# Effects of the Tucson-Melbourne three-nucleon force in the proton-deuteron breakup process at $E_{p}=65 \mathrm{MeV}$ 

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#### Abstract

We present the calculated cross sections and vector analyzing powers using the Bonn B nucleon-nucleon potential and the Tucson-Melbourne three-nucleon force ( $3 N F$ ) for six collinearity and quasi-free scattering breakup configurations. These calculations are compared to the results of the recent kinematically complete $p d$ experiments at $E_{p}=65 \mathrm{MeV}$. The TucsonMelbourne $3 N F$, adjusted together with the Bonn B potential to reproduce the triton binding energy, leads to small effects both in cross sections and analyzing powers in all six studied configurations.


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## 1. Introduction

The three-nucleon ( $3 N$ ) system plays a special role in the study of the nucleon-nucleon ( $N N$ ) interaction. It is the simplest few-nucleon system, in which it is possible to get an exact solutions for both bound and continuum states, and thus it is particularly suitable for testing the underlying nuclear dynamics. The presence of a third nucleon may introduce an additional term in the potential part of the nuclear Hamiltonian not present in the 2 N subsystems, the so-called threenucleon interaction. An interesting question arises: is a simple picture of three nucleons interacting pairwise

[^0]with a free $N N$ potential sufficient or do we have to supplement it by a three-nucleon force ( 3 NF ) in order to understand 3 N systems?
In the past ${ }^{3} \mathrm{H}$ and ${ }^{3} \mathrm{He}$ nuclei, the two 3 N bound states existing in nature, were extensively studied using modern $N N$ interactions as well as different $3 N F$ [1]. These studies show that all existing realistic $N N$ potentials underbind ${ }^{3} \mathrm{H}$ by about 0.8 MeV . For local $N N$ interactions this difference can be attributed to a $3 N$ force. For nonlocal NN forces, eg Bonn potentials [2,3], some part of this difference can be ascribed to nonlocality, leaving smaller gap between experimental and theoretical binding energy. From different models of a three-nucleon interaction the most extensively used was a $2 \pi$-exchange model of the $3 N F$ proposed
by the Tucson-Melbourne Collaboration (TM 3NF) [4]. Such a force has the largest range due to the small mass of exchanged $\pi$-mesons.

The $3 N$ continua, the nucleon-deuteron elastic scattering and deuteron breakup processes, offer a much broader opportunity for testing the underlying nuclear dynamics than the 3 N bound state. The deuteron breakup process is of special interest due to the possibility of choosing different geometries of the outgoing nucleons making it more selective with respect to the interaction. The theoretical formalism together with the corresponding numerical algorithms has been developed which allows to solve the 3 N Faddeev equations in continuum using any type of realistic $2 N$ forces [5] with the same rigorousness and precision as in case of 3 N bound state. The same applies for the inclusion of $3 N F s$ [6], though present day computer resources still pose some limitations.

From the bulk of $3 N$ data analyzed by us up to now we have found that a simple Hamiltonian composed of realistic 2 -body $N N$ forces only describes quite well the elastic $N d$ scattering and the breakup process [7]. Some possible important exceptions are pointed out in Ref. [7]. This description is quite stable with respect to replacing one $N N$ force by another, as long as they describe the 2 N data equally well. Thus the present $N N$ forces leave only a little space for $3 N$ force effects. This conclusion seems to be supported by recent theoretical studies based on an effective chiral Lagrangian approach [8].

In this work we study the effects of the $\pi-\pi$ exchange $T M 3 N F$ in specific, kinematically complete configurations of the deuteron breakup measured recently at PSI using a proton beam with an energy $E_{p}=$ $65 \mathrm{MeV}[9,10]$. These configurations include the socalled quasi-free scattering (QFS) and collinearity geometries, where the not-detected nucleon (neutron) is at rest in the laboratory and c.m. system, respectively.

## 2. Theory

The inclusion of a $3 N F, V_{4}$, into the 3 N scattering formalism amounts to solving the set of coupled equations for two operators $T$ and $T_{4}$ of the form

$$
\begin{equation*}
T=t P+t G_{0} T_{4}+t P G_{0} T, \tag{1}
\end{equation*}
$$

$T_{4}=(1+P) t_{4}+(1+P) t_{4} G_{0} T$.
Here $t$ is the 2 -body $t$-operator driven by the 2 N interaction, $G_{0}$ is the free $3 N$ propagator, $P$ is a sum of cyclic and anticyclic permutations of three nucleons and $t_{4}$ is generated by $V_{4}$ through a LippmannSchwinger type equation:
$t_{4}=V_{4}+V_{4} G_{0} t_{4}$.
The operators $T$ and $T_{4}$ determine the transition operator $U_{0}$ for the breakup process
$U_{0}=(1+P) T+T_{4}$.
Both operators $T$ and $T_{4}$ act on the incoming channel state composed of the deuteron wave function and a momentum eigenstate of the relative nucleondeuteron motion. The breakup amplitude is then given by $\left\langle\phi_{0}\right| U_{0}|\phi\rangle$ with the state $\phi_{0}$ describing the free motion of three outgoing nucleons.

