




# Applying Center Loss to Multidimensional Feature Space in Deep Neural Networks for Open-Set Recognition

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Keywords: Open-Set Recognition, Neural Networks, Image Classification, Unknown Class

Abstract: With the advent of deep learning, significant improvements in image recognition performance have been achieved. In image recognition, it is generally assumed that all the test data are composed of known classes. This approach is termed as closed-set recognition. In closed-set recognition, when an untrained, unknown class is input, it is recognized as one of the trained classes. The method whereby an unknown image is recognized as unknown when it is input is termed as open-set recognition. Although several open-set recognition methods have been proposed, none of these previous methods excel in terms of all three evaluation items: learning cost, recognition performance, and scalability from closed-set recognition models. To address this, we propose an open-set recognition method using the distance between features in the multidimensional feature space of neural networks. By applying center loss to the feature space, we aim to maintain the classification accuracy of closed-set recognition and improve the unknown detection performance. In our experiments, we achieved state-of-the-art performance on the MNIST, SVHN, and CIFAR-10 datasets. In addition, the proposed approach shows excellent performance in terms of the three evaluation items.


## 1 INTRODUCTION


With the advent of deep learning, image recognition performance has improved dramatically and has also been reported to surpass the image recognition performance of a human (He et al., 2016). When tested, most existing image recognition methods assume that all the input images belong to known classes. Thus, they can classify the known classes; however, when an unknown class is input, these methods classify it as one of the known classes. This type of image recognition is called closed-set recognition. By contrast, when an unknown class is input, the image recognition method that recognizes it as an unknown is termed as open-set recognition (Scheirer et al., 2013).


Figure 1 shows the difference between closed-set recognition and open-set recognition. For the dataset distribution shown in (a), closed-set recognition, shown in (b), calculates a hyperplane that separates each class suitably. However, in open-set recog-

niton, shown in (c), an exact region for each class is set; the region that does not belong to any class, termed as the open space, is also set. The features that appear in this open space are recognized as an unknown class.

Deep learning-based open-set recognition can be classified into two categories: discriminative model-based methods and reconstruction model-based methods. The discriminative model-based method involves low learning costs and is easily scalable as its architecture remains the same as that of closed-set recognition models; nevertheless, its recognition performance is low. By contrast, the recognition performance of reconstruction model-based methods is higher than that of the discriminative model-based methods; however, the learning costs are higher and the architecture differs significantly from that of closed-set recognition methods. This makes it difficult to develop an open-set recognition method that employs closed-set recognition models. Image recognition is often used in embedded systems, where it becomes necessary to train additional unknown classes. Therefore, an open-set recognition model with low

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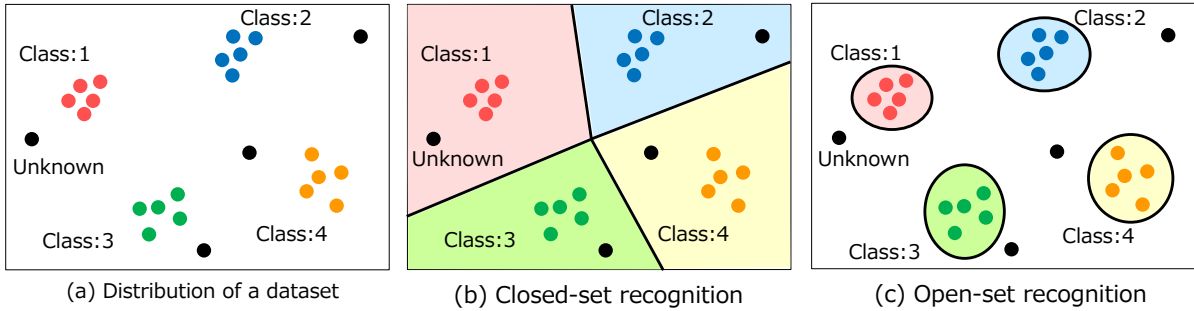


Figure 1: Comparison of closed-set recognition and open-set recognition.

training costs and high recognition performance is required. In addition, if the pre-trained closed-set recognition models can be scaled up to open-set recognition via fine tuning, the learning costs can be reduced. Consequently, it is necessary to develop an open-set recognition method with low learning costs, high recognition performance, and scalability from closed-set recognition.

Anomaly detection is a research topic similar to open-set recognition. In a previous study on anomaly detection, a method using the feature space of a recognition model pre-trained on ImageNet (Deng et al., 2009), which is a large-scale image dataset, was proposed (Rippel et al., 2020). This study confirmed that normal images and anomaly images appear at different positions in a multidimensional feature space.

