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# Suitable pitch difference to realize anti-loosening performance for various bolts-nuts diameter

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**Abstract.** In bolt-nut connection, the anti-loosening performance and high fatigue strength are always required with low cost to ensure the connected structure's safety. In the previous study, a suitable pitch difference between the bolt-nut was obtained as  $\alpha = 33 \mu\text{m}$  for M16 JIS bolt-nut through loosening experiment and FEM simulation for tightening process. However, other bolt-nut diameters have not been considered yet. In this paper, therefore, suitable pitch difference is considered for various diameters to realize anti-loosening performance. Since bolt-nut thread geometries are different depending on the diameter, they are expressed as approximate formula. Then, loosening force and anti-loosening force are considered by varying the diameter. Finally, suitable pitch difference  $\alpha_{min}^{suit} < \alpha < \alpha_{max}^{suit}$  was determined from mechanical condition.

## 1. Introduction

In a wide industrial field, bolt-nut joint is unitized as a machine element and is of great importance. However, the anti-loosening and anti-damage performances are always required. When vibration is added, the rotational loosening force on the spiral shape of the screw becomes larger than the friction between the screw surfaces, then the loosening occurs. Most previous studies have been mainly focusing on anti-loosening performance [1-4]. Only a few studies contribute toward improving fatigue strength [5-7]. To improve both the fatigue life and the performance of anti-loosening, a slight pitch difference between bolt and nut was previously proposed [8-12]. Then, the anti-loosening performance was confirmed for M16 bolt-nut connection by using FEM simulation as well as experiment [13-15]. However, other bolt-nut diameters have not been considered yet. Therefore, in this paper, the anti-loosening will be studied for different bolt-nut diameter to clarify the suitable pitch difference theoretically and experimentally. This special nut may improve the fatigue strength [13-15] without using additional components. Moreover, this special nut can be manufactured just by changing feed speed of a numerical control (NC) lathe.

## 2. Effect of the pitch difference on the rotation

### 2.1. Bolt-nut specimens

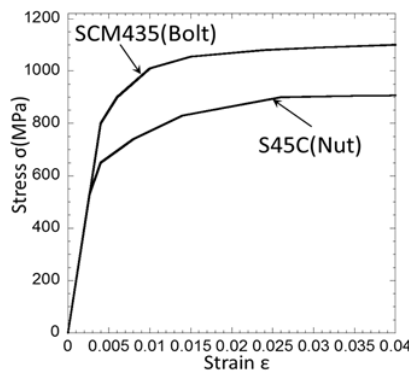
Japanese Industrial Standard (JIS) M16 bolt-nut connections with strength grade 8.8 are employed. The bolt material is chromium- molybdenum steel SCM435, and the nut material is medium carbon steel S45C quenched and tempered, whose properties are indicated in table 1, and whose stress-strain curves are shown in figure 1, respectively. The normal M16 bolt and nut have the same pitch



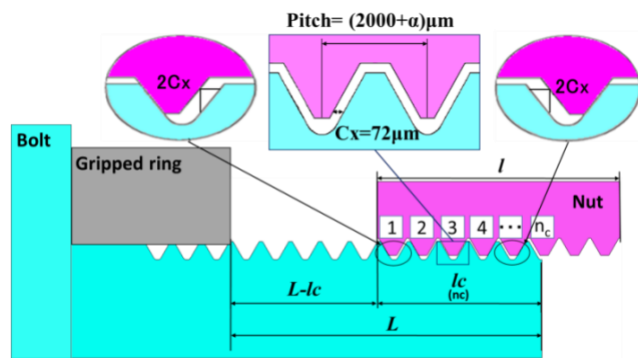
dimension as  $2000 \mu\text{m}$ . Herein, the nut pitch is assumed to be  $(2000+\alpha) \mu\text{m}$ . Figure 2 shows a contact status between bolt and nut threads during the tightening process. Notation  $C_x$  is the horizontal clearances between bolt and nut.

