr<sub>6</sub>, (i, j) Cs<sub>2</sub>TeI<sub>6</sub>. Fermi energy is set to zero.

#### 4.3.3 Optical properties

The energy-dependent dielectric constants ( $\epsilon(\omega)$ ) and optical absorption of these 5 candidate structures (Cs<sub>2</sub>TiI<sub>6</sub>, Cs<sub>2</sub>GeBr<sub>6</sub>, Cs<sub>2</sub>PtI<sub>6</sub>, Cs<sub>2</sub>PdBr<sub>6</sub>, and Cs<sub>2</sub>TeI<sub>6</sub>), which are suitable for solar cells within the appropriate bandgap range were further studied to evaluate their optical properties, as shown in Fig. 23.



**Figure. 23.** Variation of imaginary and real part of dielectric constant of (a) Cs<sub>2</sub>TiI<sub>6</sub>, (b) Cs<sub>2</sub>GeBr<sub>6</sub>, (c) Cs<sub>2</sub>PtI<sub>6</sub>, (d) Cs<sub>2</sub>PdBr<sub>6</sub> and (e) Cs<sub>2</sub>TeI<sub>6</sub>. (f) Optical absorption for 5 studied double perovskite.

The optical properties of solid materials are very sensitive to the nature of bandgap, electron recombination rate as well as electron-photon interaction. Because various optical parameters, e.g., refractive index, absorption, conductivity, reflectivity, and loss function, are calculated by dielectric constant, it is very important to describe the optical properties of any material. The frequency-dependent complex dielectric function can be obtained using Kramers-Kronig equations:

$$\varepsilon(\omega) = \varepsilon_1(\omega) + \varepsilon_2(\omega) \tag{4}$$

which has been calculated using PBE functional, as shown in Fig. 23 (a–e). The  $\omega$  represents the angular frequency of electromagnetic radiations. The  $\varepsilon_1(\omega)$  (real part of the dielectric constant) shows the dispersion and polarization of the impinging light, while the  $\varepsilon_2(\omega)$  (imaginary part) illustrates light absorption by materials. The calculated  $\varepsilon_1(\omega)$  and  $\varepsilon_2(\omega)$  of Cs<sub>2</sub>TiI<sub>6</sub> are plotted

against incident energy in Fig. 23a. The  $\varepsilon_1(0)$  (static dielectric constant) can be extracted from the low energy limit of  $\varepsilon_1(\omega)$ , which starts at 6.43 and changes with the energy of the incident electromagnetic waves. It also appears that there are three resonance peaks of  $\varepsilon_1(\omega)$  in the low energy range at 1.19 eV, 2.67 eV, and 4.15 eV. These peaks express the maximum dispersion of light and specific light energy where it is plane-polarized.<sup>58</sup> In addition, the  $\varepsilon_1(\omega)$  curve goes through zero from the energy of 8.97 eV, while the value of  $\varepsilon_1(\omega)$  is positive in the lower energy region (0-5 eV) and ensures the prevailing semiconducting behavior. <sup>59</sup> If the  $\varepsilon_1(\omega)$  of the dielectric function is negative, which means that the region where the photon is coupled with the plasma will have total reflection and form a quasi-particle called polaron. The larger the dielectric constant, the stronger the ability of the dielectric to bind the electron, and the less likely the electron is to be polarized.<sup>60</sup> Not only Cs<sub>2</sub>Til<sub>6</sub>, but also other compounds studied show good dielectric constants conducive to optical applications in visible spectrum. To further evaluate the application of photoelectric/solar cells, the absorption coefficients  $\alpha(\omega)$  are calculated from  $\varepsilon_1(\omega)$  and  $\varepsilon_2(\omega)$  by using the following equation.

$$\alpha(\omega) = \sqrt{2}\omega \left\{ \sqrt{\varepsilon_1^2(\omega) + \varepsilon_2^2(\omega)} - \varepsilon_1(\omega) \right\}^{\frac{1}{2}}$$
(5)

The calculated values of the  $\alpha(\omega)$  are shown in Fig. 23f, which describes how much light energy is absorbed by the semiconductor. The  $\varepsilon_2(\omega)$  also reflects the light absorption capacity of the material. Comparing the curves of the  $\varepsilon_2(\omega)$  and  $\alpha(\omega)$ , we can find a similar trend, and the displacements of some peaks are due to the different theoretical approximation methods used in the calculation of these two. All the materials studied have several absorption peaks in the energy range of more than 1 eV, which indicates that these materials are perfect for optoelectronic devices functional in ultraviolet and visible light. The Cs<sub>2</sub>TeI<sub>6</sub> has a peak absorption value of about  $0.62 \times 10^6$  cm<sup>-1</sup> in visible spectrum (1.6 – 3.2 eV), which is higher than that of other compounds. In contrast, Cs<sub>2</sub>GeBr<sub>6</sub> only has the lowest absorption peak only at 2.1 eV, which is unfavorable to photoelectric performance in the visible range compared with the absorption curve of other compounds.

### 4.3.4 Solar water splitting

Considering that the bandgap of  $Cs_2TeI_6$ ,  $Cs_2TiBr_6$ ,  $Cs_2PdCl_6$ ,  $Cs_2SnBr_6$ ,  $Cs_2PbCl_6$ , and  $Cs_2PtBr_6$  halide double perovskites is too large for the application of single-junction solar cells,

their performance as photocatalysts in solar water splitting was studied, as shown in Fig. 24. In the photocatalytic reaction, semiconductor compounds are usually in different phases from the reactants, so they are often used as heterogeneous photocatalysts. According to the reaction mechanism displayed in Fig. 24a, when the energy of incident light is greater than the material's bandgap, the excited electrons of semiconductors undergo the interband transition from the VB to the CB, separating holes and photogenerated electrons. After that, the separated holes and electrons can react directly with water molecules adsorbed on the surface-active sites of the photocatalyst to produce  $H_2$  and  $O_2$ . The key to driving the water-splitting reaction is the bandgap and potential of VBE and CBE in semiconductor photocatalyst.



Figure. 24. (a) Schematic diagram of the basic reaction mechanism of the photocatalytic water splitting. (b) Conduction band bottom and Valence band top of the  $Cs_2TeI_6$ ,  $Cs_2TiBr_6$ ,  $Cs_2PdCl_6$ ,  $Cs_2SnBr_6$ ,  $Cs_2PbCl_6$  and  $Cs_2PtBr_6$ . Dotted lines represent the oxidation (O<sub>2</sub>/H<sub>2</sub>O) and reduction (H<sub>2</sub>/H<sup>+</sup>) potential of water.