Deep metric learning is generally used for face recognition (Wang and Deng, 2021). In face recognition, there are few changes in the features between classes; therefore, deep metric learning generates a feature space with a bias between the classes by imposing constraints on a feature space, such that features of the same class are located near each other, whereas features of different classes are located far away. Deep metric learning methods such as contrastive-loss (Chopra et al., 2005) and triplet-loss (Wang et al., 2014) are well known. However, the disadvantage of these methods is that they require a pair of classes to be created from the dataset during training; this results in high learning costs as the number of classes increases. Center loss (Wen et al., 2016) is a loss function used in face recognition. Center loss acts as a constraint to keep features of the same class close in a given batch during training. Center loss is not classified as deep metric learning based on its properties. It has achieved high performance in the field of face recognition. In addition, unlike contrastive loss, center loss does not require a pair of classes to be created from the dataset during training. Thus, it is easier to incorporate into problems other than face recognition.

In this paper, we propose an open-set recognition method that focuses on the multidimensional feature space formed in the middle layer of neural networks. Using center loss for a multidimensional feature space during training, the distance between features of each class in a feature space is made vacant. In the multidimensional feature space of the trained classifier, clusters are formed at a certain distance for each class. When an unknown class is input, it is expected to appear at a different location from the clusters of each class within the multidimensional feature space. Thus, we propose a method that calculates the distance between each cluster and a feature of the input image; this approach estimates a class if the distance is within a set threshold and recognizes as unknown class if it exceeds the threshold.

## 2 RELATED STUDIES

### 2.1 Open-Set Recognition

Open-set recognition can be realized via traditional machine learning-based methods using SVM (Scheirer et al., 2013) and the nearest neighbor methods (Mensink et al., 2013) or via deep learning-based methods (Geng et al., 2020). In this paper, we discuss deep learning-based methods, which are the most popular approaches and exhibit high recognition performance.

#### 2.1.1 Discriminative Model (DM)-Based Methods

Discriminative model-based methods generally use the probability distribution of each class output from the classifier (Hendrycks and Gimpel, 2017; Bendale and Boult, 2016). Figure 2 presents a block diagram of discriminative model-based methods. For example, softmax-threshold recognizes an unknown class if the maximum probability of the output probability distri-

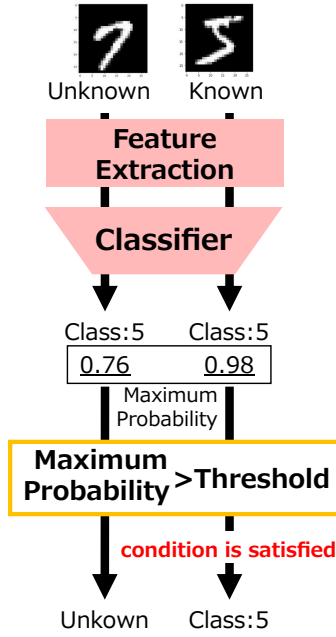


Figure 2: Block diagram of discriminative model-based methods

bution of each class exceeds a set threshold; alternatively, it estimates a class if this maximum probability is less than the threshold (Hendrycks and Gimpel, 2017). The structure of this method is almost identical to that of closed-set recognition models; it offers the advantage of low learning costs but suffers from the disadvantage of a low recognition performance.

### 2.1.2 Reconstructive Model (RM)-Based Methods

In reconstruction model-based methods, a decoder is installed in the model to reconstruct the input image and calculate the reconstruction error (Yoshihashi et al., 2019; Perera et al., 2020; Sun et al., 2020). Figure 3 depicts the block diagram of reconstruction model-based methods. If the calculated reconstruction error exceeds a set threshold, a classifier recognizes it as an unknown; however, if this error is lower than the threshold, the classifier estimates it as a class. Although this method affords higher recognition performance than discriminative model-based methods, it suffers from the disadvantage of higher learning costs because the reconstruction network needs to be added to the closed-set recognition model.