**Table 1.** Material properties of bolt and nut.

	Young's modulus (GPa)	Poisson's ratio	Yield strength (MPa)	Tensile strength (MPa)
SCM435 (Bolt)	206	0.3	800	1200
S45C (Nut)	206	0.3	530	980



**Figure 1.** Stress strain relation for SCM435 and S45C.



**Figure 2.** Schematic diagram of bolted joint.

### 2.2. Occurrence condition of $T_p$

Notation  $l_c$  is defined as the distance where the bolt-nut threads contact takes place, which can be obtained geometrically as shown in equation (1)

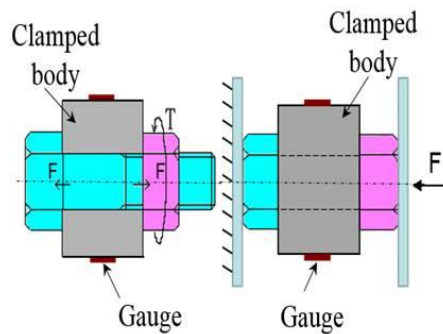
$$(n_c - 1)\alpha = 2C_x$$

$$C_x = \frac{C_y}{\tan \theta}, \quad l_c = n_c p \quad (1)$$

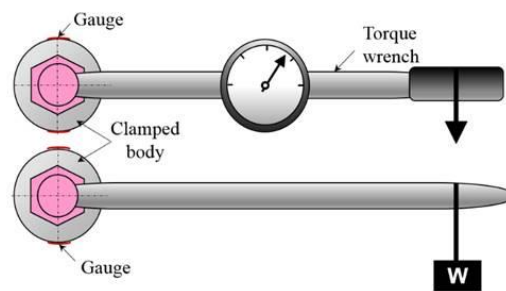
In equation (1),  $p$  is the pitch of bolt (for example,  $p=2 \text{ mm}$  for M16),  $\alpha$  is the pitch difference,  $n_c$  is the number of nut thread in contact in figure 2 except for  $n=1$ ,  $\theta$  is the thread angle ( $=60^\circ$ ) and  $C_x$  and  $C_y$  are the horizontal and vertical clearances between bolt and nut threads. Note that equation (1) is valid when  $n_c < 8$  which is the total nut threads number 8 and the nut length  $< 16 \text{ mm}$ .

### 2.3. Pitch difference $\alpha$ vs prevailing torque

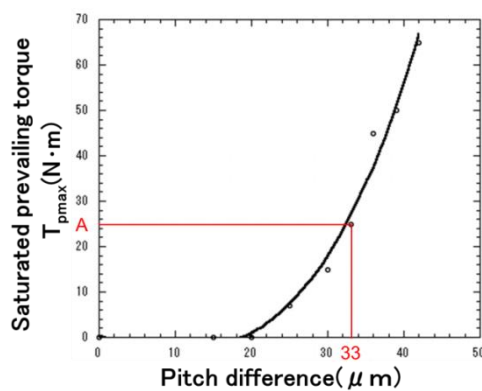
To obtain the relationship between torque and clamping force, the torque was controlled by using an electric torque wrench, and the clamping force was measured by using the strain gauge attached to the clamped body surface as shown in figure 3. The uniaxial strain gauge with a length of 2 mm KFG-2 (Kyowa Electronic Instruments Co., Ltd.) was used in this measurement. Before the experiments, calibration tests were performed by compressing the clamped body to obtain the relationship between the clamping force and surface strain as shown in figure 3. Similar tests were performed to calibrate the torque wrench as shown in figure 4.



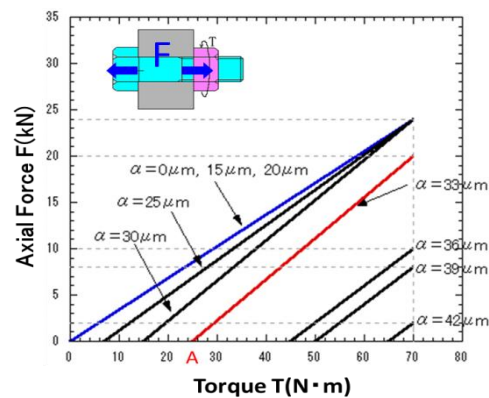
**Figure 3.** Calibration method for bolt axial force measurement.



**Figure 4.** calibration method for torque wrench.



**Figure 5.** Relationship between torque and Pitch difference (M16).



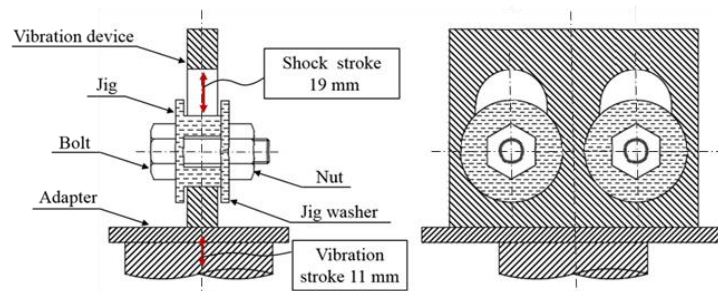
**Figure 6.** Relationship between torque and axial force (M16).