For the photocatalytic reaction to proceed normally, the top potential of VB of the semiconductor needs to be higher than the redox potential of  $O_2 / H_2O$  (+1.23 V relative to a normal hydrogen electrode (NHE)), while the bottom potential of CB needs to be lower than the redox potential of H<sup>+</sup> / H<sub>2</sub> (0 V relative to NHE). Therefore, the minimum bandgap required to drive the water-splitting reaction is 1.23 eV. According to the thermodynamic theory, the appropriate potential distribution and bandgap position of the photocatalyst with a minimum bandgap of 1.23 eV are the necessary and sufficient conditions for solar water splitting. However, the oxidation and reduction processes of H<sub>2</sub>O are four-electron and two-electron multistep reactions, respectively. There is an activation barrier between water molecules and photocatalyst in the electron transfer process, which leads to the water oxidation and reduction reaction needing a high overvoltage to drive, and the incident photons' energy must be higher than the bandgap of the

photocatalyst. Therefore, the lower limit of bandgap must be much higher than 1.23 eV to drive the whole water splitting. Generally, semiconductors with a bandgap between 1.6 and 2.4 eV have practical value.  $^{61-63}$  The bandgaps of Cs<sub>2</sub>TeI<sub>6</sub>, Cs<sub>2</sub>TiBr<sub>6</sub>, Cs<sub>2</sub>PdCl<sub>6</sub>, Cs<sub>2</sub>SnBr<sub>6</sub>, Cs<sub>2</sub>PbCl<sub>6</sub>, and Cs<sub>2</sub>PtBr<sub>6</sub> halide double perovskites are all in this ideal range based on HSE+SOC calculation. According to the previous research results, the positions of the VBE and CBE can be obtained by the following empirical formula.<sup>64</sup>

$$E_{\rm CBE} = (\chi_{Cs}^2 \chi_B \chi_X^6)^{\frac{1}{9}} - \frac{1}{2} E_g + E_0$$
(6)

$$E_{\rm VBE} = E_{CBE} + E_g \tag{7}$$

Where  $E_{CBE}$  and  $E_{VBE}$  are the CBE and VBE potential of perovskites, respectively. The  $\chi$  refers to the absolute electronegativity of the atoms Cs, B, and X of Cs<sub>2</sub>BX<sub>6</sub>.<sup>65</sup>  $E_g$  is the bandgap, and  $E_0$  is -4.5 eV for NHE, which show the scale factor from the redox level of the reference electrode to the absolute vacuum scale. Fig. 24b and Table 4 show the calculation results of the six double perovskite potentials studied. Among them, the VBE of Cs<sub>2</sub>TeI<sub>6</sub>, Cs<sub>2</sub>TiBr<sub>6</sub>, Cs<sub>2</sub>SnBr<sub>6</sub>, and Cs<sub>2</sub>PtBr<sub>6</sub> is lower than the oxidation potential of water, while the CBE is higher than the standard potential of NHE. The band edge position and wide bandgap of these perovskites indicate that they can be active under visible light and used as photocatalysts for water splitting. These results show that perovskite's properties are strongly related to the composition of B cations and halogen ions.

Table. 4	. The abso	lute ele	ectronegat	tivity (	$\chi$ ), bai	nd gap	$(E_g),$	computed	CBE,	and V	/BE po	otential

Compound	Xcs	$\chi_B$	$\chi_X$	$E_g$ /eV	CBE/eV	VBE/eV
Cs <sub>2</sub> TeI <sub>6</sub>	2.18	5.49	6.76	1.61	-4.33	-5.94
$Cs_2TiBr_6$	2.18	3.45	7.59	2.16	-4.19	-6.35
$Cs_2PbCl_6$	2.18	3.90	8.30	1.99	-4.68	-6.67
$Cs_2PdCl_6$	2.18	4.45	8.30	2.03	-4.74	-6.77
$Cs_2SnBr_6$	2.18	2.77	7.59	1.95	-4.43	-6.38
$Cs_2PtBr_6$	2.18	5.60	7.59	2.33	-4.40	-6.73

at a vacuum level of selected perovskites.

### 4.4 Conclusions

In the context of the growing need for clean energy and attention to environmental protection technology, the development and application of solar cells and photocatalysis are important technologies for renewable energy. However, as a highly concerned photoelectric material and catalyst, the lead-based perovskite cannot be widely accepted due to its toxicity. The environmental friendly materials are urgently needed to overcome the main bottleneck for application. Through the theoretical prediction results of perovskite properties covering various elements, then the promising alternatives can be found to leadcontaining perovskite and the development of environmental friendly materials may be accelerated. In this work, structural, electronic, and optical properties of Cs<sub>2</sub>BX<sub>6</sub> compounds were calculated using first-principles calculations of PBE and HSE-SOC methods, with 30 combinations of B = Ti, Zr, Ge, Hf, Pd, Te, Mo, Sn, Pt, and Pb cations, X = Cl, Br, and I halogen ion. A pre-screen for perovskites based on their stability and predicted bandgaps at PBE level were driven. The calculated enthalpy of formation is negative, which demonstrates that the cesium-based halide perovskite possesses excellent thermal stability at 0 K. The trend of tolerance factor shows that the contribution of Cl<sup>-</sup> to structural stability is greater than Br<sup>-</sup> and I<sup>-</sup>, which is consistent with the calculated formation enthalpy result. The calculated bandgap of perovskites containing Zr and Hf is too large for single-junction perovskite solar cells, while structures combining Mo also gave extremely narrow bandgaps. Furthermore, the theoretical results also revealed that all perovskites studied conforms to the typical trend of replacing halogen (Cl > Br > I) to adjust the bandgap. When the B-site cation belongs to the (Hf, Zr, Ti) group and (Pt, Pd) group, the bandgap value is directly proportional to the cation size of this group. It has guiding significance for applying Cs-based halide double perovskite bandgap engineering. After that, 10 compounds that satisfy the screening criteria were selected, and the HSE+SOC method was used to calculate their bandgap values accurately. The smallest bandgap among selected perovskites is predicted for  $Cs_2PdBr_6$  with a bandgap of 1.22 eV, and the largest one is Cs<sub>2</sub>PtBr<sub>6</sub> with a bandgap of 2.33 eV. The optical properties of perovskites with a bandgap of less than 1.6 eV were studied. They have multiple absorption peaks in the energy range above 1 eV, indicating that they are suitable for optoelectronic devices under visible and ultraviolet light. For perovskites with a bandgap higher than 1.6 eV, their performance as photocatalysts in solar water

splitting was studied. The band edge positions of  $Cs_2TeI_6$ ,  $Cs_2TiBr6$ ,  $Cs_2SnBr_6$ , and  $Cs_2PtBr_6$  are matched the water redox potential. The prediction of stable materials with  $1.22 \sim 2.33$  eV bandgap will be helpful to promote the experimental research for novel optoelectronic devices. The DFT study can provide theoretical guidance and support the rational design of high-performance double perovskites for optoelectronic applications of solar cells and solar water splitting.

