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# How to obtain the adhesive strength for double lap joint by using single lap joint

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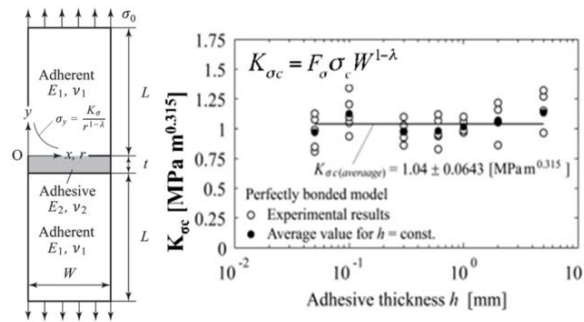
**Abstract.** The testing method of adhesive strength of lap joint is prescribed in Japanese Industrial Standard (JIS K6850). However, it has been reported that the strength of double lap joint (DLJ) is about two times larger than the one of single lap joint (SLJ). Therefore, suitable testing method has been required from industries. In this study, the equivalent conditions of strength for SLJ and DLJ are investigated in terms of the intensity of singular stress field (ISSF) appearing at the interface end. First, in order to minimize the bend effect for SLJ, the effect of the specimen geometry on ISSF and deformation angle at the interface corner is considered under the same adhesive geometry and load P. It is found that the minimum ISSF of SLJ can be obtained when the adherend thickness  $t_1$  is large enough, and the deformation angle at interface corner is also smallest when adherend thickness  $t_1$  is large enough. Therefore, it is necessary to use the specimen with thicker adherend thickness. Then, the equivalent conditions of strength for SLJ and DLJ is investigated by changing adherend thickness. The results show that the strength of the DLJ in JIS ( $t_1=1.5\text{mm}$ ) can be obtained by using the SLJ with adherend thickness  $t_1=7\text{mm}$ . When the adherend thickness  $t_1 \geq 25\text{mm}$ , the strength of SLJ is nearly equal to that of DLJ.

## 1. Introduction

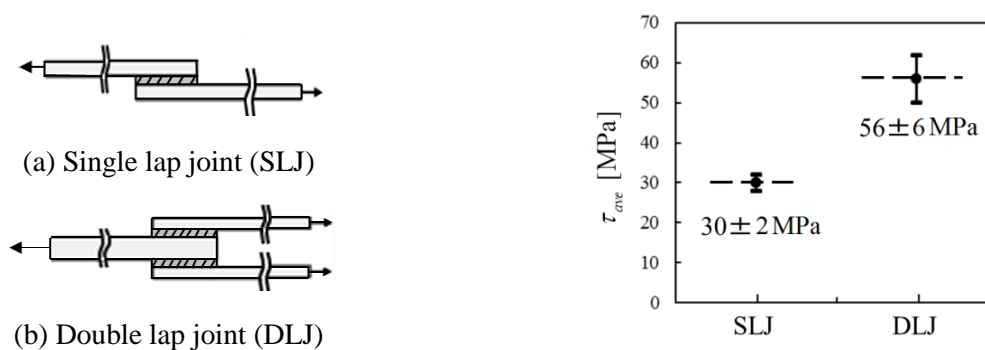
Since adhesively joints are economical, practical and easy to be used, they have been widely used in a variety of industries and a number of studies of adhesive joints have been made so far[1-4]. The authors investigated the adhesive butt joint strength in Figure 1 by changing the adhesive thickness and material combination [5]. It is found that the adhesive strength of butt joint can be expressed as the critical intensity of singular stress field (ISSF)  $K_{\sigma_c} = \text{const}$  [5]. The adhesive strength of single lap joint (SLJ) also can be expressed as  $K_{\sigma_c} = \text{const}$  [6],[7].

The testing methods for the adhesive strength of lap joints are standardized by Japanese Industrial standard (JIS) [8]. Compared with double lap joint (DLJ), SLJ can be used conveniently. However, the shear strength of DLJ in Figure 2(a) is about two times larger than the one of SLJ in Figure 2(b) (see Figure 3) [9]. Therefore, in this study, the equivalent conditions of strength for SLJ and DLJ are investigated in terms of the ISSF.