## 2.2 Anomaly Detection Using Multidimensional Feature Space

The anomaly detection method proposed by Rippe et al. focuses on the multidimensional feature

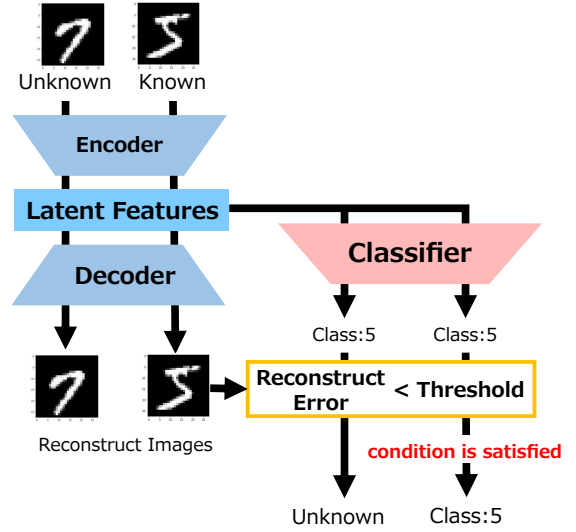


Figure 3: Block diagram of reconstructive model-based methods

space obtained from each middle layer of EfficientNet (Tan and Le, 2019) pre-trained using ImageNet (Deng et al., 2009) (Rippel et al., 2020). Figure 4 presents the block diagram of the anomaly detection method. This method is performed without re-training the pre-trained model. First, the multivariate Gaussian distribution of normal images is obtained by applying Gaussian fitting to the multidimensional features obtained from the middle layer, when normal images of the training data are input. During testing, the Mahalanobis distance between the multidimensional features when the image is input and the multivariate Gaussian distribution obtained from the normal images of the training data are calculated. If the Mahalanobis distance is within the set threshold, the image is classified as a normal image; however, if it exceeds the threshold, it is classified as an anomaly image. During verification using MVTEC-AD (Bergmann et al., 2021), which is a dataset for anomaly detection, a higher score was achieved, as compared to previous anomaly detection methods.

## 2.3 Center Loss

Center loss is a loss function used for face recognition. A model with center loss learns the center point of each class of features in a multidimensional feature space and penalizes the distance between features and the center point of the class. In this manner, a biased feature space is formed for each class. Equation 1 shows the loss function of the center loss, where  $m$  is the batch size,  $\mathbf{x}_i$  denotes the features of the input data in the feature space, and  $\mathbf{c}_{y_i}$  is the center point of class

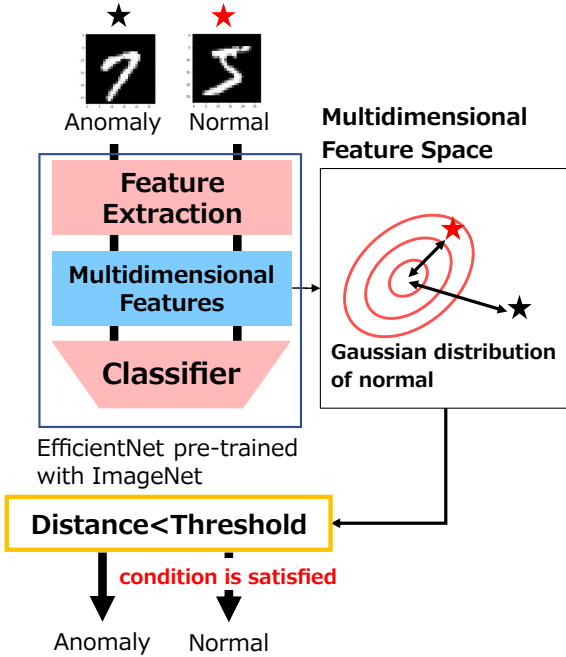


Figure 4: Block diagram of anomaly detection using multidimensional feature space

$y_i$  in the feature space.

$$L_c = \frac{1}{2} \sum_{i=1}^m \|x_i - c_{y_i}\|_2^2 \quad (1)$$

Equation 2, 3 shows the update formula for the center point  $c_j$  of class  $j$ , Where  $t$  is a learning step, and  $\alpha$  is a hyperparameter. Further,  $\delta(\text{condition}) = 1$  if the condition is satisfied; otherwise,  $\delta(\text{condition}) = 0$ .

$$c_j^{t+1} = c_j^t - \alpha \cdot \Delta c_j^t \quad (2)$$

$$\Delta c_j = \frac{\sum_{i=1}^m \delta(y_i = j) \cdot (c_j - x_i)}{1 + \sum_{i=1}^m \delta(y_i = j)} \quad (3)$$

Accordingly, the loss is calculated using Equation 1, and the center point of each class is updated based on Equation 2, 3. Based on the benchmarks conducted by the authors on face recognition datasets, high performance was confirmed even on small datasets. This also proves that the loss function is easier to optimize, as compared to the previous loss functions used for face recognition.