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# Chapter 5. Insights into the photocatalytic mechanism of g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>BBr<sub>6</sub> heterojunction photocatalysts by density functional theory calculations

## **5.1 Introduction**

Nowadays the world is facing the challenge of achieving environmental sustainability. Growing pollution, limited energy resources on earth, and increasing energy consumption have driven the need for a cleaner environment and alternative energy sources that can meet human demands in a more environmentally friendly way. Therefore, the current research is greatly accelerated in this direction. Photocatalytic reaction is used to decompose water to generate hydrogen, degrade organic pollutants, reduce CO<sub>2</sub>, and fix N<sub>2</sub>, which can provide a feasible breakthrough for future energy utilization and environmental pollution control.<sup>1,2</sup> Sunlight mainly includes three different kinds of energy radiation (near-infrared (NIR), visible light (vis) and ultraviolet (UV)). According to the light absorption rate of the working photocatalyst, specific energy radiation can be used in the above photocatalytic process. Making full use of sunlight is a key technical issue that should be addressed when designing and developing highly active photocatalysts.<sup>3</sup> In the past decades, more than one hundred kinds of semiconductors have been explored and developed in this field.<sup>2,4-5</sup> Among all the developed photocatalysts, g-C<sub>3</sub>N<sub>4</sub> has aroused great research interest in various fields,<sup>6</sup> especially in the production of hydrogen from water splitting. However, the photogenerated electron-hole pairs with high recombination rate in the isolated g-C<sub>3</sub>N<sub>4</sub> will reduce the photocatalytic efficiency, and its photocatalytic activity is only moderate.<sup>7</sup> As a result, the performance of g-C<sub>3</sub>N<sub>4</sub> based heterojunctions is still unsatisfactory, and the construction of g-C<sub>3</sub>N<sub>4</sub> based heterojunctions with excellent photocatalytic performance still needs further exploration.

The co-catalysts can provide active sites for reduction or oxidation reactions to reduce the activation energy, capture charge carriers and inhibiting the recombination of photogenerated electrons and holes.<sup>8</sup> Therefore, the practical application of g-C<sub>3</sub>N<sub>4</sub> with poor photocatalytic activity strongly usually requires surface cocatalysts with appropriate type and quantity. Many researchers have tried to combine other semiconductors to improve their photocatalytic activity.

g-C<sub>3</sub>N<sub>4</sub>/BiVO<sub>4</sub>,<sup>9</sup> g-C<sub>3</sub>N<sub>4</sub>/LaMnO<sub>3</sub>,<sup>10</sup> g-C<sub>3</sub>N<sub>4</sub>/BiFeO<sub>3</sub>,<sup>11</sup> g-C<sub>3</sub>N<sub>4</sub> modified Ag<sub>3</sub>PO<sub>4</sub>,<sup>12</sup> etc. These heterojunctions show good photocatalytic performance. In the past few years, lead halide perovskite APbX<sub>3</sub> (usually, A=MA<sup>+</sup>, FA<sup>+</sup>, Cs<sup>+</sup>; X= I<sup>-</sup>, Br<sup>-</sup>, Cl<sup>-</sup>), as one of the most attractive semiconductors, has shown great potential in photoelectric applications. Recently, these lead halide perovskite materials have been extended to the field of photocatalysis. Since Park and his colleagues<sup>13</sup> first reported the photocatalytic hydrogen evolution based on MAPbI<sub>3</sub> in saturated HI aqueous solution, people have studied various lead halide perovskite and its composites to improve their hydrogen evolution performance.<sup>14-15</sup> However, the inherent toxicity of lead severely limits the application of lead halide perovskite. To overcome these limitations, researchers are focusing on replacing Pb with non-toxic metals.<sup>16-17</sup> In these alternatives, the use of cesium based lead-free double perovskite or its composites as photocatalysts is rarely reported. Wang et al. reported that Cs<sub>2</sub>AgBiBr<sub>6</sub> double perovskite was first used for the splitting of hydrobromic acid (HBr) under visible light irradiation.<sup>18</sup> Reduced graphene oxide (RGO) with good electron transfer performance and acid stability was introduced to further improve the H<sub>2</sub> production. Tan et al. successfully synthesized Cs<sub>2</sub>SnCl<sub>6</sub>/C<sub>3</sub>N<sub>4</sub> heterojunction photocatalyst by solid grinding method. Through the construction of heterojunction, the charge separation between Cs<sub>2</sub>SnCl<sub>6</sub> and C<sub>3</sub>N<sub>4</sub> has been significantly promoted, and the photocatalytic activity can be effectively improved under visible light irradiation.<sup>19</sup> It is reported that the heterojunction between perovskite and other semiconductor materials can effectively promote charge separation and maintain the stability of photocatalyst.<sup>20</sup> These results indicate that cesium based lead-free double perovskite may be a promising candidate material for photocatalysis and various other photoelectric applications.

In this work, we used density functional theory (DFT) calculations to study the band structure and density of state (DOS) of monolayer  $g-C_3N_4/Cs_2BBr_6$  (B=Pt, Ti, Sn) heterojunctions. In addition, the interaction between  $g-C_3N_4$  and  $Cs_2BBr_6$  (001) surfaces is systematically studied. After  $g-C_3N_4$  contacts with double perovskites, due to the interaction with the interface, the edge positions of the band of the two semiconductors change, and then different kinds of band arrangements are formed. The insight gained of this work is of direct relevance to the design of new photocatalysts relating to  $g-C_3N_4$  or  $Cs_2BBr_6$ .

# **5.2 Calculation methods**

All calculations on the compounds were carried out by the Perdew–Burke–Ernzerhof (PBE)-GGA (generalized gradient approximation) based DFT study in the Vienna Ab initio simulation package (VASP) with a projector augmented waves (PAW) approach.<sup>21-23</sup> The electronic configurations of the Cs, Pt, Sn, Ti, and Br atoms are [Xe]6s<sup>1</sup>, [Xe]5d<sup>9</sup>6s<sup>1</sup>, [Kr]5s<sup>2</sup>5p<sup>2</sup>, [Ar]3d<sup>2</sup>4s<sup>2</sup>, and [Ar]3d<sup>10</sup>4s<sup>2</sup>4p<sup>5</sup>, respectively. The energy cutoff the plane-wave basis for all compounds was set to 500 eV. A Monkhorst–Pack mesh of  $3 \times 2 \times 1$  and  $5 \times 5 \times 1$  K-points is used to sample the Brillouin zone for geometry optimizations and electronic structure calculations, respectively. The vacuum space is set to be at least 15 Å to separate the interactions between neighboring slabs. Geometry optimizations were terminated when the energy and force on each ion were reduced below  $10^{-4}$  eV and 0.05 eV/Å. The band alignment between g-C<sub>3</sub>N<sub>4</sub> and Cs<sub>2</sub>BBr<sub>6</sub> is one central issue of this study. Since PBE functional usually underestimates the band gap of semiconductors,<sup>24</sup> the electronic structures of g-C<sub>3</sub>N<sub>4</sub> and Cs<sub>2</sub>BBr<sub>6</sub> are calculated using Heyd–Scuseria–Ernzerhof (HSE06) hybrid functional and HSE functional with spin-orbit coupling (SOC), respectively.