**Figure 1.** Adhesive strength expressed as  $K_{\sigma_c} = \text{const}$  for butt joint.



**Figure 2.** Two kinds of lap joint specimens.

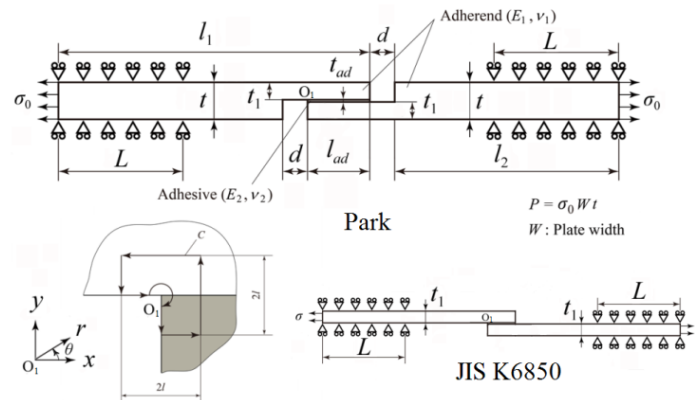
**Figure 3.** Adhesive shear strength for SLJ and DLJ (Adherend: S45C, Adhesive: Epoxy).

**2. Pure shear testing to minimize  $K_{\sigma, \lambda_1}$**

Figure 4 shows the schematic illustration of the analysis models. It has been reported that the singularity exists near the interface corner, and the singularity depending on the singular indexes  $\lambda_1$  and  $\lambda_2$  at the interface. In this paper,  $\lambda_1 = 0.6062$ ,  $\lambda_2 = 0.9989$ . The stress  $\sigma_\theta$  at  $r$  direction ( $\theta = 0$ ) can be expressed as follows. The notation  $r$  denotes the radial distance away from the corner singular point  $O_1$ .

$$\sigma_\theta = \frac{K_{\sigma, \lambda_1}}{r^{1-\lambda_1}} + \frac{K_{\sigma, \lambda_2}}{r^{1-\lambda_2}} \cong \frac{K_{\sigma, \lambda_1}}{r^{1-\lambda_1}} (1 + C_\sigma r^{\lambda_2 - \lambda_1}) \tag{1}$$

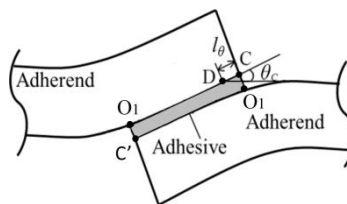
Here,  $K_{\sigma, \lambda_1}$  and  $K_{\sigma, \lambda_2}$  are ISSFs. The values of  $K_{\sigma, \lambda_1}$  and  $K_{\sigma, \lambda_2}$  can be obtained by using the method presented in [6-7]. The ISSF can be represented with only  $K_{\sigma, \lambda_1}$  since  $C_\sigma$  is almost constant expressed as  $C_\sigma = -5.321 \pm 0.338$ .