Iterating the set of equations (1), (2) reveals the underlying physics of multiple scattering in terms of corresponding pure $2 N$ and genuine $3 N$ transitions. The set (1), (2) is solved in a perturbation approach in powers of $V_{4}$. The various orders in $V_{4}$ are summed up by the Padé method. For general background, details of the formalism and the numerical performance we refer to Refs. [5,6,11,12].

We solved the set (1), (2) using the mesonexchange Bonn B potential [2] as the $N N$ interaction. The $3 N F$ was chosen to be the $2 \pi$-exchange three-nucleon interaction in the form proposed by the Tucson-Melbourne collaboration [4]. Its effect depends on the value of the cut-off parameter $\Lambda_{\pi}$ in the strong $\pi-N N$ formfactor. We performed calculations taking the "standard" value [6] $\Lambda_{\pi}=5.8 \mu$ ( $\mu=139.6 \mathrm{MeV}$ ) and also with $\Lambda_{\pi}=4.55 \mu$. The first one leads together with the Bonn B potential to overbinding the triton by about 2 MeV . The $T M$ $3 N F$ using the second value of $\Lambda_{\pi}$ together with the Bonn B potential reproduces the experimental triton binding energy. In our calculations both the $2 N$ and the 3 N forces were allowed to act in all partial wave states with total two-body subsystem angular momenta $j \leq 2$. Such a restriction does not lead to a completely convergent results at the energy of the present study. We know that $j=3 N N$-force components influence noticeably some observables at this


Fig. 1. Cross section and analyzing power $A_{y}$ for the collinearity configurations at $E_{p}^{\text {lab }}=65 \mathrm{MeV}$, (a) $\left(\boldsymbol{\vartheta}_{1}=20.0^{\circ}, \vartheta_{2}=116.2^{\circ}, \varphi_{12}=\right.$ $180.0^{\circ}$ ), (b) ( $30.0^{\circ}, 98.0^{\circ}, 180.0^{\circ}$ ), (c) ( $45.0^{\circ}, 75.6^{\circ}, 180.0^{\circ}$ ) and (d) $\left(59.5^{\circ}, 59.5^{\circ}, 180.0^{\circ}\right)$ as a function of the arc-length $S$ along the kinematical curve. The full dots show our experimental data [9,10]. The dotted and dash-doted curves are the theoretical predictions obtained using the Bonn B potential with 2 N -angular momentum space limited to $j \leq 3$ and $j \leq 2$, respectively. The dashed and solid curves result when in addition to the Bonn B potential $(j \leq 2)$ the $T M 3 N F$ is included with the cut-off parameter $\Lambda_{\pi}=5.8 \mu$ and $\Lambda_{\pi}=$ $4.55 \mu$, respectively. The arrows show the exact position where the collinearity condition is fulfilled.


Fig. 2. The same as Fig. 1 but for the pp-QFS configuration at (a) ( $44.0^{\circ}, 44.0^{\circ}, 180.0^{\circ}$ ) and (b) (30.0 ${ }^{\circ}, 59.5^{\circ}, 180.0^{\circ}$ ). The arrows show the exact position where the QFS condition is fulfilled.
energy. However, it is sufficient to get a first insight into the magnitudes of possible $3 N F$ effects. In order to see the magnitude of $j=3$ contributions we performed also calculations with the Bonn B potential only taking into account all $j \leq 3$ partial waves.

## 3. Comparison with experiment and conclusions

The fully converged theory obtained with different $N N$ interactions only have been presented in our previous papers [9,10]. Results obtained with the Bonn B potential are showed in this study in figures by the dotted lines. All measured cross sections and analyzing powers are compared to the theoretical predictions evaluated in a "point-like" geometry. This makes sense since for the chosen configurations the finite geometry and resolution effects of the experimental setup are negligible. For a more detailed discussion we refer to [9,10].
Comparison of the predictions obtained without and with the $T M 3 N F$ using $\Lambda_{\pi}=5.8 \mu$ shows that the $3 N F$ effects depend significantly on the configuration and the region along the kinematical curve. The large effects (up to about $25 \%$ ) are seen in the region of
collinearity (Fig. 1). The significantly smaller effects (about $2 \%$ ) appear in case of the QFS configurations - Fig. 2. Practically everywhere the inclusion of the $T M 3 N F$ increases the cross section for the collinearity configurations - the new theoretical values overestimate the measured ones. For the QFS case the cross section is decreased slightly around the maximum but still staying above the data.