## 5.3 Results and discussions

#### 5.3.1 Geometry structure and stability

Before checking the properties of g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>PtBr<sub>6</sub>, g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>SnBr<sub>6</sub> and g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>TiBr<sub>6</sub> heterojunctions, we first investigated the lattice structure of Cs<sub>2</sub>BBr<sub>6</sub> (B= Pt, Sn, Ti) bulk and single layer g-C<sub>3</sub>N<sub>4</sub>. In Fig. 1a, the optimized lattice constant of g- g-C<sub>3</sub>N<sub>4</sub> is predicted to be 4.784 Å, which agrees well with previous experimental measurements and theoretical results.<sup>25-26</sup> In the single layer g-C<sub>3</sub>N<sub>4</sub>, there are three atoms in a g-C<sub>3</sub>N<sub>4</sub> unit cell, corresponding to two nitrogen atoms at the edge and corner, and one carbon atom. After structural optimization, the bond lengths of carbon and nitrogen atoms are 1.46 Å and 1.33 Å, which are consistent with previously reported distances of 1.47 and 1.34Å, respectively.<sup>27</sup> The optimized geometry models of Cs<sub>2</sub>PtBr<sub>6</sub>, Cs<sub>2</sub>SnBr<sub>6</sub> and Cs<sub>2</sub>TiBr<sub>6</sub> drawn using the VESTA program are illustrated in Fig. 1b-d, the Cs<sub>2</sub>BBr<sub>6</sub> has a face-centered cubic structure with space group Fm $\bar{3}$ m (No.225), which is alternately formed by isolated [BX<sub>6</sub>] clusters and twisted tetragonal Cs cations (space group P4/mnc). The optimized lattice parameters of Cs<sub>2</sub>PtBr<sub>6</sub>, Cs<sub>2</sub>SnBr<sub>6</sub> and Cs<sub>2</sub>TiBr<sub>6</sub> are 11.04 Å, 10.14 Å and 10.81 Å, respectively.



Figure. 1. Optimized geometric structures of (a) monolayer g-C<sub>3</sub>N<sub>4</sub>,

(b) Cs<sub>2</sub>PtBr<sub>6</sub>, (c) Cs<sub>2</sub>SnBr<sub>6</sub>, and (d) Cs<sub>2</sub>TiBr<sub>6</sub> primitive cell.

The structural parameters of an optimized in this paper are consistent with those reported in earlier reference.<sup>28-30</sup> Schematic representations of the heterojunctions are reported in Fig. 2.  $Cs_2BBr_6$  (001) surface was selected to construct g- $C_3N_4/Cs_2BBr_6$  heterojunction. A vacuum layer of 15 Å is used to isolate the slab as the boundary condition, which is good enough to make interactions between neighboring slabs negligible. To examine the vdW interaction, the mismatch ratio and mismatch energies of the relaxed g- $C_3N_4/Cs_2BBr_6$  heterojunction are calculated after geometry optimization and the results are listed in Table 1. The a% and b% are lattice mismatch ratios of heterojunction occur along the a and b direction, which are less than 3%, and the calculated distance between g- $C_3N_4$  nanosheet and  $Cs_2BBr_6$  (001) surface is 3.5-5 Å. As shown in Fig. 2, there is a strong interaction between nitrogen and perovskite B metal cation at the interface of the two heterojunctions, which leads to the distortion of g- $C_3N_4$  plane and the change of bond angle. It is well known that the interlayer interaction will directly affect the thermodynamic stability of the interface structure of the prepared heterojunctions. To analyze the interaction between  $Cs_2BBr_6$  and g- $C_3N_4$ , the binding energy is calculated by the following formula:

$$E_b = E_{g-C_3N_4/Cs_2BBr_6} - E_{g-C_3N_4} - E_{Cs_2BBr_6}$$
(1)

where  $E_{g-C_3N_4/Cs_2BBr_6}$ ,  $E_{g-C_3N_4}$  and  $E_{Cs_2BBr_6}$  represent the total energies of the relaxed g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>BBr<sub>6</sub>(001) heterojunction, monolayer g-C<sub>3</sub>N<sub>4</sub>, and Cs<sub>2</sub>BBr<sub>6</sub>(001) slab, respectively. Negative binding energy indicates that g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>BBr<sub>6</sub> composites can form stable interfaces. The calculated binding energy of g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>PtBr<sub>6</sub> is -4.2979 eV, which indicates that there is a strong interaction between the g-C<sub>3</sub>N<sub>4</sub> layer and the Cs<sub>2</sub>PtBr<sub>6</sub> layer. In contrast, Cs<sub>2</sub>SnBr<sub>6</sub> and Cs<sub>2</sub>TiBr<sub>6</sub> are not as stable as the other two heterojunctions. In addition, the lattice mismatch energy can also roughly evaluate the stability of the heterojunction. The lattice mismatch energy of the studied composites can be estimated as

$$E_{mismatch} = E_{g-C_3N_4} + E_{Cs_2BBr_6} - E'_{g-C_3N_4} - E'_{Cs_2BBr_6}$$
(2)

where  $E_{g-C_3N_4}$  and  $E_{Cs_2BBr_6}$  are the total energies of the isolated monolayer g-C<sub>3</sub>N<sub>4</sub> and isolated Cs<sub>2</sub>BBr<sub>6</sub>(001) with the equilibrium lattice constant of the g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>BBr<sub>6</sub> heterojunction, respectively. The  $E'_{g-C_3N_4}$  and  $E'_{Cs_2BBr_6}$  represent the total energies of the isolated monolayer g-C<sub>3</sub>N<sub>4</sub> and Cs<sub>2</sub>BBr<sub>6</sub>(001) after all free geometry relaxation, respectively. The calculated lattice mismatch energies in this work are 4.15 eV for Cs<sub>2</sub>PtBr<sub>6</sub>, 10.26 eV for Cs<sub>2</sub>SnBr<sub>6</sub>, and 6.26 eV for Cs<sub>2</sub>TiBr<sub>6</sub>, which indicate that the lattice match of model Cs<sub>2</sub>PtBr<sub>6</sub> is superior to that of Cs<sub>2</sub>SnBr<sub>6</sub> and Cs<sub>2</sub>TiBr<sub>6</sub>.



Figure. 2. Theoretical models for (a) g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>PtBr<sub>6</sub>, (b) g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>SnBr<sub>6</sub>, and (c) g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>TiBr<sub>6</sub> heterojunctions. Optimized geometric structures of (d) g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>PtBr<sub>6</sub>, (e) g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>SnBr<sub>6</sub>, and (f) g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>TiBr<sub>6</sub> heterojunctions.