### 3 PROPOSED METHOD

In this paper, we propose an open-set recognition method using the multidimensional feature space of neural networks. We train the neural network on a

dataset comprising only known classes, as in the case of closed-set recognition. During training, center loss is applied to the middle layer, immediately before the output layer of the neural network. In a multidimensional feature space, features of the unknown class are expected to appear at different positions from features of the trained classes. By applying center-loss to the multidimensional feature space, the distance between features of the trained classes can be shortened, so that features of the unknown class appear farther from features of the trained classes compared to the case where center-loss is not applied. We also calculate the cross-entropy loss for the probability distributions of each class, which is the final output. The sum of these values is used in training as the loss of the neural network. Next, the training data are input to the trained neural network, and multivariate Gaussian fitting is performed on the clusters of each class that appear in the feature space.

Figure 5 shows the block diagram for testing. First, the test data are input, and the classes are estimated. Next, we calculate the Mahalanobis distance between the multivariate Gaussian distribution of the estimated classes and the test data. Equation 4 presents the formula for calculating the Mahalanobis distance  $d(\mathbf{x})$ . Here,  $\mathbf{x}$  is a feature in the multidimensional feature space, and  $\boldsymbol{\mu}_i$  and  $\boldsymbol{\Sigma}_i$  are the mean and covariance matrix of the multivariate Gaussian distribution of an estimated class  $i$ , respectively.

$$d(\mathbf{x}) = \sqrt{(\mathbf{x} - \boldsymbol{\mu}_i)^T \boldsymbol{\Sigma}_i^{-1} (\mathbf{x} - \boldsymbol{\mu}_i)} \quad (4)$$

When the distance of the 95% confidence interval of the multivariate Gaussian distribution is set as the threshold, the model recognizes class as an unknown if the distance exceeds this threshold.

### 4 EXPERIMENT

We verified the performance of the proposed method on three datasets: MNIST (LeCun et al., 2010), SVHN (Netzer et al., 2011), and CIFAR-10 (Krizhevsky, 2012). All of these are 10-class datasets. In open-set recognition, the model is only trained on certain classes of the dataset; the untrained classes are then tested as unknown classes, and the performance is evaluated using macro-F1 scores. Similarly, in this experiment, we trained the model on 6 randomly selected classes out of the 10 classes in each dataset; the remaining 4 classes were used as unknown classes. We calculated the mean and standard deviation of the scores after five trials. All of our experiments were conducted using AI Bridging Cloud Infrastruc-

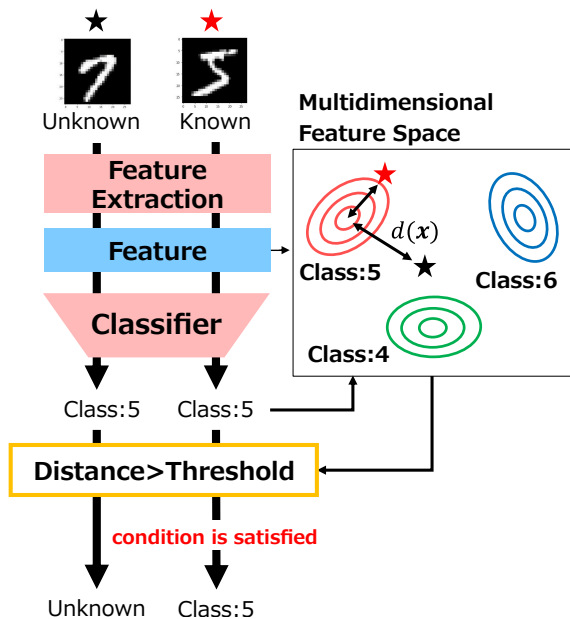


Figure 5: Block diagram of proposed method

ture provided by National Institute of Advanced Industrial Science and Technology. The model was trained for about 2 hours using 8 cores of Intel Xeon Platinum 8360Y Processor 2.4 GHz, NVIDIA A100 with 40GB and 32GB RAM. The experimental conditions are shown in Table 1.

Table 2 presents the experimental results. The scores of the comparison methods were obtained from (Sun et al., 2020). The experimental results indicate that the proposed method achieves better scores than the previous methods on all the datasets.

## 5 DISCUSSION

The proposed method outperformed the previous methods on all the datasets; compared to the previous methods, it achieved 6 points higher on the MNIST dataset but only 2 points higher on the SVHN and CIFAR-10 datasets. MNIST is a grayscale handwritten character dataset; hence, there is little difference in the shapes of the recognition targets within the same class; moreover, the color surrounding the recognition targets remains constant. By contrast, SVHN and CIFAR-10 are datasets created from actual environments; hence, the shapes of the recognition targets vary within the same class, and the surroundings of the recognition targets are also different. Hence, the low score is attributed to the large variance in the multidimensional feature space of the neural network. This suggests that center loss is not as effec-

tive as MNIST for these datasets. Therefore, changing the method to apply the multidimensional feature space may be effective for these datasets. Therefore, we conclude that the proposed method is highly effective when the recognition target is simple.