Taking the value $\Lambda_{\pi}=4.55 \mu$ for the TM 3NF, which together with the Bonn B potential reproduces the triton binding energy, reduces the $3 N F$ effects and makes them nearly negligible, especially in case of the QFS configurations.

The vector analyzing powers in all six studied configurations are more influenced by the TM 3NF than the corresponding cross sections. The effects are also cut-off dependent and even in case of $\Lambda_{\pi}=4.55 \mu$ they can be seen. However, in nearly all cases the inclusion of the TM $3 N F$ increases disagreement between the theory and the experimental data.

Summarizing, we have found that the size of the TM 3NF effects in the $p d$ breakup at the energy of $E_{p}=65 \mathrm{MeV}$ are strongly cut-off dependent. For the value of the cut-off parameter $\Lambda_{\pi}=4.55 \mu$, which re-
produces the experimental triton binding energy, these effects are negligible for both cross sections and analyzing powers for QFS configurations, and are very small for collinearity configurations. In nearly all cases inclusion of the TM 3NF brings theory away from the measured values - some improvement can be seen only in the cross section of the collinearity configuration ( $20^{\circ}, 116^{\circ}, 180^{\circ}$ ).

It should be, however, pointed out that the TM 3NF was not derived in the same theoretical framework as the Bonn B potential. It would be interesting to find out how far this incompatibility is important by performing calculations with both $N N$ and $3 N F$ forces derived consistently in the same theoretical framework as e.g. in [13]. Such a work is under way.

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## References

(1) C.H. Hajduk, P.U. Sauer and W. Struewe, Nucl. Phys. A 405 (1983) 581;
Y. Wu, S. Ishikawa and T. Sasakawa, Few-Body Systems 15 (1993) 145;
A. Picklesimer, R.A. Rice and R. Brandemburg, Phys. Rev. C 45 (1992) 2045;
J.L. Friar et al., Phys. Lett. B 311 (1993) 4;
W. Glöckle, H. Witała, H. Kamada, D. Hüber and J. Golak, accepted for publication in Few-Body Systems Suppl.
[2] R. Machleidt, Adv. Nucl. Phys. 19 (1989) 189.
[3] R. Machleidt, private communication.
[4] S.A. Coon, M.D. Scadron, P.C. McNamee, B.R. Barret, D.W.E. Blatt and B.H.J. McKellar, Nucl. Phys. A 317 (1979) 242;
S.A. Coon and W. Glöckle, Phys. Rev. C 23 (1981) 1790.
[5] H. Witała, T. Cornelius and W. Glöckle. Few-Body Systems 3 (1988) 123.
[6] D. Hüber, H. Witała and W. Glöckle, Few-Body Systems 14 (1993) 171.
[7] W. Glöckle, H. Witała, H. Kamada, D. Hüber and J. Golak. AIP Conference Proceedings No. 334 of the 14th Conference Few-Body Problems in Physics, Williamsburg, Virginia, USA, 45 (1994), ed. F. Gross, and references therein.
[8] U. van Kolck, Phys. Rev. C 49 (1994) 2932, and references therein.
[9] M. Allet, K. Bodek, W. Hajdas, J. Lang, R. Müller, O. Naviliat-Cuncic, J. Sromicki, J. Zejma, L. Jarczyk, St. Kistryn, J. Smyrski, A. Strzałkowski, W. Glöckle, J. Golak, H. Witała, B. Dechant. J. Krug and P.A. Schmelzbach, Phys. Rev. C 50 (1994) 602.
[10] M. Allet. K. Bodek, W. Hajdas, J. Lang, R. Müller, O. Naviliat-Cuncic, J. Sromicki, J. Zejma, L. Jarczyk, St. Kistryn, J. Smyrski, A. Strzałkowski, W. Glöckle, J. Golak, D. Hüber, H. Kamada and H. Witała, accepted for publication in Few-Body Systems.
[11] W. Glöckle, The Quantum Mechanical Few-Body Problem (Springer-Verlag, Berlin, 1983).
[12] W. Glöckle, Lecture Notes in Physics 3 (1987) 273.
[13] M. Gari, private communication.


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