**Figure 4.** Analysis model and boundary condition.

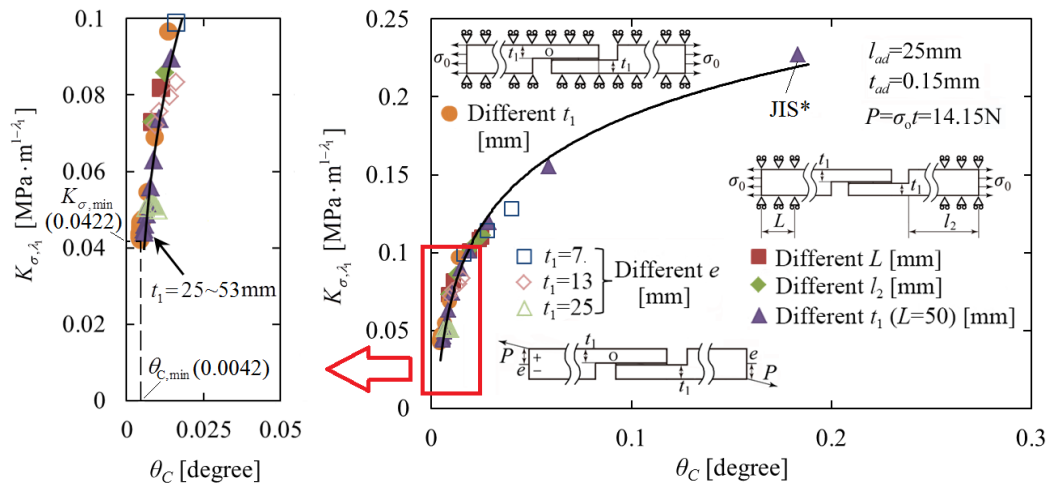
The butt joint in Figure 1 is used to obtain the adhesive strength under pure tension [5] and the SLJ in Figure 2 is used to obtain the adhesive strength under pure shear. However, due to the deformation of SLJ during testing, the peeling force is applied to the adhesive region. Then the  $K_{\sigma, \lambda_1}$  at the interface corner is affected by the peeling force. Since the single lap joint testing should be done under pure shear loading, smaller  $K_{\sigma, \lambda_1}$  is desirable. Therefore, in order to minimize the  $K_{\sigma, \lambda_1}$ , the effect of the specimen geometry is considered under the same adhesive geometry and load  $P$  based on the specimen used by Park [10] in Figure 4 (Adherend: Aluminum alloy 6061-T6, Adhesive: FM73M epoxy). The total length of the specimen is 225mm, adhesive length  $l_{ad} = 25$ mm, adhesive thickness  $t_{ad} = 0.15$ mm,  $d = 10$ mm,  $P = 14.15$ N.  $L$  is fixed boundary length,  $t_1$  is adherend thickness.

Figure 5 shows the deformation near the interface corner. In this study, the deformation angle at interface corner C will be considered to explain the deformation. Here, the deformation angle  $\theta_c$  is considered by using the maximum  $\theta_c$  since the value of maximum  $\theta_c$  is almost constant independent of element sizes.



**Figure 5.** Deformation angle at corner edge C.

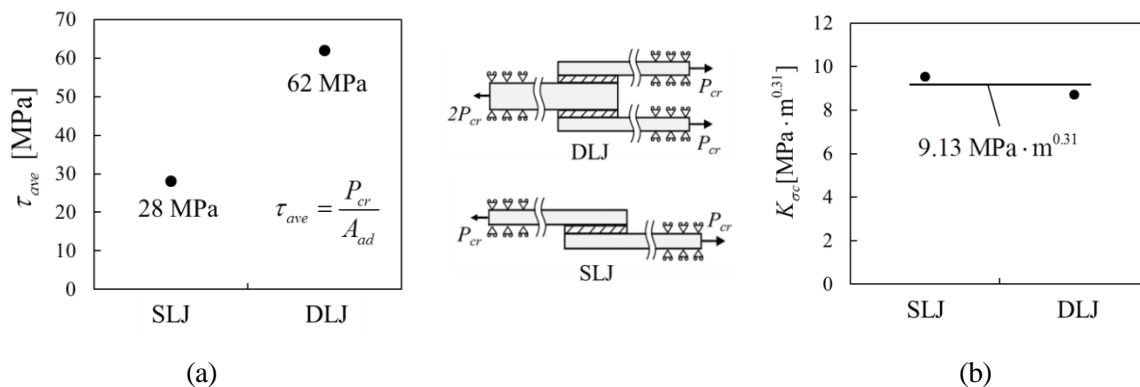
The relationship between the ISSF  $K_{\sigma, \lambda_1}$  and deformation angle  $\theta_c$  for three types of models is shown in Figure 6. It is found that the  $K_{\sigma, \lambda_1}$  decreases with decreasing  $\theta_c$ . This means that the changing of the ISSF can be explained by the deformation angle at the interface corner. Here, the minimum ISSF of SLJ can be obtained when  $t_1$  is large enough ( $t_1 \geq 25$ mm), and the deformation angle at interface corner is also smallest when  $t_1$  is large enough ( $t_1 \geq 25$ mm). The possible reason of minimum  $K_{\sigma, \lambda_1} \neq 0$  is the existence of local surface deformation at the interface corner even for very large thickness. Therefore, it is necessary to use thick adherend.