**Table. 1.** The lattice mismatch ratios, mismatch energies (eV) and binding energies (eV) of g-<br/> $C_3N_4/Cs_2BBr_6$  using GGA-PBE functional.

Species	g-C <sub>3</sub> N <sub>4</sub> / Cs <sub>2</sub> PtBr <sub>6</sub>	g-C <sub>3</sub> N <sub>4</sub> / Cs <sub>2</sub> SnBr <sub>6</sub>	g-C <sub>3</sub> N <sub>4</sub> / Cs <sub>2</sub> TiBr <sub>6</sub>
a%	0.3	2.8	0.8
b%	0.9	2.8	1.0
Binding energy (eV)	-4.2979	-1.6596	-2.8896
Mismatch energy (eV)	4.1542	10.2574	6.2574

#### **5.3.2 Electronic properties**

In order to study the photocatalytic activity of  $g-C_3N_4/Cs_2BX_6$  heterojunction, we calculated the band structure of the heterojunction using PBE functional. At the same time, the bands of monolayer  $g-C_3N_4$  and  $Cs_2BX_6$  (001) surfaces were calculated by using HSE06 functional for comparison. The band structure is shown in Fig. 3. The monolayer layer  $g-C_3N_4$  is a direct bandgap semiconductor, where the valence band maximum (VBM) and conduction band minimum (CBM) are at GAMMA-point (Fig. 3a). The calculated bandgap is 2.73 eV, which is very consistent with the experimental value (2.7 eV) and the previous calculation results.<sup>31-32</sup>



**Figure. 3.** Calculated band structure of (a) monolayer g-C<sub>3</sub>N<sub>4</sub>, (b) Cs<sub>2</sub>PtBr<sub>6</sub>(001) slab, (c) Cs<sub>2</sub>SnBr<sub>6</sub>(001) slab, (d) Cs<sub>2</sub>TiBr<sub>6</sub>(001) slab using HSE06 functional. The vertical line is Fermi level.

The total density of state (TDOS) and projected density of state (PDOS) are shown in Fig. 4. In DOS of  $g-C_3N_4$  (Fig. 4a), the s-orbital electrons of N atom and the s-orbital electrons of C atom only occupy the state far away from VBM. The VBM is dominated by

N-p orbitals, while CBM is mainly contributed by N-p and C-p orbitals. Therefore, excited electron holes located on adjacent carbon and nitrogen atoms will be easily recombined according to this distribution, which leads to relatively low quantum yields. In other words, the possible high recombination probability of photogenerated carriers leads to the unsuitable band structure of g-C<sub>3</sub>N<sub>4</sub> as a qualified photocatalyst for many catalytic reactions.<sup>33</sup> Cs<sub>2</sub>PtBr<sub>6</sub> (001) slabs have indirect bandgap, its CBM is at X-point, and its VBM is at GAMMA-point (Fig. 3b). The calculated  $E_g$  is 2.11eV, which is close to the theoretical bandgap (2.23 eV) of other calculated bulk Cs<sub>2</sub>PtBr<sub>6</sub>.<sup>42</sup> The PDOS analysis of Cs<sub>2</sub>PtBr<sub>6</sub> (001) surface shows that VBM is largely contributed by Br-p state, while CB is attributed to 5d of Pt and 4p state of Br (Fig. 4b). The calculated band structure and DOS of Cs<sub>2</sub>SnBr<sub>6</sub> (001) slab are plotted in Fig. 3c and Fig. 4c, respectively. Obviously, this perovskite is a semiconductor with a direct bandgap of 2.65 eV, which is consistent with the experimental bandgap of 2.7 eV.<sup>34</sup> Both CBM and VBM are located at the GAMMA point. This direct bandgap facilitates the easier transfer of electrons from VBM to CBM. The VB of the Cs<sub>2</sub>SnBr<sub>6</sub> (001) surface is mainly dominated by the Br-p state, while the CBM is mainly attributed to the Sn-d and Br-p states. The Cs orbit mainly contributes to the region far from the Fermi level. In Fig. 3d, the band structure results indicate that  $Cs_2TiBr_6$  (001) is also an indirect bandgap (2.09 eV) semiconductor, which agrees well with experimental value (2.0 eV).<sup>35</sup> By analysing the PDOS of Cs<sub>2</sub>TiBr<sub>6</sub> (001) (Fig. 4d), we can see that the electronic states near CBM and VBM are mainly contributed by Ti-d orbit and Br-p orbit. There is a strong hybridization between the Ti-3d orbitals and the Br-4p orbitals.



Figure. 4. Calculated TDOS and PDOS of (a) monolayer g-C<sub>3</sub>N<sub>4</sub>, (b) Cs<sub>2</sub>PtBr<sub>6</sub>(001) slab, (c) Cs<sub>2</sub>SnBr<sub>6</sub>(001) slab, (d) Cs<sub>2</sub>TiBr<sub>6</sub>(001) slab. The vertical line is Fermi level.

To describe the g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>BBr<sub>6</sub> interaction more clearly, it is insightful to analyze their electronic structures. The band structure and total DOS of g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>PtBr<sub>6</sub> (001), g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>SnBr<sub>6</sub> (001) and g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>TiBr<sub>6</sub> (001) composites and the PDOS of perovskite and g-C<sub>3</sub>N<sub>4</sub> monolayer are shown in Fig 5a-c. Although PBE functional tends to underestimate the band gap value, by comparing the band structures of heterojunctions g-C<sub>3</sub>N<sub>4</sub> and Cs<sub>2</sub>BBr<sub>6</sub>, the bandgap of composite materials is reduced to a certain extent, which is due to the interaction between g-C<sub>3</sub>N<sub>4</sub> and perovskites layer. The bandgap values of g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>PtBr<sub>6</sub> (001), g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>SnBr<sub>6</sub> (001) are 0.83eV, 0.49 eV and 0.56 eV respectively. It is possible that the electric field will be formed at the interface of g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>BBr<sub>6</sub> heterojunction. In particular, the interaction between B-site cation of Cs<sub>2</sub>BBr<sub>6</sub>, and N atoms will lead to the redistribution of electronic state density, and change the relative state positions at C, N and B-site cation. The combination of g-C<sub>3</sub>N<sub>4</sub> and perovskite leads to the redistribution of N-p state, which provides more electrons to participate in the d orbital state of the B atom at the CBM. The charge compensation effect between B-d and N-p reduces the transition energy of electrons from VB to CB. Therefore, the bandgap of heterojunction is much smaller than that of monolayer g-C<sub>3</sub>N<sub>4</sub> and isolated

perovskites. This result is somewhat similar to the band gap of previously reported  $g-C_3N_4/WS_2^{36}$ ,  $g-C_3N_4/CdS^{37}$  and  $g-C_3N_6/TiO_2^{38}$  heterojunctions, and due to the coupling between planes, the band distribution of the three heterojunctions near the Fermi level changes slightly. As shown in Fig. 5, the figure of the computed DOS projected on two different layers in the proposed hybrid nanocomposite is similar to the TDOS isolating Cs<sub>2</sub>PtBr<sub>6</sub>, Cs<sub>2</sub>SnBr<sub>6</sub>, Cs<sub>2</sub>TiBr<sub>6</sub> and  $g-C_3N_4$  monolayers. It is easy to understand, because the separation between the perovskite and  $g-C_3N_4$  is relatively large, there is no covalent bond when the mixed interface is formed.<sup>25</sup>



Figure. 5. Band structure and partial density of states of the (a) g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>PtBr<sub>6</sub>, (b) g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>SnBr<sub>6</sub>, (c) g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>TiBr<sub>6</sub> heterojunctions by PBE functional.