Figure 5 shows the prevailing torque  $T_p$  when the nut rotation is large enough by varying the pitch difference. From figure 5, it is seen that saturated prevailing torque  $T_p$  is nearly proportional to the pitch difference  $\alpha$  in the range of  $15 \mu\text{m} < \alpha < 42 \mu\text{m}$ . Figure 6 shows the tightening torque vs clamping force experimentally obtained. When  $\alpha = 0 \sim 30 \mu\text{m}$ , the torque–clamping force relationship is the same as the one of  $\alpha = 0 \mu\text{m}$ . When  $\alpha = 33 \mu\text{m}$ , the prevailing torque of  $25 \text{ N}\cdot\text{m}$  is required before the nut touches the clamped plate. Under the same tightening torque of  $70 \text{ N}\cdot\text{m}$ , the clamping force was reduced to  $20 \text{ kN}$ . When  $\alpha = 39 \mu\text{m}$ , under a torque of  $70 \text{ N}\cdot\text{m}$  the axial force decreased significantly to  $8 \text{ kN}$ , which was only  $1/3$  of the axial force of  $\alpha = 0 \mu\text{m}$ .

### 3. Loosening experiment

#### 3.1. Device and conditions

The bolt-axial force  $24 \text{ kN}$  was considered for the standard bolt–nut, and the corresponding tightening torque was  $70 \text{ N}\cdot\text{m}$ . It is tighten ring that insert to bolt at  $70 \text{ N}\cdot\text{m}$  for nut. And experiment machine is built up. Also an extra length is  $10 \text{ mm}$ . As shown in figure 7, the experimental device was an impact-vibration testing machine based on NAS3350 (National Aerospace Standard), whose vibration frequency was about  $30 \text{ Hz}$ , and vibration acceleration is  $20 \text{ g}$ . The maximum vibration cycle of NAS3350 is  $30\,000$ , therefore, if the number of vibration cycles was over  $30\,000$ , the anti-loosening performance may be considered to be good enough.



**Figure 7.** Loosening experimental device based on NAS3350.

### 3.2. Results

Table 2 lists the number of cycles for the start loosening and the nut dropping. Table 2 also lists the prevailing torque measured in the loosening experiments and the bolt axial forces estimated from figure 6. For each pitch difference  $\alpha$ , two specimens were tested. For  $\alpha=0 \mu\text{m}$  and  $\alpha = 15 \mu\text{m}$ , the nuts dropped at about 1000 cycles. For  $\alpha = 33 \mu\text{m}$ , no loosening was observed until 30 000 cycles and prevailing torque was  $25 \text{ N}\cdot\text{m}$ . For  $\alpha = 42 \mu\text{m}$ , no loosening was observed until 30 000 cycles although the axial force was estimated to be only  $1\sim 4 \text{ kN}$ . It may be concluded that if  $\alpha$  is too small, the anti-loosening cannot be expected and if  $\alpha$  is too large, the clamping ability is not good enough. By considering both the anti-loosening and clamping abilities,  $\alpha=33\sim 42 \mu\text{m}$  can be selected as the most suitable pitch difference.

**Table 2.** Anti-loosening Performance (M16).

Pitch difference $\alpha(\mu\text{m})$	Cycles for dropping	Prevailing torque ( $\text{N}\cdot\text{m}$ )	Axial force(kN)
0	751	0	24
	876		
15	813	0	24
	1528		
33	30000	25	14~24
	30000		
42	30000	67	1~4
	30000	57	

## 4. Suitable pitch difference for various bolt-nut diameter

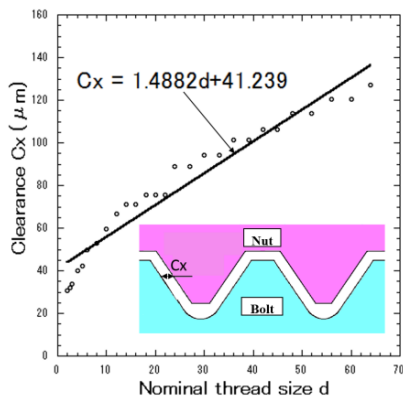
### 4.1. How to estimate suitable pitch difference