Table 3 presents the evaluation results of the proposed method in terms of three evaluation items: learning cost, recognition performance, and scalability from previous closed-set recognition. The learning cost is expected to be affected by the multivariate Gaussian fitting and the center loss computation that were additionally introduced to the network. Multivariate Gaussian fitting involves low computational costs because it can be performed by inputting all the training data into the model just once. On introducing center loss to the network, the number of additional trainable parameters was only 5,120; by contrast, the number of trainable parameters in ResNet34 used in the experiment was approximately 20 million. Therefore, we concluded that the effects of introducing these additional computations on the learning cost were significantly small. With regard to the recognition performance, we achieved a score exceeding those of all the previous methods. Finally, the extension from the closed-set recognition models is highly effective because it only employs the multidimensional feature space formed in the middle layer of the classifier and does not alter the structure of the classifier. To summarize, the proposed method is superior to the previous approaches in terms of the three evaluation items.

## 6 FUTURE WORKS

In the future, we aim to improve the recognition performance of the proposed method and to further research incremental learning for open-world recognition.

In this study, we applied center loss to the middle layer. However, in the field of facial recognition, several loss functions have been proposed that do not require the creation of class pairs on datasets, similar to the center loss (Deng et al., 2019; Liu et al., 2017; Wang et al., 2018). A model with center loss learns to locate features of the same class near each other; however, a model with these methods can learn to locate features of different classes situated far away in the multidimensional feature space. Therefore, by changing the loss function applied in the middle layer, the recognition performance can be improved. The threshold for recognition as an unknown class was determined based on the confidence interval. Therefore, the unknown recognition performance can be

Table 1: Experiment condition

Network	ResNet34(He et al., 2016)
Training epochs	300
Number of dimensions of multidimensional feature space	512
Optimization method for cross-entropy loss	Adam
Optimization method for center loss	SGD

Table 2: Macro-F1 scores

	Method	MNIST	SVHN	CIFAR-10
DM-based methods	Softmax (Hendrycks and Gimpel, 2017)	0.768 $\pm$ 0.008	0.725 $\pm$ 0.012	0.600 $\pm$ 0.037
	Openmax (Bendale and Boulton, 2016)	0.798 $\pm$ 0.018	0.737 $\pm$ 0.011	0.623 $\pm$ 0.038
RM-based methods	CROSR (Yoshihashi et al., 2019)	0.803 $\pm$ 0.013	0.753 $\pm$ 0.019	0.668 $\pm$ 0.013
	GDFR (Perera et al., 2020)	0.821 $\pm$ 0.021	0.716 $\pm$ 0.010	0.700 $\pm$ 0.024
	CGDL (Sun et al., 2020)	0.837 $\pm$ 0.055	0.776 $\pm$ 0.040	0.655 $\pm$ 0.023
	Proposed method	<b>0.901 <math>\pm</math> 0.021</b>	<b>0.780 <math>\pm</math> 0.006</b>	<b>0.715 <math>\pm</math> 0.019</b>

improved by using a different threshold determination method, instead of the traditional anomaly detection.

The open-set recognition proposed herein does not learn the additional classes recognized as unknown classes. The recognition method that includes incremental learning, whereby classes recognized as unknown in open-set recognition are additionally learned, is termed as open-world recognition (Bendale and Boulton, 2015). In the future, we aim to study and apply incremental learning for the proposed open-set recognition.

## 7 CONCLUSION

In this work, we developed and verified an open-set recognition method using the Mahalanobis distance in the multidimensional feature space formed at the middle layer of a neural network. We applied center loss to the middle layer during training; consequently, features of the same class were located near each other in the multidimensional feature space. The experimental results show that the proposed method achieves better scores than state-of-the-art methods on all datasets (i.e., MNIST, SVHN, and CIFAR-10). In addition, the proposed method achieves better results than the previous methods in terms of three metrics: learning cost, recognition performance, and scalability from closed-set recognition models. In the future, we plan to further improve the recognition performance and research open-world recognition.

## ACKNOWLEDGMENT

This paper is based on results obtained from a project, JPNP16007, commissioned by the New En-

ergy and Industrial Technology Development Organization (NEDO).

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Table 3: Performance in terms of three evaluation items

	DM model-based methods	RM model-based methods	Proposed method
Learning cost	<b>Low</b>	<b>High</b>	<b>Low</b>
Recognition performance	Low	<b>High</b>	<b>High</b>
Scalability from closed-set recognition models	○	×	○

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