#### 5.3.3 Charge density difference and mechanism analysis

The work function( $\phi$ ) analysis can help us understand the origin of interfacial charge transfer. <sup>37</sup> The reactivity of the photocatalyst is evaluated by its work function, which is well defined as the minimum energy required to remove electrons from the solid surface to the vacuum level. The work function is given by the following formula:

$$\phi = E_{Vacuum} - E_F \tag{3}$$

where  $E_{vacuum}$  and  $E_F$  represent the energy of a stationary electron in the vacuum near the surface and the Fermi energy, respectively. The vacuum energy is the average potential energy on the plane parallel to the heterojunction. The average plane electron potential obtained about the Z-axis is shown in Fig. 6. On the basis of eq 3, the work functions of g-C<sub>3</sub>N<sub>4</sub> supercell, Cs<sub>2</sub>PtBr<sub>6</sub> (001) supercell, and g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>PtBr<sub>6</sub> (001) heterojunction were 4.35, 6.52, and 6.14 eV, respectively. The results are illustrated in Fig. 6a-c. For g-C<sub>3</sub>N<sub>4</sub> supercell, Cs<sub>2</sub>SnBr<sub>6</sub> (001) supercell, and g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>SnBr<sub>6</sub> (001) heterojunction, the work functions are estimated to be 4.28, 5.50 and 5.23eV respectively, and shown in Fig. 6d-f. Fig. 6g-i show the calculated work function of g-C<sub>3</sub>N<sub>4</sub> supercell, Cs<sub>2</sub>TiBr<sub>6</sub> (001) heterojunction, respectively. The calculated work functions of the g-C<sub>3</sub>N<sub>4</sub> is almost consistent with that reported previously.<sup>37</sup> The difference of work functions between g-C<sub>3</sub>N<sub>4</sub> and Cs<sub>2</sub>BBr<sub>6</sub> shows that when g-C<sub>3</sub>N<sub>4</sub> contacts Cs<sub>2</sub>BBr<sub>6</sub>, electrons flow from g-C<sub>3</sub>N<sub>3</sub> to Cs<sub>2</sub>BBr<sub>6</sub>.

In the photocatalytic reaction, when the light ( $hv \ge e^{-}$ ) falls on the semiconductor material and is excited from the VB to the CB, leaving holes ( $h^+$ ). This is the basic step involved in all photocatalytic processes, as shown in Eq 4. In particular, the energy should be higher so that the photogenerated charge can migrate to the surface of the photocatalyst, thus participating in the redox reaction. These electrons and holes can be used in various photocatalytic reactions as long as their reduction potential meets the application requirements. Eqs 5-8 give descriptions of the general reactions and reduction potential involved in organic pollutant degradation, H<sub>2</sub> generation, CO<sub>2</sub> reduction and N<sub>2</sub> fixation, and the relevant reaction potentials are shown in Fig. 7.<sup>2</sup> All these conditions may be slightly different during the experiment, because not every reaction is carried out at pH=0 or 7.

photocatalyst + 
$$hv \rightarrow$$
 photogenerated charges (e<sup>-</sup> and h<sup>+</sup>) (4)

pollutant molecules + reactive species  $\rightarrow$  degraded products

$$2\mathrm{H}^{+} + 2\mathrm{e}^{-} \to \mathrm{H}_{2} \tag{6}$$

(5)

$$CO_2 + xH^+ + xe^- \rightarrow useful \text{ products}$$
 (7)



**Figure. 6**. Calculated electrostatic potentials for (a) monolayer  $g-C_3N_4$  of the  $g-C_3N_4/Cs_2PtBr_6$  heterojunction, (b)  $Cs_2PtBr_6(110)$  surface, and (c)  $g-C_3N_4/Cs_2PtBr_6$  heterojunction slab model;

Calculated electrostatic potentials for (d) monolayer  $g-C_3N_4$  of the  $g-C_3N_4/Cs_2SnBr_6$ heterojunction, (e)  $Cs_2SnBr_6(110)$  surface, and (f)  $g-C_3N_4/Cs_2SnBr_6$  heterojunction slab model;

Calculated electrostatic potentials for (g) monolayer  $g-C_3N_4$  of the  $g-C_3N_4/Cs_2TiBr_6$ heterojunction, (h)  $Cs_2TiBr_6(110)$  surface, and (i)  $g-C_3N_4/Cs_2TiBr_6$  heterojunction slab model.



Figure. 7. Schematic illustration of photoexcitation in a photocatalyst and reduction potential values for the formation of different photocatalytic products at pH = 0 vs. NHE.

The mechanism of photocatalytic water decomposition and pollutant degradation mainly depends on the generation, separation, transfer and participation of photoinduced charge carriers.<sup>39</sup> In order to understand the influence of photogenerated charge carriers on the recombination behaviour and redox reaction in g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>BBr<sub>6</sub> heterojunction, the band edge positions of g-C<sub>3</sub>N<sub>4</sub>, Cs<sub>2</sub>PtBr<sub>6</sub>, Cs<sub>2</sub>SnBr<sub>6</sub>, and Cs<sub>2</sub>TiBr<sub>6</sub> were calculated using empirical eqs 9-10:<sup>40</sup>

$$E_{\rm CBE} = E_{CBE} + E_g \tag{9}$$

$$E_{\rm VBE} = \left(\chi_{Cs}^2 \chi_B \chi_{Br}^6\right)^{\frac{1}{9}} - \frac{1}{2} E_g + E_0 \tag{10}$$