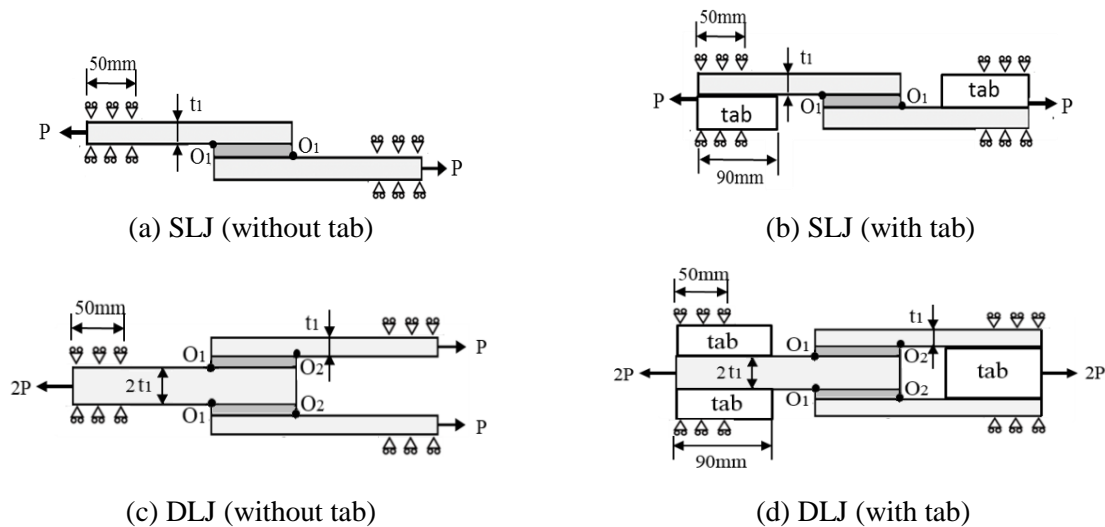
**Figure 6.** Relationship between  $K_{\sigma, \lambda_i}$  and  $\theta_C$ .

### 3. Equivalent conditions of strength for lap joints in terms of ISSF

The experimental results show that the strength of DLJ is about two times larger than the one of SLJ (see Figure 7(a)) [9]. However, the critical ISSF  $K_{\sigma_c}$  of SLJ is almost the same as the  $K_{\sigma_c}$  of DLJ (see Figure 7(b)). Therefore, in this chapter, the equivalent conditions of strength for the DLJ and SLJ in Figure 8 are investigated in terms of the ISSF  $K_{\sigma, \lambda_i}$ . Here, based on the conclusions in chapter 2, the effect of the adherend thickness on the  $K_{\sigma, \lambda_i}$  is considered. Since end tab is often bonded at the ends of experimental specimens to reduce bend effect when loaded, the influence of the tab on  $K_{\sigma, \lambda_i}$  is also considered in this chapter. The same material as adherend is used for tab. The total length of the specimen is 225mm, tab length is 90mm, adhesive length  $l_{ad}=25\text{mm}$ , adhesive thickness  $t_{ad}=0.15\text{mm}$ ,  $P=14.15\text{N}$ .

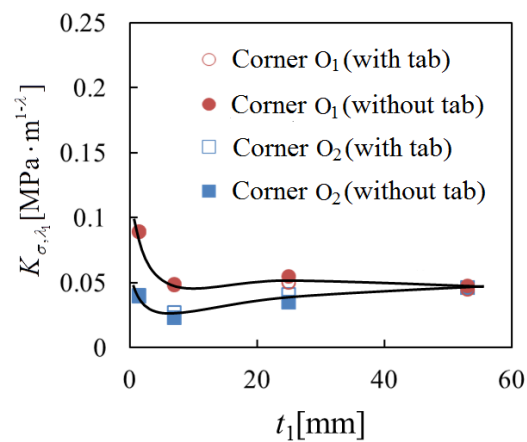


**Figure 7.** (a) Average shear strengths of SLJ and DLJ, (b)  $K_{\sigma_c}$  of SLJ and DLJ (Adherend: S45C, Adhesive: Epoxy B).