In this section, suitable pitch difference will be considered for various thread nominal diameters. First bolt-nut geometries are different depending on the diameter. Figure 8 shows JIS clearance  $C_x$  between the bolt and nut threads by varying nominal thread diameter  $d$ . It is seen that the clearance  $C_x$  can be expressed as equation (2)

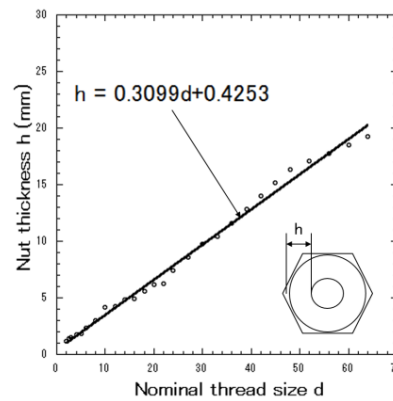
$$C_x = 1.4882d + 41.239 \quad (2)$$

Similarly, figure 9 shows JIS nut thickness  $h$  by varying nominal thread diameter  $d$ . In this study, we have to estimate loosening force  $F_l$  which is closely related to the volume of the nut. Then,  $h$  is an important dimension. It is seen that nut thickness can be expressed as equation (3).

$$h = 0.3099d + 0.4253 \quad (3)$$



**Figure 8.** Relationship between Nominal thread size  $d$  and Clearance  $C_x$ .



**Figure 9.** Relationship between Nut size  $d$  and Nut thickness  $h$ .

In the following discussion, loosening force  $F_l$  and anti-loosening force  $F_a$  are assumed. Figure 10 shows the relationship between  $F_l$  and  $F_a$ . On the one hand, loosening force  $F_l$  can be proportional as equation (4) since  $F_l$  should be proportional to the nut weight.

$$F_l \propto \gamma V \cong \gamma(\pi d)hl \tag{4}$$

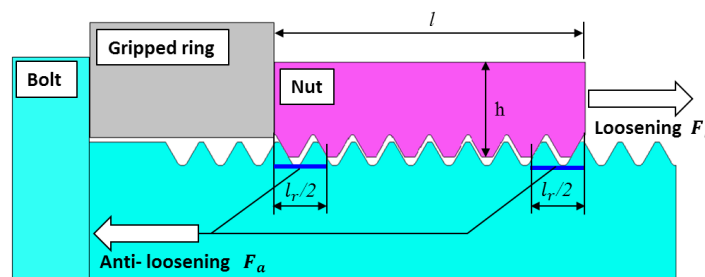
Here,  $\gamma$ = specific gravity,  $V$ = the volume of nut,  $l$ = the length of nut.

On the other hand, anti-loosening force  $F_a$  should be proportional to be contact surface area between the nut and bolt threads.

$$F_a \propto \tau_s(\pi d)l_r \tag{5}$$

In equation (6)  $\tau_s$  = average shear stress between the nut and bolt threads, and  $l_r$  is the length of the nut threads in contact in figure 10. Therefore, loosening condition can be expressed as equation (6) assuming loosening and anti-loosening forces should be balanced.

$$F_l = KF_a \tag{6}$$



**Figure 10.** Relationship between loosening force  $F_l$  and anti-loosening force  $F_a$ .

Therefore, we have

$$\gamma(\pi d)hl = K\tau_s(\pi d)l_r, = \frac{\gamma hl}{\tau_s l_r} = \frac{\gamma}{\tau_s} K', K' = \frac{lh}{l_r} \tag{7}$$

Here,  $K$  and  $K'$  are proportional constants. From figure 2 and equation (1) by using equation (7), the number of nut thread in contact in figure 2 will be expressed since  $n_c$  is important for anti-loosening.