Where  $E_{CBE}$  and  $E_{VBE}$  are the CBE and VBE potential of perovskites, respectively. The  $\chi$  refers to the absolute electronegativity of the atoms Cs, B, and Br of Cs<sub>2</sub>BBr<sub>6</sub>.  $E_g$  is the bandgap, and  $E_0$  is -4.5 eV for NHE, which show the scale factor from the redox level of the reference electrode to the absolute vacuum scale. The results are shown in left part of Fig. 8, the calculated band edge position of g-C<sub>3</sub>N<sub>4</sub> and Cs<sub>2</sub>BBr<sub>6</sub> are their potential before contact. When g-C<sub>3</sub>N<sub>4</sub> contacts Cs<sub>2</sub>BBr<sub>6</sub>, the heterojunctions are formed, and the relative positions of CB and VB change with the Fermi level. Therefore, it is very important to accurately calculate the changes of CB and VB positions after contact to determine the redox ability of g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>BBr<sub>6</sub> heterojunctions. Fig. 8a shows that the work function (6.52 eV) of  $Cs_2PtBr_6$  is higher than that of g-C<sub>3</sub>N<sub>4</sub> (4.35eV), which causes electrons to move from g-C<sub>3</sub>N<sub>4</sub> to  $Cs_2PtBr_6$  until the Fermi energies of the two semiconductors align. The work function (6.14 eV) of g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>PtBr<sub>6</sub> heterojunction is between that of g-C<sub>3</sub>N<sub>4</sub> and Cs<sub>2</sub>PtBr<sub>6</sub>. Due to electron transfer, when the two components reach the same Fermi energy level, the built-in electric field from the g-C<sub>3</sub>N<sub>4</sub> sheet to the Cs<sub>2</sub>PtBr<sub>6</sub> surface will be established. For heterojunctions, a potential well is formed between the g-C<sub>3</sub>N<sub>4</sub> and the Cs<sub>2</sub>PtBr<sub>6</sub>. The built-in potential can stop the charge diffusion between the g-C<sub>3</sub>N<sub>4</sub> and Cs<sub>2</sub>PtBr<sub>6</sub>. Similarly, since the work function of g-C<sub>3</sub>N<sub>4</sub> is smaller than that of Cs<sub>2</sub>SnBr<sub>6</sub> (5.50 eV) and Cs<sub>2</sub>TiBr<sub>6</sub> (4.73 eV), the work function of the heterojunction is also between them. Negative charges accumulate on the surface areas of Cs<sub>2</sub>SnBr<sub>6</sub> and Cs<sub>2</sub>TiBr<sub>6</sub>. On the contrary, the g-C<sub>3</sub>N<sub>4</sub> layer accumulates positive charges. The net positive and negative charges induce the internal electric field from g-C<sub>3</sub>N<sub>4</sub> to Cs<sub>2</sub>BBr<sub>6</sub>. The internal electric field at the interface generates another force on holes and electrons, which is opposite to the diffusion force. In thermal equilibrium, electric field force and diffusion force reach equilibrium.

With the change of Fermi energy, VB and CB of g-C<sub>3</sub>N<sub>4</sub> move down 1.79 eV in g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>PtBr<sub>6</sub>, while VB and CB of Cs<sub>2</sub>PtBr<sub>6</sub> move up 0.38 eV. According to the analysis in Fig 8a, after the contact of the two semiconductors, the CBM in Cs<sub>2</sub>PtBr<sub>6</sub> is higher than g-C<sub>3</sub>N<sub>4</sub>, while the VBM in g-C<sub>3</sub>N<sub>4</sub> is lower than Cs<sub>2</sub>PtBr<sub>6</sub>. VB offset (VBO) and CB offset (CBO) are the relative positions of VBM and CBM on both sides of the interface, respectively. They are the key factors affecting the photocatalytic performance of g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>PtBr<sub>6</sub> heterojunctions. When the g- $C_3N_4/Cs_2PtBr_6$  heterojunction absorbs photon energy under visible light irradiation, an electronic transition from VB to CB occurs, and photogenerated holes are generated in VB. The presence of CBO induces the photogenerated electrons in the CB of Cs<sub>2</sub>PtBr<sub>6</sub> to transfer to the CB of g-C<sub>3</sub>N<sub>4</sub>. On the contrary, the existence of VBO leads to the transfer of photogenerated holes in VB of g-C<sub>3</sub>N<sub>4</sub> to VB in Cs<sub>2</sub>PtBr<sub>6</sub>, which leads to the accumulation of electrons at CB of g-C<sub>3</sub>N<sub>4</sub> and holes at VB of Cs<sub>2</sub>PtBr<sub>6</sub>. In addition, the internal electric field in the g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>PtBr<sub>6</sub> heterojunction acts as a selector. This field promotes the movement of photogenerated electrons from CB in Cs<sub>2</sub>PtBr<sub>6</sub> to CB in g-C<sub>3</sub>N<sub>4</sub>, and the movement of photogenerated holes from VB in g-C<sub>3</sub>N<sub>4</sub> to VB in Cs<sub>2</sub>PtBr<sub>6</sub>. At the same time, the reverse motion of photogenerated electrons and holes is inhibited. Therefore, under the combined action of band offset and built-in electric field, photogenerated electrons and holes are effectively separated on different surfaces.<sup>41</sup> Similar to g $C_3N_4/Cs_2PtBr_6$ , g- $C_3N_4/Cs_2SnBr_6$  heterojunction also forms a type II staggered band arrangement, which is conducive to the separation and transfer of photoinduced electrons and holes. After the two semiconductors g- $C_3N_4$  and  $Cs_2SnBr_6$  contact, the VB edge position of g- $C_3N_4$  becomes 2.71 eV, which is more positive than OH<sup>-</sup>/HO\* (1.89 eV). The CB edge position of  $Cs_2SnBr_6$  becomes -1.04 eV, which is more negative than the CB edge position of  $Cs_2PtBr_6$  in g- $C_3N_4/Cs_2PtBr_6$ heterojunction, and can cover the potential required by most nitrogen catalytic reactions. The VBM of g- $C_3N_4$  is lower than that of  $Cs_2TiBr_6$ , and the CBM is higher than that of  $Cs_2TiBr_6$ . However, after the contact between the two, the VB edge of  $Cs_2TiBr_6$  changes to the negative direction and is finally lower than that of g- $C_3N_4$ . Compared with  $Cs_2TiBr_6$ , g- $C_3N_4$  is a semiconductor photocatalyst with highly negative CB and highly positive VB, which forms a type I (straddling gap) heterojunction after contact. This heterojunction will accumulate photogenerated charge on  $Cs_2TiBr_6$ , so it is not conducive to photocatalysis.



Figure. 8. Diagram of the band edge positions before and after contact of (a) g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>PtBr<sub>6</sub>, (b) g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>SnBr<sub>6</sub>, (c) g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>TiBr<sub>6</sub> heterojunction photocatalysts.