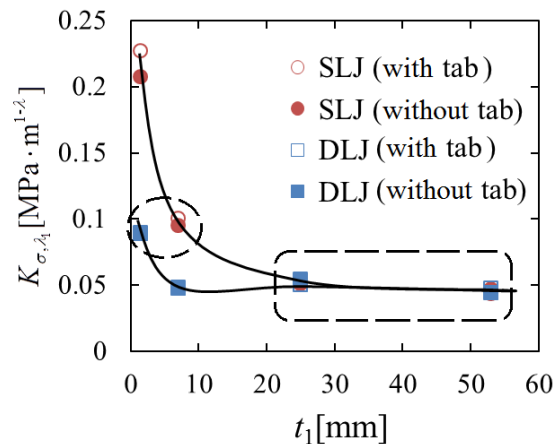
**Figure 8.** Models of SLJ and DLJ.

For DLJ, the  $K_{\sigma, \lambda_1}$  at interface corner  $O_1$  is not equal to the  $K_{\sigma, \lambda_1}$  at interface corner  $O_2$ . Figure 9 shows the results of  $K_{\sigma, \lambda_1}$  at interface corners  $O_1$  and  $O_2$ . It is found that the  $K_{\sigma, \lambda_1}$  for the specimen with tab is nearly equal to the  $K_{\sigma, \lambda_1}$  for the specimen without tab, the  $K_{\sigma, \lambda_1}$  at corner  $O_1$  is large than that at corner  $O_2$ . Therefore, the fracture may occur at corner  $O_1$  during testing. For this reason, the equivalent conditions of strength for SLJ and DLJ will be considered by using the  $K_{\sigma, \lambda_1}$  at corner  $O_1$ .



**Figure 9.** Results of DLJ (see Figure 8(c),(d)).

Figure 10 shows the results of  $K_{\sigma, \lambda_1}$  at interface corner  $O_1$  with different adherend thickness  $t_1$  for SLJ and DLJ. It is found that the  $K_{\sigma, \lambda_1}$  for the specimen with tab is nearly equal to the  $K_{\sigma, \lambda_1}$  for the specimen without tab, the  $K_{\sigma, \lambda_1}$  decreases with increasing  $t_1$ . When  $t_1 \geq 25$ mm, the minimum  $K_{\sigma, \lambda_1}$  can be obtained and the minimum  $K_{\sigma, \lambda_1} \approx 0$ . At that time, the bend effect is minimized, the possible reason of minimum  $K_{\sigma, \lambda_1} \neq 0$  is the existence of local surface deformation at the interface corner even for very large thickness. In JIS, the adherend thickness  $t_1 = 1.5$ mm (see Figure 4). The strength of DLJ with  $t_1 = 7$ mm is nearly equal to that of DLJ with  $t_1 = 1.5$ mm (JIS) since the  $K_{\sigma, \lambda_1}$  of SLJ and DLJ are nearly the same. For the same reason, the strength of SLJ is nearly equal to that of DLJ when  $t_1 \geq 25$ mm.



**Figure 10.** Comparison of SLJ and DLJ at corner  $O_1$ (see Figure 8(a)-(d)).

#### 4. Conclusion

- (1) The minimum ISSF of SLJ can be obtained when  $t_1$  is large enough, and the deformation angle at interface corner is also smallest when  $t_1$  is large enough.
- (2) The strength of SLJ with  $t_1=7\text{mm}$  is nearly equal to that of DLJ with  $t_1=1.5\text{mm}$  (JIS) since the ISSFs of SLJ and DLJ are nearly the same. For the same reason, the strength of SLJ is nearly equal to that of DLJ when  $t_1 \geq 25\text{mm}$ .

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