$$l_r = \frac{lh}{K'}$$

From figure 2 with equation (1)

$$l_r = l - l_c = l - n_c p \quad (8)$$

$$n_c = n \left( 1 - \frac{h}{K'} \right) \quad (9)$$

From table 2, suitable prevailing torque range to prevent loosening can be expressly as  $30 < T_p < 60$  for M16. Similarly, suitable pitch difference can be expressed as  $\alpha_{min}^{suit} = 34 \mu m < \alpha^{suit} < \alpha_{max}^{suit} = 41 \mu m$ . From equation (1), we have  $\alpha = 2C_x / (n_c - 1)$ . Assume  $n_{c max}$  is the number of nut threads for  $\alpha_{min}^{suit}$  and  $n_{c min}$  is the number of nut threads for  $\alpha_{max}^{suit}$ . Then,

$$n_{c max} = n \left( 1 - \frac{h}{K'_{max}} \right) \quad (10)$$

$$n_{c min} = n \left( 1 - \frac{h}{K'_{min}} \right) \quad (11)$$

Here,  $K'_{max}$  is the proportional constant for  $\alpha_{min}^{suit}$  and  $K'_{min}$  is the proportional constant for  $\alpha_{max}^{suit}$ . Therefore, generally, the suitable  $\alpha$  can be expressed as

$$\frac{2C_x}{n_{c max} - 1} < \alpha < \frac{2C_x}{n_{c min} - 1} \quad (12)$$

By substituting equation (8) into (9),

$$\frac{2C_x}{n \left( 1 - \frac{h}{K'_{max}} \right) - 1} < \alpha < \frac{2C_x}{n \left( 1 - \frac{h}{K'_{min}} \right) - 1} \quad (13)$$

Since the values of the proportional constants  $K$  and  $K'$  are unknown, in this study, the loosening experimental results for M16 in table 2 is used. From  $\alpha_{min}^{suit} = 34 \mu m < \alpha^{suit} < \alpha_{max}^{suit} = 41 \mu m$  for M16 with  $C_x = 72 \mu m$ , equation (14) is obtained by using equation (1).

$$4.5 \leq n_c \leq 5.2 \quad (14)$$

By substituting  $n_{c max}$  and  $n_{c min}$  into (8), we have

$$5.6 \leq l_r \leq 7 \quad (15)$$

Here, For M16 bolt–nut connection, substituting by  $l = 16 \text{ mm}$ ,  $h = 5 \text{ mm}$ (M16), equations (2) and (3).

$$K'_{min} = 11.4 \leq K' \leq K'_{max} = 14.3 \quad (16)$$

Assumed this  $K'_{max}$  and  $K'_{min}$  can be for various nominal thread diameter. By using equation (2) and equation (3) into (13)

$$\frac{2.9764d+82.478}{n \left( 1 - \frac{0.3099d+0.4253}{14.3} \right) - 1} < \alpha < \frac{2.9764d+82.478}{n \left( 1 - \frac{0.3099d+0.4253}{11.4} \right) - 1} \quad (17)$$

**Table 3.** Suitable pitch difference estimated for M12~M16.

Diameter	Pitch $p$ (mm)	Nut length $l$ (mm)	Number of threads $n$	Nut thickness $h$ (mm)	Clearance $C_x$ ( $\mu$ m)	Suitable Pitch difference range $\alpha$ ( $\mu$ m)
M12	1.75	10	5.7	4.1	59.1	$38.6 < \alpha < 44.8$
M14	2	11	5.5	4.8	62.1	$46.5 < \alpha < 56.4$
M16	2	13	6.5	5.4	65.1	$42.6 < \alpha < 53.5$
	2	16	8	5.4	65.1	$32.6 < \alpha < 40.4$

#### 4.2. Validity of equation (17)

Suitable pitch difference can be estimated by using equation (17). Table 3 shows suitable pitch difference obtained from equation (17) for M12~M16 bolt-nut connection. As an example, for M12 the suitable  $\alpha$  can be expressed as  $38.6 \mu\text{m} < \alpha < 44.8 \mu\text{m}$ . By using Junker vibration test, we have confirmed that  $\alpha = 40 \mu\text{m}$  have no loosening equation (17) is valid. Therefore, the validity of equation (17) is confirmed for M12.

### 5. Conclusion

In the previous study, a suitable pitch difference between the bolt-nut was obtained as  $\alpha = 33 \mu\text{m}$  for M16 JIS bolt-nut through loosening experiment and FEM simulation for tightening process. In this paper, suitable pitch difference was considered for other nominal thread diameters to realize anti-loosening performance. Suitable pitch difference was determined by assuming that loosening force should be balanced to the anti-loosening force. Then, the suitable pitch difference was expressed as approximate formula. By using Junker vibration test, we have confirmed that the proposed formula is valid for M12 since  $\alpha = 40 \mu\text{m}$  have no loosening equation (17) is valid.

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