# **5.4 Conclusions**

In conclusion, the structural, electronic properties and photocatalytic mechanism of g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>BBr<sub>6</sub> were systematically investigated by performing first-principles calculations. When they are close to each other, the two layers of  $g-C_3N_4$  and  $Cs_2BBr_6$  can produce obvious synergistic effect, which can lead to the distortion of g-C<sub>3</sub>N<sub>4</sub> plane and lattice structure change. The combination of Cs<sub>2</sub>BBr<sub>6</sub> and g-C<sub>3</sub>N<sub>4</sub> can obtain a narrower band gap than the isolated one. Our calculation results show that both g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>PtBr<sub>6</sub> and g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>SnBr<sub>6</sub> heterojunctions have indirect band gaps, while g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>TiBr<sub>6</sub> heterojunctions have direct band gaps. The band gap values of g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>PtBr<sub>6</sub>, g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>SnBr<sub>6</sub> and g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>TiBr<sub>6</sub> are 0.83, 0.49 and 0.56 eV, respectively. By analyzing the work function and the energy level matching between the two semiconductors, it can be inferred that negative charges accumulate on the surface areas of  $Cs_2BBr_6$ . On the contrary, the g- $C_3N_4$  layer accumulates positive charges. The net positive and negative charges induce the internal electric field from g-C<sub>3</sub>N<sub>4</sub> to Cs<sub>2</sub>BBr<sub>6</sub>. The internal electric field at the interface generates another force on holes and electrons, which is opposite to the diffusion force. The calculated band arrangement between  $g-C_3N_4$  monolayer and  $Cs_2BBr_6$  (001) surface shows that the g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>PtBr<sub>6</sub> and g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>SnBr<sub>6</sub> heterojunction forms a type II staggered band arrangement. The g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>TiBr<sub>6</sub> forms a type I (straddling gap) heterojunction after contact. The type II heterojunction is conducive to the separation and transfer of photoinduced electrons and holes. The type I heterojunction will accumulate photogenerated charge on Cs2TiBr6 and hinder transmission, so it is not conducive to photocatalysis.

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### **Chapter 6. General conclusions and future prospects**

In this thesis, we mainly focused on find potential materials suitable for solar cells or photocatalysts in Cs Based Vacancy Ordered Double Perovskites. Firstly, we simulated and optimized the structure of the Cs<sub>2</sub>PtI<sub>6-y</sub>Cl<sub>y</sub>, Cs<sub>2</sub>PtI<sub>6-y</sub>Br<sub>y</sub>, and Cs<sub>2</sub>PtBr<sub>6-y</sub>Cl<sub>y</sub> (y = 0, 1, 2, 3, 4, 5, 6) and systematically studied their electronic properties. Secondly, we investigate the structural, electronic, and optical properties of Cs<sub>2</sub>BX<sub>6</sub> compounds, with the goal of finding suitable candidates for photocatalysts and perovskite solar cells. Thirdly, the structural, electronic properties and photocatalytic mechanism of g-C<sub>3</sub>N<sub>4</sub>/Cs<sub>2</sub>BBr<sub>6</sub> were systematically investigated by performing first-principles calculations.

In chapter 1, the background and development status of photovoltaic technology and photocatalysis, including the classification of devices and photocatalysts, and the basic principles of solar cells and photocatalysis are introduced.

In chapter 2, the density functional theory and calculation methods based on which this paper is based are introduced, and the calculation tools used are listed.

In chapter 3, we performed a first-principles investigation based on density functional theory to study the structural and electronic properties of  $Cs_2PtI_{6-y}Cl_y$ ,  $Cs_2PtI_{6-y}Br_y$ ,  $Cs_2PtBr_{6-y}Cl_y$  (y = 0, 1, 2, 3, 4, 5, 6). The calculated structural parameters revealed a good mechanical stability for all these compounds, and the trend in the formation energy indicated that the substitution of I<sup>-</sup> with Cl<sup>-</sup> and Br<sup>-</sup> can significantly reduce the energy and improve the thermodynamic stability. Through a comparative analysis of the electronic properties of  $Cs_2PtX_6$  (X = Cl, Br, I), we found that the substitutional doping of halogen ions can effectively adjust the bandgap and show an obvious trend.

In chapter 4, Screening homovalent alternatives for B and X-site ions in vacancy-ordered double perovskite Cs<sub>2</sub>BX<sub>6</sub> for solar cell applications and photocatalyst was done using Perdew–Burke–Ernzerhof and Heyd–Scuseria–Ernzerhof functional with spin-orbit coupling. Three empirical factors and formation enthalpy were used to evaluate the stability of 30 materials at different temperatures. Finally, the Cs-based vacancy-ordered double perovskites with suitable bandgap for optoelectronic applications can thus be obtained.

In chapter 5, the structural, electronic properties and photocatalytic mechanism of g- $C_3N_4/Cs_2BBr_6$  were systematically investigated by performing first-principles calculations.

The bandgap of three heterojunction of three heterojunction are 0.83eV, 0.49 eV and 0.56 eV respectively, which will be smaller than that of the isolated semiconductor. The difference of work functions between  $g-C_3N_4$  and perovskite shows that when two semiconductor contacts, electrons will transfer from  $g-C_3N_4$  layer to perovskites layer. According to the work function and band edge position of the semiconductor, it can be found  $Cs_2PtBr_6$  based and  $Cs_2SnBr_6$  based heterojunction belong to Type II. The  $Cs_2TiBr_6$  based heterojunction belongs to Type I.

The prospects of the research content may include the following aspects. 1. Synthesize  $Cs_2PtI_yBr_{6-y}$  and characterize the performance of perovskite solar cells by experiments. 2. Calculate the properties of Rb based vacancy ordered double perovskites and predict their potential application value. 3. Calculate the differential charge density of  $g-C_3N_4/Cs_2TiBr_6$  heterojunction to support the conclusion. We present the guiding value of theoretical research for experiments with an optimistic attitude, and believe that this field will successfully predict the perovskite solar cell materials and photocatalysts with practical value in the future.

# Achievements

#### **Publications**

- <u>Xinvu Ye</u>, Anmin Liu\*, Liguo Gao, Chu Zhang, Lijing Yan, Shizheng Wen, Tingli Ma\*. High-Performance Computational screening of Cs based vacancy-ordered double perovskites for solar cell and photocatalysis applications. *EcoMat*. 2022, e12295.
- Xinvu Ye, Anmin Liu\*, Yue Zhao, Qianji Han, Takeshi Kitamura, Tingli Ma\*. DFT study of X-site ion substitution doping of Cs<sub>2</sub>PtX<sub>6</sub> on its structural and electronic properties. *Int. J. Energy Res.* 2022, 46, 8471-8479.

#### Conferences

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 <u>Xinyu Ye</u>, Chu Zhang, Tingli Ma. "Studies on Development of New Materials and Improvement Stability of Perovskite Solar Cells", 19th "Next-Generation Photovoltaic Power Generation System" Symposium (2nd Annual Meeting of the Japan Photovoltaic Energy Society). Online, June 28th - 29th 2022.

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